



GLOBAL VAN-CONG EFFECTIVE KINETIC, GRAVITATIONAL POTENTIAL, AND TOTAL ENERGIES, OBTAINED IN THE PLANET-SUN INTERACTION SYSTEM, AND ENHANCED BY OUR EMPIRICAL GLOBAL EFFECTIVE KINETIC MASS OF THE PLANET, EXPRESSED AS A FUNCTION OF ANY SPEED (OR ANY RELATIVITY) (38)

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ABSTRACT

In this work, we present the new expressions of global effective kinetic, gravitational potential and total energies, obtained in the planet-sun interaction systems, as those given in Equations (4, 5, 6), and enhanced by a new global effective kinetic mass of the planet, as that given in Eq. (1). Some concluding remarks are given as follows. At the low speed v ($\ll c$), c being the light speed, given in the non-relativistic case, they are found to be correct. At $v=c$, given in the relativistic case, the kinetic energy is found to be equal to: $m \times c^2 \times \left[\frac{2+p}{4} \right]$, $p > 0$, and, in particular, for $p=2$, to: $m \times c^2$, in good agreement with that proposed by Einstein in 1905 [1], m being the rest mass of the planet, as those shown in Tables 2-10, for various planet-sun interaction systems.

KEYWORDS: Global effective kinetic-potential-total energies, global effective kinetic mass, light speed, relativity, non-relativity.

First of all, from the expression of the kinetic energy of the planet, with its rest mass m , in motion with a speed v , being equal to the light speed c , $\frac{2m \times c^2}{2}$, and proposed by Einstein in 1905^[1-3], we propose a **global effective kinetic mass**, valid at any v , by^[4]:

$$m^*(v; p > 0) = m \times \left(1 + p \times \frac{v^2}{c^2}\right), \quad (1)$$

increasing with increasing v and noting that at lowest v : $m^*(v; p) \simeq m$, given in the non-relativistic case, and then, at $v=c$, given in the relativistic case: $m^*(v=c; p) = m \times (1 + p)$. Here, the numerical results of m and c are given in Table 1 in Appendix 1.

Then, from Eq. (1), this planet is in motion, due to the **global effective Newton force**

$$F_{\text{GEN}}^*(v; p) \equiv m^*(v; p) \times \frac{dv}{dt} = m \times \left(1 + p \times \frac{v^2}{c^2}\right) \times \frac{dv}{dt}, \quad (2)$$

where $\frac{dv}{dt}$ is its acceleration. Further, it is attracted by the sun of the mass M , due to the **global effective gravitational force**, defined as:

$$F_{\text{GEG}}^*(v; p) \equiv -\frac{GMm^*(v; p)}{r^2} = -\frac{GMm \times \left(1 + p \times \frac{v^2}{c^2}\right)}{r^2}, \quad (3)$$

where r is the distance between the sun and the planet, and G is the universal gravitational constant, noting that the numerical values of M and G are given in Table 1 in Appendix 1.

From Eq. (2), noting that $\frac{dv}{dt} \times dr = v dv$, our **global effective kinetic energy** is defined by:

$$K^*(v; p) \equiv \int F_{\text{GEN}}^*(v; p) \times dr = \int m \times \left(1 + p \times \frac{v^2}{c^2}\right) \times v dv = m \times v^2 \times \left[\frac{2 + p \times \frac{v^2}{c^2}}{4}\right], \quad (4)$$

being reduced to the correct result at the lowest v ($\ll c$) as: $\frac{m \times v^2}{2}$, given in the non-relativistic case, and at $v=c$, to: $K_o(p) \equiv m \times c^2 \times \left[\frac{2+p}{4}\right]$, and for $p=2$, to: mc^2 , for example, as that proposed by Einstein in the relativistic case [1].

Further, from Eq. (3), our global effective gravitational energy, $U^*(v, r; p)$, is defined by:

$$U^*(v, r; p) \equiv -\int_{\infty}^r F_{\text{GEG}}^*(v; p) \times dx \equiv -\int_{\infty}^r -\frac{GMm^*(v; p)}{x^2} dx = -\frac{GMm^*(v; p)}{r} = -\frac{GMm \times \left(1 + p \times \frac{v^2}{c^2}\right)}{r},$$

being reduced to the correct result at the lowest v ($\ll c$) as: $= -\frac{GMm}{r}$, given in the non-relativistic case, and at $v=c$, to: $-\frac{GMm \times (1+p)}{r}$, given in the relativistic case. Here, we choose:

$r = r_p$, being the distance from the planet to the sun at perihelion, and $v_p \leq v \leq c$, v_p being

The planet speed at perihelion, noting that the values of r_p and v_p are found to be given in Table 1 in Appendix 1. That gives :

$$U^*(v; p) = -\frac{GMm \times (1+p \times \frac{v^2}{c^2})}{r_p}, \quad (5)$$

according at $v=c$ to: $U_o(p) \equiv -\frac{GMm \times (1+p)}{r_p}$, given in the relativistic case.

Therefore, from Equations (4, 5), the **global effective total energy**, $E^*(v; p)$, is found to be given by:

$$E^*(v; p) \equiv m \times v^2 \times \left[\frac{2+p \times \frac{v^2}{c^2}}{4} \right] - \frac{GMm \times (1+p \times \frac{v^2}{c^2})}{r_p} \quad (6)$$

according at $v=c$ to: $E_o(p) = K_o(p) + U_o(p) = m \times v^2 \times \left[\frac{2+p}{4} \right] - \frac{GMm \times (1+p)}{r_p}$.

Furthermore, it is interesting to evaluate the relative errors between $K^*(v; p)$ and $E^*(v; p)$, defined by:

$$RE(v; p) \equiv 1 - \frac{E^*(v; p)}{K^*(v; p)}. \quad (7)$$

Then, in following Tables 2-10 in Appendix 1, the numerical results of $RE(v; p)$, $K^*(v; p)/K_o(p)$, $U^*(v; p)/U_o(p)$ and $E^*(v; p)/E_o(p)$ are obtained for $p=1, 2$ and 3 , respectively, using Equations (7, 4, 5, 6), noting that, for a given p , $RE(v; p)$ decreases with increasing v , and at $v=c$, one obtains $K^*(v; p) \cong E^*(v; p)$, with highest precision.

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APPENDIX 1

Table 1. The numerical results of the planetary parameters are given by: the rest planet mass, m (Kg), the distance from the planet to the sun at perihelion, r_p (m), and the planet speed at perihelion, $v_p \left(\frac{10^3 \times m}{s} \right)$. Further, the sun mass M , universal gravitational constant G , and light speed c , are found to be given respectively by : $M = 1.988475 \times 10^{30}$ kg, $G = 6.6743 \times 10^{-11} \frac{m^3}{kg \times s^2}$, and $c = 2.9979 \times 10^8 \left(\frac{m}{s} \right)$.

Celestial body	m (Kg)	r_p (m)	$v_p \left(\frac{10^3 \times m}{s} \right)$
Mercury	3.30101×10^{23}	4.60009×10^{10}	47.87
Venus	4.86732×10^{24}	1.07477×10^{11}	35.02
Earth	5.97219×10^{24}	1.47100×10^{11}	29.78
Mars	6.41693×10^{23}	2.06645×10^{11}	24.13
Jupiter	1.89852×10^{27}	7.40603×10^{11}	13.06
Saturn	5.68460×10^{26}	1.35096×10^{12}	9.64
Uranus	8.68192×10^{25}	2.73854×10^{12}	6.79
Neptune	1.02431×10^{26}	4.46384×10^{12}	5.43
Moon	7.34581×10^{22}	3.62106×10^8	1.03

Table 2. In the **Mercury-Sun interaction system**, in which the values of m , r_p and v_p are given in Table 1, the numerical results of $RE(v; p)$, $K^*(v; p)/K_o(p)$, $U^*(v; p)/U_o(p)$ and $E^*(v; p)/E_o(p)$, are obtained by using Equations (7, 4, 5, 6), respectively, noting that $v_p \leq v \leq c$.

$X(v)=v/c$	$RE(v; p)$	$K^*(v; p)/K_o(p)$	$U^*(v; p)/U_o(p)$	$E^*(v; p)/E_o(p)$
Here, for $p=1$ and at $v=c$, $K_o(p) = \left(\frac{3}{4}\right) \times mc^2 = 2.22506339 \times 10^{40}$ J, $U_o(p) = -1.90474291 \times 10^{33}$ J and $E_o(p) = 2.2250632 \times 10^{40}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $8.56039842 \times 10^{-8}$.				
0.00015968	2.51799115	$1.69984685 \times 10^{-8}$	0.50000001	$-2.58035269 \times 10^{-8}$
0.09	$7.95826684 \times 10^{-6}$	0.00542187	0.50405	0.00542183
0.30	$7.44085668 \times 10^{-7}$	0.0627	0.545	0.06269996
0.40	$4.30992282 \times 10^{-7}$	0.1152	0.58	0.11519996
0.60	2.0554629×10^{-7}	0.2832	0.68	0.28319997
0.80	$1.24636483 \times 10^{-7}$	0.5632	0.82	0.56319998

0.90	$1.02110987 \times 10^{-7}$	0.7587	0.905	0.75869999
0.95	$9.32589377 \times 10^{-8}$	0.87316875	0.95125	0.87316874
1	$8.56039842 \times 10^{-8}$	1	1	1

Here, for $p=2$ and at $v=c$, $K_o(p) = mc^2 = 2.96675118 \times 10^{40}$ J, in good agreement with that, proposed by Einstein in 1905, $U_o(p) = -2.85711437 \times 10^{33}$ J and $E_o(p) = 2.9667509 \times 10^{40}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $9.63044823 \times 10^{-8}$.

0.00015968	2.51799118	$1.27488515 \times 10^{-8}$	0.33333335	$-1.93526461 \times 10^{-8}$
0.09	$7.99013828 \times 10^{-6}$	0.00408281	0.33873333	0.00408277
0.30	$7.72283469 \times 10^{-7}$	0.04905	0.39333333	0.04904997
0.40	$4.56625013 \times 10^{-7}$	0.0928	0.44	0.09279997
0.60	$2.25554126 \times 10^{-7}$	0.2448	0.57333333	0.24479997
0.80	$1.39468061 \times 10^{-7}$	0.5248	0.76	0.52479998
0.90	$1.14736457 \times 10^{-7}$	0.73305	0.87333333	0.73304999
0.95	1.0488774×10^{-7}	0.85850312	0.935	0.85850312
1	$9.63044823 \times 10^{-8}$	1	1	1

Here, for $p=3$ and further at $v=c$, $K_o(p) = \frac{5}{4} mc^2 = 3.70843898 \times 10^{40}$ J, $U_o(p) = -3.80948582 \times 10^{33}$ J and $E_o(p) = 3.7084386 \times 10^{40}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $1.02724781 \times 10^{-7}$.

0.00015968	2.51799121	$1.01990814 \times 10^{-8}$	0.25000002	$-1.54821175 \times 10^{-8}$
0.09	$8.02144326 \times 10^{-6}$	0.00327937	0.256075	0.00327934
0.30	$7.98216299 \times 10^{-7}$	0.04086	0.3175	0.04085997
0.40	$4.78933581 \times 10^{-7}$	0.07936	0.37	0.07935997
0.60	$2.40877012 \times 10^{-7}$	0.22176	0.52	0.22175997
0.80	$1.49452109 \times 10^{-7}$	0.50176	0.73	0.50175998
0.90	1.2274127×10^{-7}	0.71766	0.8575	0.71765999
0.95	$1.12054385 \times 10^{-7}$	0.84970375	0.926875	0.84970374
1	$1.02724781 \times 10^{-7}$	1	1	1

Table 3. In the **Venus-Sun interaction system**, in which the values of m , r_p and v_p are given in above Table 1, the numerical results of $RE(v; p)$, $K^*(v; p)/K_o(p)$, $U^*(v; p)/U_o(p)$ and $E^*(v; p)/E_o(p)$, are obtained by using Equations (7, 4, 5, 6), respectively, noting that $v_p \leq v \leq c$.

$X(v)=v/c$	$RE(v; p)$	$K^*(v; p)/K_o(p)$	$U^*(v; p)/U_o(p)$	$E^*(v; p)/E_o(p)$
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Here, for $p=1$ and at $v=c$, $K_o(p) = \left(\frac{3}{4}\right) \times mc^2 = 3.28084299 \times 10^{41}$ J, $U_o(p) = -1.20207127 \times 10^{34}$ J and $E_o(p) = 3.28084287 \times 10^{41}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $3.66390978 \times 10^{-8}$.

0.00010681	2.4086972	7.60558411 × 10⁻⁹	0.50000001	-1.07139654 × 10⁻⁸
0.09	3.4061933×10^{-6}	0.00542187	0.50405	0.00542185
0.30	$3.18473817 \times 10^{-7}$	0.0627	0.545	0.06269998
0.40	1.8446768×10^{-7}	0.1152	0.58	0.11519998
0.60	$8.79752348 \times 10^{-8}$	0.2832	0.68	0.28319999
0.80	$5.33452774 \times 10^{-8}$	0.5632	0.82	0.56319999
0.90	$4.37042093 \times 10^{-8}$	0.7587	0.905	0.75869999
0.95	$3.99154708 \times 10^{-8}$	0.87316875	0.95125	0.87316875
1	$3.66390978 \times 10^{-8}$	1	1	1

Here, for $p=2$ and at $v=c$, $K_o(p) = mc^2 = 4.37445732 \times 10^{41}$ J, in good agreement with that, proposed by Einstein in 1905, $U_o(p) = -1.80310691 \times 10^{34}$ J and $E_o(p) = 4.37445714 \times 10^{41}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of 4.1218985×10^{-8} .

0.00010681	2.40869721	5.70418812 × 10⁻⁹	0.33333334	-8.03547421 × 10⁻⁹
0.09	$3.41976759 \times 10^{-6}$	0.00408281	0.33873333	0.00408279
0.30	$3.30536204 \times 10^{-7}$	0.04905	0.39333333	0.04904999
0.40	$1.95434843 \times 10^{-7}$	0.0928	0.44	0.09279999
0.60	$9.65368387 \times 10^{-8}$	0.2448	0.57333333	0.24479999
0.80	$5.96921278 \times 10^{-8}$	0.5248	0.76	0.52479999
0.90	$4.91070372 \times 10^{-8}$	0.73305	0.87333333	0.73304999
0.95	$4.48918005 \times 10^{-8}$	0.85850312	0.935	0.85850312
1	4.1218985×10^{-8}	1	1	1

Here, for $p=3$ and further at $v=c$, $K_o(p) = \frac{5}{4} \times mc^2 = 5.46807165 \times 10^{41}$ J, $U_o(p) = -2.40414255 \times 10^{34}$ J and $E_o(p) = 5.46807141 \times 10^{41}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $4.39669173 \times 10^{-8}$.

0.00010681	2.40869722	4.56335052 × 10⁻⁹	0.25000001	-6.42837949 × 10⁻⁹
0.09	$3.43323324 \times 10^{-6}$	0.00327937	0.256075	0.00327935
0.30	$3.41642102 \times 10^{-7}$	0.04086	0.3175	0.04085999
0.40	$2.04986888 \times 10^{-7}$	0.07936	0.37	0.07935999
0.60	$1.03097029 \times 10^{-7}$	0.22176	0.52	0.22175999

0.80	$6.39665372 \times 10^{-8}$	0.50176	0.73	0.50175999
0.90	5.2534×10^{-8}	0.71766	0.8575	0.71765999
0.95	$4.79600526 \times 10^{-8}$	0.84970375	0.926875	0.84970375
1	$4.39669173 \times 10^{-8}$	1	1	1

Table 4. In the **Earth-Sun interaction system**, in which the values of m , r_p and v_p are given in above Table 1, the numerical results of $RE(v; p)$, $K^*(v; p)/K_o(p)$, $U^*(v; p)/U_o(p)$ and $E^*(v; p)/E_o(p)$, are obtained by using Equations (7, 4, 5, 6), respectively, noting that $v_p \leq v \leq c$.

$X(v)=v/c$	$RE(v; p)$	$K^*(v; p)/K_o(p)$	$U^*(v; p)/U_o(p)$	$E^*(v; p)/E_o(p)$
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Here, for $p=1$ and at $v=c$, $K_o(p) = \left(\frac{3}{4}\right) \times mc^2 = 4.02558651 \times 10^{41}$ J, $U_o(p) = -1.07764768 \times 10^{34}$ J and $E_o(p) = 4.0255864 \times 10^{41}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $2.67699546 \times 10^{-8}$.

9.9336×10^{-5}	2.03466914	$6.57845405 \times 10^{-9}$	0.50	$-6.80652355 \times 10^{-9}$
0.09	$2.48869774 \times 10^{-6}$	0.00542187	0.50405	0.00542186
0.30	$2.32689398 \times 10^{-7}$	0.0627	0.545	0.06269999
0.40	$1.34779285 \times 10^{-7}$	0.1152	0.58	0.11519999
0.60	$6.42781395 \times 10^{-8}$	0.2832	0.68	0.28319999
0.80	$3.89761413 \times 10^{-8}$	0.5632	0.82	0.56319999
0.90	$3.19320006 \times 10^{-8}$	0.7587	0.905	0.7587
0.95	$2.91638005 \times 10^{-8}$	0.87316875	0.95125	0.87316875
1	$2.67699546 \times 10^{-8}$	1	1	1

Here, for $p=2$ and at $v=c$, $K_o(p) = mc^2 = 5.36744867 \times 10^{41}$ J, in good agreement with that, proposed by Einstein in 1905, $U_o(p) = -1.61647152 \times 10^{34}$ J and $E_o(p) = 5.36744851 \times 10^{41}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $3.01161989 \times 10^{-8}$.

9.9336×10^{-5}	2.03466915	$4.93384056 \times 10^{-9}$	0.33333334	$-5.10489275 \times 10^{-9}$
0.09	$2.49861564 \times 10^{-6}$	0.00408281	0.33873333	0.00408279
0.30	$2.41502648 \times 10^{-7}$	0.04905	0.39333333	0.04904999
0.40	$1.42792322 \times 10^{-7}$	0.0928	0.44	0.09279999
0.60	$7.05335813 \times 10^{-8}$	0.2448	0.57333333	0.24479999
0.80	$4.36133978 \times 10^{-8}$	0.5248	0.76	0.52479999
0.90	$3.58795175 \times 10^{-8}$	0.73305	0.87333333	0.73305
0.95	$3.27997012 \times 10^{-8}$	0.85850312	0.935	0.85850312
1	$3.01161989 \times 10^{-8}$	1	1	1

Here, for $p=3$ and further at $v=c$, $K_o(p) = \frac{5}{4} \times mc^2 = 6.70931084 \times 10^{41}$ J, $U_o(p) = -2.15529536 \times 10^{34}$ J and $E_o(p) = 6.70931063 \times 10^{41}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $3.21239455 \times 10^{-8}$.

9.9336 × 10⁻⁵	2.03466916	3.94707247 × 10⁻⁹	0.25000001	-4.08391427 × 10⁻⁹
0.09	2.50845418 × 10 ⁻⁶	0.00327937	0.256075	0.00327936
0.30	2.49617051 × 10 ⁻⁷	0.04086	0.3175	0.04085999
0.40	1.49771419 × 10 ⁻⁷	0.07936	0.37	0.07935999
0.60	7.5326712 × 10 ⁻⁸	0.22176	0.52	0.22175999
0.80	4.6736448 × 10 ⁻⁸	0.50176	0.73	0.50175999
0.90	3.83834731 × 10 ⁻⁸	0.71766	0.8575	0.71766
0.95	3.50414858 × 10 ⁻⁸	0.84970375	0.926875	0.84970375
1	3.21239455 × 10⁻⁸	1	1	1

Table 5. In the Mars-Sun interaction system, in which the values of m , r_p and v_p are given in above Table 1, the numerical results of $RE(v; p)$, $K^*(v; p)/K_o(p)$, $U^*(v; p)/U_o(p)$ and $E^*(v; p)/E_o(p)$, are obtained by using Equations (7, 4, 5, 6), respectively, noting that $v_p \leq v \leq c$.

$X(v)=v/c$	$RE(v; p)$	$K^*(v; p)/K_o(p)$	$U^*(v; p)/U_o(p)$	$E^*(v; p)/E_o(p)$
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Here, for $p=1$ and at $v=c$, $K_o(p) = \left(\frac{3}{4}\right) \times mc^2 = 4.32536587 \times 10^{40}$ J, $U_o(p) = -8.24248669 \times 10^{32}$ J and $E_o(p) = 4.32536579 \times 10^{40}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $1.90561606 \times 10^{-8}$.

8.0490 × 10⁻⁵	2.20605487	4.31905865 × 10⁻⁹	0.50	-5.20902183 × 10⁻⁹
0.09	1.77157655 × 10 ⁻⁶	0.00542187	0.50405	0.00542186
0.30	1.65639674 × 10 ⁻⁷	0.0627	0.545	0.06269999
0.40	9.59424754 × 10 ⁻⁸	0.1152	0.58	0.11519999
0.60	4.57563181 × 10 ⁻⁸	0.2832	0.68	0.28319999
0.80	2.77451202 × 10 ⁻⁸	0.5632	0.82	0.5632
0.90	2.27307571 × 10 ⁻⁸	0.7587	0.905	0.7587
0.95	2.07602171 × 10 ⁻⁸	0.87316875	0.95125	0.87316875
1	1.90561606 × 10⁻⁸	1	1	1

Here, for $p=2$ and at $v=c$, $K_o(p) = mc^2 = 5.7671545 \times 10^{40}$ J, in good agreement with that, proposed by Einstein in 1905, $U_o(p) = -1.236373 \times 10^{33}$ J and $E_o(p) = 5.76715437 \times 10^{40}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $2.14381807 \times 10^{-8}$.

8.0490 × 10⁻⁵	2.20605488	3.239294 × 10⁻⁹	0.33333334	-3.90676642 × 10⁻⁹
0.09	1.7786366 × 10 ⁻⁶	0.00408281	0.33873333	0.0040828
0.30	1.71913376 × 10 ⁻⁷	0.04905	0.39333333	0.04904999
0.40	1.01646547 × 10 ⁻⁷	0.0928	0.44	0.09279999
0.60	5.02092468 × 10 ⁻⁸	0.2448	0.57333333	0.24479999
0.80	3.10461459 × 10 ⁻⁸	0.5248	0.76	0.52479999
0.90	2.55407924 × 10 ⁻⁸	0.73305	0.87333333	0.73305
0.95	2.33484286 × 10 ⁻⁸	0.85850312	0.935	0.85850312

1	$2.14381807 \times 10^{-8}$	1	1	1	
Here, for $p=3$ and further at $v=c$, $K_o(p) = \frac{5}{4} \times mc^2 = 7.20894312 \times 10^{40}$ J, $U_o(p) = -1.64849734 \times 10^{33}$ J and $E_o(p) = 7.20894296 \times 10^{40}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $2.28673928 \times 10^{-8}$.					
8.0490	$\times 10^{-5}$	2.20605489	$2.59143521 \times 10^{-9}$	0.25	$-3.12541317 \times 10^{-9}$
0.09	$1.78564015 \times 10^{-6}$	0.00327937	0.256075	0.00327936	
0.30	$1.77689604 \times 10^{-7}$	0.04086	0.3175	0.04085999	
0.40	$1.06614608 \times 10^{-7}$	0.07936	0.37	0.07935999	
0.60	$5.36212312 \times 10^{-8}$	0.22176	0.52	0.22175999	
0.80	$3.32692857 \times 10^{-8}$	0.50176	0.73	0.50175999	
0.90	$2.73232301 \times 10^{-8}$	0.71766	0.8575	0.71766	
0.95	$2.49442406 \times 10^{-8}$	0.84970375	0.926875	0.84970375	
1	$2.28673928 \times 10^{-8}$	1	1	1	

Table 6. In the **Jupiter-Sun interaction system**, in which the values of m , r_p and v_p are given in above Table 1, the numerical results of $RE(v; p)$, $K^*(v; p)/K_o(p)$, $U^*(v; p)/U_o(p)$ and $E^*(v; p)/E_o(p)$, are obtained by using Equations (7, 4, 5, 6), respectively, noting that $v_p \leq v \leq c$.

$X(v)=v/c$	$RE(v; p)$	$K^*(v; p)/K_o(p)$	$U^*(v; p)/U_o(p)$	$E^*(v; p)/E_o(p)$	
Here, for $p=1$ and at $v=c$, $K_o(p) = \left(\frac{3}{4}\right) \times mc^2 = 1.27970753 \times 10^{44}$ J, $U_o(p) = -6.80433307 \times 10^{35}$ J and $E_o(p) = 1.27970752 \times 10^{44}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $5.31710009 \times 10^{-9}$.					
4.3564	$\times 10^{-5}$	2.10128052	$1.26520474 \times 10^{-9}$	0.50	$-1.39334534 \times 10^{-9}$
0.09	$4.94309957 \times 10^{-7}$	0.00542187	0.50405	0.00542187	
0.30	$4.62172181 \times 10^{-8}$	0.0627	0.545	0.0627	
0.40	$2.67701222 \times 10^{-8}$	0.1152	0.58	0.1152	
0.60	$1.27670483 \times 10^{-8}$	0.2832	0.68	0.2832	
0.80	$7.74151654 \times 10^{-9}$	0.5632	0.82	0.5632	
0.90	$6.34239572 \times 10^{-9}$	0.7587	0.905	0.7587	
0.95	$5.79257042 \times 10^{-9}$	0.87316875	0.95125	0.87316875	
1	$5.31710009 \times 10^{-9}$	1	1	1	

Here, for $p=2$ and at $v=c$, $K_o(p) = mc^2 = 1.7062767 \times 10^{44}$ J, in good agreement with that, proposed by **Einstein in 1905**, $U_o(p) = -1.02064996 \times 10^{36}$ J and $E_o(p) = 1.70627669 \times 10^{44}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $5.98173766 \times 10^{-9}$.

4.3564	$\times 10^{-5}$	2.10128052	$9.48903557 \times 10^{-10}$	0.33333333	$-1.04500901 \times 10^{-9}$
0.09	$4.96279871 \times 10^{-7}$	0.0040828	0.33873333	0.0040828	
0.30	$4.79677231 \times 10^{-8}$	0.04905	0.39333333	0.04905	

0.40	$2.83616872 \times 10^{-8}$	0.0928	0.44	0.0928
0.60	$1.40095162 \times 10^{-8}$	0.2448	0.57333333	0.2448
0.80	$8.66257732 \times 10^{-9}$	0.5248	0.76	0.5248
0.90	7.1264592×10^{-9}	0.73305	0.87333333	0.73305
0.95	$6.51474008 \times 10^{-9}$	0.85850312	0.935	0.85850312
1	$5.98173766 \times 10^{-9}$	1	1	1

Here, for $p=3$ and further at $v=c$, $K_o(p) = \frac{5}{4} \times mc^2 = 2.13284588 \times 10^{44}$ J, $U_o(p) = -1.36086661 \times 10^{36}$ J and $E_o(p) = 2.13284586 \times 10^{44}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $6.38052022 \times 10^{-9}$.

4.3564×10^{-5}	2.10128052	$7.59122846 \times 10^{-10}$	0.25	$-8.36007211 \times 10^{-10}$
0.09	$4.98234019 \times 10^{-7}$	0.00327937	0.256075	0.00327936
0.30	$4.95794213 \times 10^{-8}$	0.04086	0.3175	0.04086
0.40	$2.97478889 \times 10^{-8}$	0.07936	0.37	0.07936
0.60	$1.49615371 \times 10^{-8}$	0.22176	0.52	0.22176
0.80	$9.28288357 \times 10^{-9}$	0.50176	0.73	0.50176
0.90	7.6237997×10^{-9}	0.71766	0.8575	0.71766
0.95	$6.96000757 \times 10^{-9}$	0.84970375	0.926875	0.84970375
1	$6.38052022 \times 10^{-9}$	1	1	1

Table 7. In the **Saturn-Sun interaction system**, in which the values of m , r_p and v_p are given in above Table 1, the numerical results of $RE(v; p)$, $K^*(v; p)/K_o(p)$, $U^*(v; p)/U_o(p)$ and $E^*(v; p)/E_o(p)$, are obtained by using Equations (7, 4, 5, 6), respectively, noting that $v_p \leq v \leq c$.

$X(v)=v/c$	$RE(v; p)$	$K^*(v; p)/K_o(p)$	$U^*(v; p)/U_o(p)$	$E^*(v; p)/E_o(p)$
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Here, for $p=1$ and at $v=c$, $K_o(p) = \left(\frac{3}{4}\right) \times mc^2 = 3.83173493 \times 10^{43}$ J, $U_o(p) = -1.11689739 \times 10^{35}$ J and $E_o(p) = 3.83173492 \times 10^{43}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of 2.9148608×10^{-9} .

3.2156×10^{-5}	2.1142644	$6.89332134 \times 10^{-10}$	0.50	$-7.68098259 \times 10^{-10}$
0.09	2.7098318×10^{-7}	0.00542187	0.50405	0.00542187
0.30	$2.53365091 \times 10^{-8}$	0.0627	0.545	0.0627
0.40	$1.46755144 \times 10^{-8}$	0.1152	0.58	0.1152
0.60	$6.99895952 \times 10^{-9}$	0.2832	0.68	0.2832
0.80	$4.24393787 \times 10^{-9}$	0.5632	0.82	0.5632
0.90	$3.47693296 \times 10^{-9}$	0.7587	0.905	0.7587
0.95	$3.17551596 \times 10^{-9}$	0.87316875	0.95125	0.87316875
1	2.9148608×10^{-9}	1	1	1

Here, for $p=2$ and at $v=c$, $K_o(p) = mc^2 = 5.10897991 \times 10^{43}$ J, in good agreement with that, proposed by Einstein in 1905, $U_o(p) = -1.67534608 \times 10^{35}$ J and $E_o(p) = 5.10897989 \times 10^{43}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $3.27921834 \times 10^{-9}$.

3.2156×10^{-5}	2.1142644	5.16999101	$\times 10^{-10}$	0.33333333	-5.76073695	$\times 10^{-10}$
0.09	$2.72063096 \times 10^{-7}$	0.00408281		0.33873333	0.0040828	
0.30	$2.62961447 \times 10^{-8}$	0.04905		0.39333333	0.04905	
0.40	$1.55480181 \times 10^{-8}$	0.0928		0.44	0.0928	
0.60	$7.68008668 \times 10^{-8}$	0.2448		0.57333333	0.2448	
0.80	$4.74886808 \times 10^{-9}$	0.5248		0.76	0.5248	
0.90	$3.90676047 \times 10^{-9}$	0.73305		0.87333333	0.73305	
0.95	$3.57141294 \times 10^{-9}$	0.85850312		0.935	0.85850312	
1	$3.27921834 \times 10^{-9}$	1		1	1	

Here, for $p=3$ and further at $v=c$, $K_o(p) = \frac{5}{4} \times mc^2 = 6.38622489 \times 10^{43}$ J, $U_o(p) = -2.23379477 \times 10^{35}$ J and $E_o(p) = 6.38622487 \times 10^{43}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $3.49783291 \times 10^{-9}$.

3.2156×10^{-5}	2.1142644	4.13599281	$\times 10^{-10}$	0.25	-4.60858957	$\times 10^{-10}$
0.09	$2.73134371 \times 10^{-7}$	0.00327937		0.256075	0.00327937	
0.30	$2.71796856 \times 10^{-8}$	0.04086		0.3175	0.04086	
0.40	$1.63079409 \times 10^{-8}$	0.07936		0.37	0.07936	
0.60	8.2019892×10^{-9}	0.22176		0.52	0.22176	
0.80	$5.08892306 \times 10^{-9}$	0.50176		0.73	0.50176	
0.90	$4.17940482 \times 10^{-9}$	0.71766		0.8575	0.71766	
0.95	$3.81551091 \times 10^{-9}$	0.84970375		0.926875	0.84970375	
1	$3.49783291 \times 10^{-9}$	1		1	1	

Table 8. In the Uranus-Sun interaction system, in which the values of m , r_p and v_p are given in above Table 1, the numerical results of $RE(v; p)$, $K^*(v; p)/K_o(p)$, $U^*(v; p)/U_o(p)$ and $E^*(v; p)/E_o(p)$, are obtained by using Equations (7, 4, 5, 6), respectively, noting that $v_p \leq v \leq c$.

$X(v)=v/c$	$RE(v; p)$	$K^*(v; p)/K_o(p)$	$U^*(v; p)/U_o(p)$	$E^*(v; p)/E_o(p)$
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Here, for $p=1$ and at $v=c$, $K_o(p) = (\frac{3}{4}) \times mc^2 = 5.85209446 \times 10^{42}$ J, $U_o(p) = -8.41496949 \times 10^{33}$ J and $E_o(p) = 5.85209445 \times 10^{42}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $1.43794143 \times 10^{-9}$.

2.2649×10^{-5}	2.10231223	3.41990472	$\times 10^{-10}$	0.50	-3.76980279	$\times 10^{-10}$
0.09	$1.33679785 \times 10^{-7}$	0.00542187		0.50405	0.00542187	
0.30	$1.24988536 \times 10^{-8}$	0.0627		0.545	0.0627	
0.40	$7.23963600 \times 10^{-9}$	0.1152		0.58	0.1152	
0.60	$3.45268436 \times 10^{-9}$	0.2832		0.68	0.2832	

0.80	$2.09359374 \times 10^{-9}$	0.5632	0.82	0.5632
0.90	$1.71521952 \times 10^{-9}$	0.7587	0.905	0.7587
0.95	$1.56652635 \times 10^{-9}$	0.87316875	0.95125	0.87316875
1	$1.43794143 \times 10^{-9}$	1	1	

Here, for $p=2$ and at $v=c$, $K_o(p) = mc^2 = 7.80279261 \times 10^{42}$ J, in good agreement with that, proposed by Einstein in 1905, $U_o(p) = -1.26224542 \times 10^{34}$ J and $E_o(p) = 7.80279260 \times 10^{42}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $1.61768410 \times 10^{-9}$.

2.2649	$\times 10^{-5}$	2.10231223	2.56492854	$\times 10^{-10}$	0.33333333	-2.8273521	$\times 10^{-10}$
0.09	$1.34212522 \times 10^{-7}$	0.00408281	0.33873333	0.0040828			
0.30	$1.29722553 \times 10^{-8}$	0.04905	0.39333333	0.04905			
0.40	$7.67005426 \times 10^{-9}$	0.0928	0.44	0.0928			
0.60	$3.78869391 \times 10^{-9}$	0.2448	0.57333333	0.2448			
0.80	$2.34268294 \times 10^{-9}$	0.5248	0.76	0.5248			
0.90	$1.92725935 \times 10^{-9}$	0.73305	0.87333333	0.73305			
0.95	$1.76182779 \times 10^{-9}$	0.85850312	0.935	0.85850312			
1	$1.61768410 \times 10^{-9}$	1	1	1			

Here, for $p=3$ and further at $v=c$, $K_o(p) = \frac{5}{4} \times mc^2 = 9.75349076 \times 10^{42}$ J, $U_o(p) = -1.6829939 \times 10^{34}$ J and $E_o(p) = 9.75349075 \times 10^{42}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $1.72552972 \times 10^{-9}$.

2.2649	$\times 10^{-5}$	2.10231223	2.05194283	$\times 10^{-10}$	0.25	-2.26188168	$\times 10^{-10}$
0.09	$1.34740997 \times 10^{-7}$	0.00327937	0.256075	0.00327937			
0.30	$1.34081182 \times 10^{-8}$	0.04086	0.3175	0.04086			
0.40	$8.04493483 \times 10^{-8}$	0.07936	0.37	0.07936			
0.60	$4.04615574 \times 10^{-9}$	0.22176	0.52	0.22176			
0.80	$2.51043675 \times 10^{-9}$	0.50176	0.73	0.50176			
0.90	$2.06175876 \times 10^{-9}$	0.71766	0.8575	0.71766			
0.95	$1.88224480 \times 10^{-9}$	0.84970375	0.926875	0.84970375			
1	$1.72552972 \times 10^{-9}$	1	1	1			

Table 9. In the Neptune-Sun interaction system, in which the values of m , r_p and v_p are given in above Table 1, the numerical results of $RE(v; p)$, $K^*(v; p)/K_o(p)$, $U^*(v; p)/U_o(p)$ and $E^*(v; p)/E_o(p)$, are obtained by using Equations (7, 4, 5, 6), respectively, noting that $v_p \leq v \leq c$.

$X(v)=v/c$	$RE(v; p)$	$K^*(v; p)/K_o(p)$	$U^*(v; p)/U_o(p)$	$E^*(v; p)/E_o(p)$
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Here, for $p=1$ and at $v=c$, $K_o(p) = \left(\frac{3}{4}\right) \times mc^2 = 6.90441616 \times 10^{42}$ J, $U_o(p) = -6.09086043 \times 10^{33}$ J and $E_o(p) = 6.90441615 \times 10^{42}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $8.82168782 \times 10^{-10}$.

1.8113×10^{-5}	2.01672915	$2.18712758 \times 10^{-10}$	0.50	$-2.22371636 \times 10^{-10}$
0.09	8.2011774×10^{-8}	0.00542187	0.50405	0.00542187
0.30	$7.66797437 \times 10^{-9}$	0.0627	0.545	0.0627
0.40	$4.44147485 \times 10^{-9}$	0.1152	0.58	0.1152
0.60	$2.11820184 \times 10^{-9}$	0.2832	0.68	0.2832
0.80	$1.28440769 \times 10^{-9}$	0.5632	0.82	0.5632
0.90	$1.05227727 \times 10^{-9}$	0.7587	0.905	0.7587
0.95	$9.61054791 \times 10^{-10}$	0.87316875	0.95125	0.87316875
1	$8.82168782 \times 10^{-10}$	1	1	1

Here, for $p=2$ and at $v=c$, $K_o(p) = mc^2 = 9.20588821 \times 10^{42}$ J, in good agreement with that, proposed by Einstein in 1905, $U_o(p) = -9.13629064 \times 10^{33}$ J and $E_o(p) = 9.20588820 \times 10^{42}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $9.92439908 \times 10^{-10}$.

1.8113×10^{-5}	2.01672915	$1.64034569 \times 10^{-10}$	0.33333333	$-1.66778727 \times 10^{-10}$
0.09	$8.23386056 \times 10^{-8}$	0.00408281	0.33873333	0.0040828
0.30	$7.95840338 \times 10^{-9}$	0.04905	0.39333333	0.04905
0.40	$4.70553407 \times 10^{-9}$	0.0928	0.44	0.0928
0.60	$2.32434172 \times 10^{-9}$	0.2448	0.57333333	0.2448
0.80	$1.43722245 \times 10^{-9}$	0.5248	0.76	0.5248
0.90	$1.18236254 \times 10^{-9}$	0.73305	0.87333333	0.73305
0.95	$1.08087117 \times 10^{-9}$	0.85850312	0.935	0.85850312
1	$9.92439908 \times 10^{-10}$	1	1	1

Here, for $p=3$ and further at $v=c$, $K_o(p) = \frac{5}{4} \times mc^2 = 1.15073603 \times 10^{43}$ J, $U_o(p) = -1.21817209 \times 10^{34}$ J and $E_o(p) = 1.150736025 \times 10^{43}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $1.05860254 \times 10^{-9}$.

1.8113×10^{-5}	2.01672915	$1.31227655 \times 10^{-10}$	0.25	$-1.33422982 \times 10^{-10}$
0.09	$8.26628215 \times 10^{-8}$	0.00327937	0.256075	0.00327937
0.30	$8.22580293 \times 10^{-9}$	0.04086	0.3175	0.04086
0.40	$4.93552099 \times 10^{-9}$	0.07936	0.37	0.07936
0.60	$2.48229315 \times 10^{-9}$	0.22176	0.52	0.22176
0.80	$1.54013835 \times 10^{-9}$	0.50176	0.73	0.50176
0.90	$1.26487709 \times 10^{-9}$	0.71766	0.8575	0.71766
0.95	$1.15474630 \times 10^{-9}$	0.84970375	0.926875	0.84970375
1	$1.05860254 \times 10^{-9}$	1	1	1

Table 10. In the **Moon-Sun interaction system**, in which the values of m , r_p and v_p are given in above Table 1, the numerical results of $RE(v; p)$, $K^*(v; p)/K_o(p)$, $U^*(v; p)/U_o(p)$ and $E^*(v; p)/E_o(p)$, are obtained by using Equations (7, 4, 5, 6), respectively, noting that $v_p \leq v \leq c$.

$X(v)=v/c$	$RE(v; p)$	$K^*(v; p)/K_o(p)$	$U^*(v; p)/U_o(p)$	$E^*(v; p)/E_o(p)$
Here, for $p=1$ and at $v=c$, $K_o(p) = \left(\frac{3}{4}\right) \times mc^2 = 4.95148239 \times 10^{39}$ J, $U_o(p) = -5.38467907 \times 10^{34}$ J and $E_o(p) = 4.95142854 \times 10^{39}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $1.08748828 \times 10^{-5}$.				
3.4357×10^{-6}	6.90948509×10^5	$7.86953201 \times 10^{-12}$	0.50	$-5.43749267 \times 10^{-6}$
0.09	0.001011	0.00542187	0.50405	0.00541645
0.30	$9.45264934 \times 10^{-5}$	0.0627	0.545	0.06269475
0.40	$5.47520142 \times 10^{-5}$	0.1152	0.58	0.11519495
0.60	$2.61120068 \times 10^{-5}$	0.2832	0.68	0.28319568
0.80	$1.58334586 \times 10^{-5}$	0.5632	0.82	0.56319721
0.90	$1.29718847 \times 10^{-5}$	0.7587	0.905	0.75869841
0.95	$1.18473460 \times 10^{-5}$	0.87316875	0.95125	0.87316790
1	$1.08748828 \times 10^{-5}$	1	1	1
Here, for $p=2$ and at $v=c$, $K_o(p) = mc^2 = 6.60197652 \times 10^{39}$ J, in good agreement with that, proposed by Einstein in 1905 , $U_o(p) = -8.07701861 \times 10^{34}$ J and $E_o(p) = 6.60189575 \times 10^{39}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $1.22342432 \times 10^{-5}$.				
3.4357×10^{-6}	6.90948509×10^5	$5.90214900 \times 10^{-12}$	0.33333333	$-4.07812505 \times 10^{-6}$
0.09	0.00101502	0.00408281	0.33873333	0.00407871
0.30	9.8106741×10^{-5}	0.04905	0.39333333	0.04904579
0.40	$5.80071874 \times 10^{-5}$	0.0928	0.44	0.09279575
0.60	$2.86531839 \times 10^{-5}$	0.2448	0.57333333	0.24479598
0.80	$1.77172729 \times 10^{-5}$	0.5248	0.76	0.52479712
0.90	$1.45755029 \times 10^{-5}$	0.73305	0.87333333	0.73304828
0.95	$1.33243748 \times 10^{-5}$	0.85850312	0.935	0.85850219
1	$1.22342432 \times 10^{-5}$	1	1	1
Here, for $p=3$ and further at $v=c$, $K_o(p) = \frac{5}{4} \times mc^2 = 8.25247065 \times 10^{39}$ J, $U_o(p) = -1.07693581 \times 10^{35}$ J and $E_o(p) = 8.25236296 \times 10^{39}$ J, suggesting that $E_o(p) \cong K_o(p)$, with a precision of the order of $1.30498594 \times 10^{-5}$.				
3.4357×10^{-6}	6.90948509×10^5	$4.72171920 \times 10^{-12}$	0.25	$-3.2625027 \times 10^{-6}$
0.09	0.00101902	0.00327937	0.256075	0.00327607
0.30	0.0001014	0.04086	0.3175	0.04085639
0.40	$6.08423383 \times 10^{-5}$	0.07936	0.37	0.07935621
0.60	$3.06003196 \times 10^{-5}$	0.22176	0.52	0.22175611

0.80	$1.89859641 \times 10^{-5}$	0.50176	0.73	0.50175702
0.90	$1.55926963 \times 10^{-5}$	0.71766	0.8575	0.71765818
0.95	$1.42350654 \times 10^{-5}$	0.84970375	0.926875	0.84970274
1	$1.30498594 \times 10^{-5}$	1	1	1
