Oríginal Article

World Journal of Engineering Research and Technology



www.wjert.org

SJIF Impact Factor: 7.029



# OPTICAL COEFFICIENTS IN THE N(P)-TYPE DEGENERATE GaTe(1-x) Sb(x)-CRYSTALLINE ALLOY, DUE TO THE NEW STATIC DIELECTRIC CONSTANT-LAW AND THE GENERALIZED MOTT CRITERIUM IN THE METAL-INSULATOR TRANSITION. (7)

# Prof. Dr. Huynh Van Cong\*

Université de Perpignan Via Domitia, Laboratoire de Mathématiques et Physique (LAMPS), EA 4217, Département de Physique, 52, Avenue Paul Alduy, F-66 860 Perpignan, France.

Article Received on 21/08/2024

Article Revised on 11/09/2024

Article Accepted on 01/10/2024



\*Corresponding Author Prof. Dr. Huynh Van Cong Université de Perpignan Via Domitia, Laboratoire de Mathématiques et Physique (LAMPS), EA 4217, Département de Physique, 52, Avenue Paul Alduy, F-66 860 Perpignan, France.

# ABTRACT

In the n(p)-type GaTe<sub>1-x</sub>Sb<sub>x</sub>- crystalline alloy, with  $0 \le x \le 1$ , basing on our two recent works<sup>[1,2]</sup>, for a given x, and with an increasing  $r_{d(a)}$ , the optical coefficients have been determined, as functions of the photon energy E, total impurity density N, the donor (acceptor) radius  $r_{d(a)}$ , concentration x, and temperature T. Those results have been affected by (i) the important new  $\varepsilon(r_{d(a)}, x)$ -law, developed in Equations (8a, 8b), stating that, for a given x, due to the impurity-size effect,  $\varepsilon$  decreases ( $\Sigma$ ) with an increasing ( $\nearrow$ )  $r_{d(a)}$ , and then by (ii) the generalized Mott critical d(a)-density defined in the metal-insulator transition (MIT),  $N_{CDn(NDp)}(r_{d(a)}, x)$ , as observed in Equations (8c, 9a). Furthermore, we also showed that  $N_{CDn(NDp)}$  is just the density of

carriers localized in exponential band tails, with a precision of the order of  $2.87 \times 10^{-7}$ , as that given in Table 4 of Ref.<sup>[1]</sup>, according to a definition of the effective density of electrons (holes) given in parabolic conduction (valence) bands by:  $N^*(N, r_{d(a)}, x) \equiv N - N_{CDn(NDp)}(r_{d(a)}, x)$ , as defined in Eq. (9d). In summary, due to the new  $\epsilon(r_{d(a)}, x)$ -law and to the effective density of electrons (holes) given in parabolic conduction (valence) bands  $N^*(N, r_{d(a)}, x)$ , for a given x, and with an increasing  $r_{d(a)}$ , the numerical results of all the optical coefficients, obtained in appropriated physical conditions (E, N, T),

and calculated by using Equations (15, 16, 20, 21), are reported in Tables 1, 2, 3n, 3p, 4n, 4p, 5n, and 5p in Appendix 1.

**KEYWORS:**  $GaTe_{1-x}Sb_x$ - crystalline alloy; impurity-size effect; Mott critical impurity density in the MIT, optical coefficients.

#### INTRODUCTION

Here, basing on our two recent works<sup>[1, 2]</sup> and also other ones<sup>[3-8]</sup>, all the optical coefficients given in the n(p)-type  $\mathbf{X}(\mathbf{x}) \equiv \mathbf{GaTe_{1-x}Sb_x}$  - crystalline alloy, with  $0 \le x \le 1$ , are investigated, as functions of the photon energy E, total impurity density N, the donor (acceptor) radius  $\mathbf{r_{d(a)}}$ , concentration x, and temperature T.

Then, for a given x, and with an increasing  $r_{d(a)}$ , the numerical results of all the optical coefficients, obtained in appropriated physical conditions (E, N, T), and calculated by using Equations (15, 16, 20, 21), are reported in Tables 1, 2, 3n, 3p, 4n, 4p, 5n, and 5p in Appendix 1.

#### **ENERGY BAND STUCTURE PARAMETERS**

First of all, in the  $n^+(p^+) - p(n) X(x)$ - crystalline alloy at T=0 K, we denote the donor (acceptor) d(a)-radius by  $r_{d(a)}$ , and also the intrinsic one by:  $r_{do(ao)} = r_{Te(Ga)} = 0.132$  nm (0.126 nm).

**A. Effect of x- concentration**Here, the intrinsic energy-band-structure parameters<sup>[1]</sup>, are expressed as functions of x, are given in the following.

(i)-The unperturbed relative effective electron (hole) mass in conduction (valence) bands are given by:

$$m_{c(v)}(x)/m_{o} = 0.047(0.3) \times x + 0.209(0.4) \times (1 - x)$$
 (1)

(ii)-The unperturbed relative static dielectric constant of the intrinsic of the single crystalline X- alloy is found to be defined by:

$$\varepsilon_0(\mathbf{x}) = 15.69 \times \mathbf{x} + 12.3 \times (1 - \mathbf{x}). \tag{2}$$

(iii)-Finally, the unperturbed band gap at 0 K is found to be given by:

$$E_{ao}(x) = 0.81 \times x + 1.796 \times (1 - x). \tag{3}$$

Therefore, we can define the effective donor (acceptor)-ionization energy in absolute values as:

$$E_{do(ao)}(x) = \frac{13600 \times [m_{c(v)}(x)/m_0]}{[\varepsilon_0(x)]^2} \text{ meV},$$
(4)

and then, the isothermal bulk modulus, by:

$$B_{do(ao)}(x) \equiv \frac{E_{do(ao)}(x)}{\left(\frac{4\pi}{3}\right) \times \left(r_{do(ao)}\right)^3}.$$
(5)

### B. Effect of Impurity $r_{d(a)}$ -size, with a given x

Here, the changes in all the energy-band-structure parameters, expressed in terms of the effective relative dielectric constant  $\epsilon(r_{d(a)}, x)$ , developed as follows.

At  $r_{d(a)} = r_{do(ao)}$ , the needed boundary conditions are found to be, for the impurity-atom volume  $V = (4\pi/3) \times (r_{d(a)})^3$ ,  $V_{do(ao)} = (4\pi/3) \times (r_{do(ao)})^3$ , for the pressure p,  $p_o = 0$ , and for the deformation potential energy (or the strain energy)  $\sigma$ ,  $\sigma_o = 0$ . Further, the two important equations [1, 7], used to determine the  $\sigma$ -variation,  $\Delta\sigma \equiv \sigma - \sigma_o = \sigma$ , are defined by:  $\frac{dp}{dv} = -\frac{B}{v}$  and  $p = -\frac{d\sigma}{dv}$ . giving:  $\frac{d}{dv} (\frac{d\sigma}{dv}) = \frac{B}{v}$ . Then, by an integration, one gets:  $[\Delta\sigma(r_{d(a)}, x)]_{n(p)} = B_{do(ao)}(x) \times (V - V_{do(ao)}) \times \ln$  $(\frac{V}{V_{do(ao)}}) = E_{do(ao)}(x) \times \left[ \left( \frac{r_{d(a)}}{r_{do(ao)}} \right)^3 - 1 \right] \times \ln \left( \frac{r_{d(a)}}{r_{do(ao)}} \right)^3 \ge 0.$  (6)

Furthermore, we also shown that, as  $r_{d(a)} > r_{do(ao)} (r_{d(a)} < r_{do(ao)})$ , the compression (dilatation) gives rise to the increase (the decrease) in the energy gap  $E_{gn(gp)}(r_{d(a)}, x)$ , and the effective donor (acceptor)-ionization energy  $E_{d(a)}(r_{d(a)}, x)$  in absolute values, obtained in the effective Bohr model, which is represented respectively by:  $\pm [\Delta\sigma(r_{d(a)}, x)]_{n(p)}$ ,

$$\begin{split} E_{\text{gno}(\text{gpo})}(\mathbf{r}_{d(a)}, \mathbf{x}) - E_{\text{go}}(\mathbf{x}) &= E_{d(a)}(\mathbf{r}_{d(a)}, \mathbf{x}) - E_{do(ao)}(\mathbf{x}) = E_{do(ao)}(\mathbf{x}) \times \left[ \left( \frac{\varepsilon_0(\mathbf{x})}{\varepsilon(\mathbf{r}_{d(a)})} \right)^2 - 1 \right] \\ &= + \left[ \Delta \sigma(\mathbf{r}_{d(a)}, \mathbf{x}) \right]_{n(p)} \end{split}$$

 $\text{for } r_{d(a)} \geq r_{do(ao)} \text{, and for } r_{d(a)} \leq r_{do(ao)} \text{,}$ 

$$\begin{split} E_{gno(gpo)}(r_{d(a)}, x) - E_{go}(x) &= E_{d(a)}(r_{d(a)}, x) - E_{do(ao)}(x) = E_{do(ao)}(x) \times \left[ \left( \frac{\varepsilon_0(x)}{\varepsilon(r_{d(a)})} \right)^2 - 1 \right] \\ &= - \left[ \Delta \sigma(r_{d(a)}, x) \right]_{n(p)} \end{split}$$
(7)

Therefore, from Equations (6) and (7), one obtains the expressions for relative dielectric constant  $\varepsilon(r_{d(a)}, x)$  and energy band gap  $E_{gn(gp)}(r_{d(a)}, x)$ , as:

(i)-for 
$$r_{d(a)} \ge r_{do(ao)}$$
, since  $\epsilon(r_{d(a)}, x) = \frac{\epsilon_0(x)}{\sqrt{1 + \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3}} \le \epsilon_0(x)$ , being a new

 $\epsilon(\mathbf{r}_{\mathbf{d}(\mathbf{a})}, \mathbf{x})$ -law,

$$\begin{split} E_{gno(gpo)}\big(r_{d(a)}, x\big) - E_{go}(x) &= E_{d(a)}\big(r_{d(a)}, x\big) - E_{do(ao)}(x) = E_{do(ao)}(x) \times \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \\ &\ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 \ge 0, \end{split}$$
(8a)

according to the increase in both  $E_{gn(gp)}(r_{d(a)}, x)$  and  $E_{d(a)}(r_{d(a)}, x)$ , with increasing  $r_{d(a)}$  and for a given x, and

(ii)-for 
$$r_{d(a)} \leq r_{do(ao)}$$
, since  $\epsilon(r_{d(a)}, x) = \frac{\epsilon_0(x)}{\sqrt{1 - \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3}} \geq \epsilon_0(x)$ , with a condition, given by:  $\left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 < 1$ , being a **new**  $\epsilon(r_{d(a)}, x)$ -law,  
 $E_{gno(gpo)}(r_{d(a)}, x) - E_{go}(x) = E_{d(a)}(r_{d(a)}, x) - E_{do(ao)}(x) = -E_{do(ao)}(x) \times \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3$ 

$$\leq 0,$$
(8b)

corresponding to the decrease in both  $E_{gn(gp)}(r_{d(a)}, x)$  and  $E_{d(a)}(r_{d(a)}, x)$ , with decreasing  $r_{d(a)}$  and for a given x; therefore, the effective Bohr radius  $a_{Bn(Bp)}(r_{d(a)}, x)$  is defined by:

$$a_{Bn(Bp)}(r_{d(a)},x) \equiv \frac{\epsilon(r_{d(a)},x) \times \hbar^2}{m_{c(v)}(x) \times q^2} = 0.53 \times 10^{-8} \text{ cm} \times \frac{\epsilon(r_{d(a)},x)}{m_{c(v)}(x)/m_0}.$$
(8c)

Furthermore, it is interesting to remark that the critical total donor (acceptor)-density in the metal-insulator transition (**MIT**) at T=0 K,  $N_{CDn(NDp)}(r_{d(a)}, x)$ , was given by the Mott's criterium, with an empirical parameter,  $M_{n(p)}$ , as:

$$N_{CDn(CDp)}(r_{d(a)}, x)^{1/3} \times a_{Bn(Bp)}(r_{d(a)}, x) = M_{n(p)}, M_{n(p)} = 0.25,$$
(9a)

depending thus on our new  $\epsilon(\mathbf{r}_{d(a)}, \mathbf{x})$ -law.

This excellent one can be explained from the definition of the reduced effective Wigner-Seitz (**WS**) radius  $r_{sn(sp)}$ , characteristic of interactions, by:

$$r_{sn(sp)}(N, r_{d(a)}, x) \equiv \left(\frac{3}{4\pi N}\right)^{1/3} \times \frac{1}{a_{Bn(Bp)}(r_{d(a)}, x)} = 1.1723 \times 10^8 \times \left(\frac{1}{N}\right)^{1/3} \times \frac{m_{C(V)}(x)/m_0}{\epsilon(r_{d(a)}, x)},$$
(9b)

being equal to, in particular, at N=N<sub>CDn(CDp)</sub>( $r_{d(a)}, x$ ):  $r_{sn(sp)}(N_{CDn(CDp)}(r_{d(a)}, x), r_{d(a)}, x) =$ 2.4814, for any ( $r_{d(a)}, x$ )-values. So, from Eq. (9b), one also has:  $N_{CDn(CDp)}(r_{d(a)}, x)^{1/3} \times a_{Bn(Bp)}(r_{d(a)}, x) = \left(\frac{3}{4\pi}\right)^{\frac{1}{3}} \times \frac{1}{2.4814} = 0.25 = (WS)_{n(p)} = M_{n(p)}.$  (9c)

Thus, the above Equations (9a, 9b, 9c) confirm our new  $\epsilon(r_{d(a)}, x)$ -law, given in Equations (8a, 8b).

Furthermore, by using  $\mathbf{M}_{\mathbf{n}(\mathbf{p})} = \mathbf{0}.\mathbf{25}$ , according to the empirical Heisenberg parameter  $\mathcal{H}_{\mathbf{n}(\mathbf{p})} = \mathbf{0}.\mathbf{47137}$ , as those given in Equations (8, 15) of the Ref.<sup>[1]</sup>, we have also showed that  $N_{\text{CDn}(\text{CDp})}$  is just the density of electrons (holes) localized in the exponential conduction (valence)-band tail, with a precision of the order of  $\mathbf{2}.\mathbf{87} \times \mathbf{10^{-7}}$ . Therefore, the density of electrons (holes) given in parabolic conduction (valence) bands can be defined, as that given in compensated materials, by:

$$N^*(N, r_{d(a)}, x) \equiv N - N_{CDn(NDp)}(r_{d(a)}, x).$$
(9d)

#### C. Effect of temperature T, with given x and $r_{d(a)}$

Here, the intrinsic band gap  $E_{gni(gpi)}(r_{d(a)}, x, T)$  at any T is given by:

$$E_{gni(gpi)}(r_{d(a)}, x, T) \text{ in } eV = E_{gno(gpo)}(r_{d(a)}, x) - 10^{-4} \times T^2 \times \left\{ \frac{5.405 \times x}{T + 204 \text{ K}} + \frac{3.065 \times (1-x)}{T + 94 \text{ K}} \right\},$$
(10)

suggesting that, for given x and  $r_{d(a)}$ ,  $E_{gni(gpi)}$  decreases with an increasing T.

Then, in the following, for the study of optical phenomena, one denote the conduction (valence)-band density of states by  $N_{c(v)}(T, x)$  as:

$$N_{c(v)}(T,x) = 2 \times g_{c(v)}(x) \times \left(\frac{m_{\Gamma(x) \times k_{B}T}}{2\pi\hbar^{2}}\right)^{\frac{3}{2}} (cm^{-3}), \ g_{v}(x) \equiv 1 \times x + 1 \times (1-x) = 1,$$
(11)

where  $m_r(x)/m_o$  is the reduced effective mass  $m_r(x)/m_o$ , defined by :  $m_r(x) \equiv [m_c(x) \times m_v(x)]/[m_c(x) + m_v(x)].$ 

# D. Heavy Doping Effect, with given T, x and $r_{d(a)}$

Here, as given in our previous works<sup>[1,2]</sup>, the Fermi energy  $E_{Fn}(-E_{Fp})$ , and the band gap narrowing are reported in the following.

First, the reduced Fermi energy  $\eta_{n(p)}$  or the Fermi energy  $E_{Fn}(-E_{Fp})$ , obtained for any T and any effective d(a)-density,  $N^*(N, r_{d(a)}, x) = N^*$ , defined in Eq. (9d), for a simplicity of presentation, being investigated in our previous paper<sup>[8]</sup>, with a precision of the order of  $2.11 \times 10^{-4}$ , is found to be given by:

$$\eta_{n(p)}(u) \equiv \frac{E_{Fn}(u)}{k_B T} \left( \frac{-E_{Fp}(u)}{k_B T} \right) = \frac{G(u) + A u^B F(u)}{1 + A u^B}, A = 0.0005372 \text{ and } B = 4.82842262,$$
(12)

where u is the reduced electron density,  $u(N, r_{d(a)}, x, T) \equiv \frac{N^*}{N_{C(v)}(T, x)}$ ,  $F(u) = au^{\frac{2}{3}} \left(1 + bu^{-\frac{4}{3}} + cu^{-\frac{8}{3}}\right)^{-\frac{2}{3}}$ ,  $a = \left[(3\sqrt{\pi}/4) \times u\right]^{2/3}$ ,  $b = \frac{1}{8} \left(\frac{\pi}{a}\right)^2$ ,  $c = \frac{62.3739855}{1920} \left(\frac{\pi}{a}\right)^4$ , and  $G(u) \simeq Ln(u) + 2^{-\frac{3}{2}} \times u \times e^{-du}$ ;  $d = 2^{3/2} \left[\frac{1}{\sqrt{27}} - \frac{3}{16}\right] > 0$ . Therefore, from Eq. (12), the Fermi energies are expressed as functions of variables : N,  $r_{d(a)}$ , x, and T.

Here, one notes that: (i) as  $u \gg 1$ , according to the HD [d(a)-X(x)- alloy] ER-case, or to the degenerate case, Eq. (12) is reduced to the function F(u), and in particular at T=0 and as  $N^* = 0$ , according to the metal-insulator transition (**MIT**), one has: + $E_{Fn}(-E_{Fp}) = \frac{\hbar^2}{2 \times m_r(x)} \times (3\pi^2 N^*)^{2/3} = 0$ , and (ii)  $\frac{E_{Fn}(u\ll 1)}{k_BT} (\frac{-E_{Fp}(u\ll 1)}{k_BT}) \ll -1$ , to the LD [a(d)-X(x)- alloy] BR-case, or to the non-degenerate case, Eq. (12) is reduced to the function G(u), noting that the notations: **HD**(**LD**) and **ER**(**BR**) denote the heavily doped (lightly doped)-cases and emitter (base)-regions, respectively.

Now, in Eq. (9b), in which one replaces  $m_{c(v)}(x)$  by  $m_r(x)$ , the effective Wigner-Seitz radius becomes as:

$$r_{sn(sp)}(N, r_{d(a)}, x) = 1.1723 \times 10^8 \times \left(\frac{g_{c(v)}(x)}{N^*}\right)^{1/3} \times \frac{m_r(x)}{\varepsilon(r_{d(a)}, x)},$$
(13a)

the correlation energy of an effective electron gas,  $E_{cn(cp)}(N, r_{d(a)}, x)$ , is given as:

$$E_{cn(cp)}(N, r_{d(a)}, x) = \frac{-0.87553}{0.0908 + r_{sn(sp)}} + \frac{\frac{0.87553}{0.0908 + r_{sn(sp)}} + \left(\frac{2[1 - \ln(2)]}{\pi^2}\right) \times \ln(r_{sn(sp)}) - 0.093288}{1 + 0.03847728 \times r_{sn(sp)}^{1.67378876}}.$$
 (13b)

Then, taking into account various spin-polarized chemical potential-energy contributions such as: exchange energy of an effective electron (hole) gas, majority-carrier correlation energy of an effective electron (hole) gas, minority hole (electron) correlation energy, majority electron (hole)-ionized d(a) interaction screened Coulomb potential energy, and

Cong.

finally minority hole (electron)-ionized d(a) interaction screened Coulomb potential energy, the band gap narrowings are given in the following.

In the n-type HD X(x)- alloy, the BGN is found to be given by:

$$\begin{split} \Delta E_{\rm gno}(N, r_{\rm d}, x) &= a_1 \times \frac{\varepsilon_0(x)}{\varepsilon(r_{\rm d}, x)} \times N_r^{1/3} + a_2 \times \frac{\varepsilon_0(x)}{\varepsilon(r_{\rm d}, x)} \times N_r^{\frac{1}{3}} \times (2.503 \times [-E_{\rm cn}(r_{\rm sn}) \times r_{\rm sn}]) + \\ a_3 \times \left[\frac{\varepsilon_0(x)}{\varepsilon(r_{\rm d}, x)}\right]^{5/4} \times \sqrt{\frac{m_v}{m_r}} \times N_r^{1/4} + a_4 \times \sqrt{\frac{\varepsilon_0(x)}{\varepsilon(r_{\rm d}, x)}} \times N_r^{1/2} \times 2 + a_5 \times \left[\frac{\varepsilon_0(x)}{\varepsilon(r_{\rm d}, x)}\right]^{\frac{3}{2}} \times N_r^{\frac{1}{6}} \\ , N_r \equiv \left(\frac{N^*}{N_{\rm CDn}(r_{\rm d}, x)}\right), \\ \Delta E_{\rm gn}(N, r_{\rm d}, x) = \Delta E_{\rm gno}(N, r_{\rm d}, x) \times \{0.2 \times x + 6 \times (1 - x)\}, \end{split}$$
(14n)

where  $a_1 = 3.8 \times 10^{-3} (eV)$ ,  $a_2 = 6.5 \times 10^{-4} (eV)$ ,  $a_3 = 2.8 \times 10^{-3} (eV)$  $a_4 = 5.597 \times 10^{-3} (eV)$  and  $a_5 = 8.1 \times 10^{-4} (eV)$ , and in the p-type HD X(x)- alloy, as:

$$\begin{split} \Delta E_{gpo}(N, r_{a}, x) &= a_{1} \times \frac{\varepsilon_{0}(x)}{\varepsilon(r_{a}, x)} \times N_{r}^{1/3} + a_{2} \times \frac{\varepsilon_{0}(x)}{\varepsilon(r_{a}, x)} \times N_{r}^{\frac{1}{3}} \times \left(2.503 \times \left[-E_{cp}(r_{sp}) \times r_{sp}\right]\right) + \\ a_{3} \times \left[\frac{\varepsilon_{0}(x)}{\varepsilon(r_{a}, x)}\right]^{5/4} \times \sqrt{\frac{m_{c}}{m_{r}}} \times N_{r}^{1/4} + 2a_{4} \times \sqrt{\frac{\varepsilon_{0}(x)}{\varepsilon(r_{a}, x)}} \times N_{r}^{1/2} + a_{5} \times \left[\frac{\varepsilon_{0}(x)}{\varepsilon(r_{a}, x)}\right]^{\frac{3}{2}} \times N_{r}^{\frac{1}{6}} \\ N_{r} \equiv \left(\frac{N^{*}}{N_{CDp}(r_{a}, x)}\right), \\ \Delta E_{gp}(N, r_{a}, x) = \Delta E_{gpo}(N, r_{a}, x) \times \{0.2 \times x + 6 \times (1 - x)\}, \end{split}$$
(14p)

where  $a_1 = 3.15 \times 10^{-3} (eV)$ ,  $a_2 = 5.41 \times 10^{-4} (eV)$ ,  $a_3 = 2.32 \times 10^{-3} (eV)$ ,  $a_4 = 4.12 \times 10^{-3} (eV)$  and  $a_5 = 9.8 \times 10^{-5} (eV)$ .

One also remarks that, as  $N^* = 0$ , according to the MIT,  $\Delta E_{gn(gp)}(N, r_{d(a)}, x) = 0$ .

#### **OPTICAL BAND GAP**

Here, the optical band gap is found to be defined by:

$$E_{gn1(gp1)}(N, r_{d(a)}, x, T) \equiv E_{gni(gpi)}(r_{d(a)}, x, T) - \Delta E_{gn(gp)}(N, r_{d(a)}, x) + (-)E_{Fn(Fp)}(N, r_{d(a)}, x, T) ,$$
(15)

where  $E_{gin(gip)}$ ,  $[+E_{Fn}, -E_{Fp}] \ge 0$ , and  $\Delta E_{gn(gp)}$  are respectively determined in Equations [10, 12, 14n(p)], respectively. So, as noted above, at the MIT, Eq. (15) thus becomes:  $E_{gn1(gp1)}(r_{d(a)}, x) = E_{gno(gpo)}(r_{d(a)}, x)$ , according to:  $N = N_{CDn(NDp)}(r_{d(a)}, x)$ .

#### **OPTICAL COEFFICIENTS**

The optical properties of any medium can be described by the complex refraction index  $\mathbb{N}$  and the complex dielectric function  $\varepsilon$ ,  $\mathbb{N} \equiv n - i\kappa$  and  $\varepsilon \equiv \varepsilon_1 - i\varepsilon_2$ , where  $i^2 = -1$  and  $\varepsilon \equiv \mathbb{N}^2$ . Therefore, the real and imaginary parts of  $\varepsilon$  denoted by  $\varepsilon_1$  and  $\varepsilon_2$  can thus be expressed in terms of the refraction index n and the extinction coefficient  $\kappa$  as:  $\varepsilon_1 \equiv n^2 - \kappa^2$  and  $\varepsilon_2 \equiv 2n\kappa$ . One notes that the optical absorption coefficient  $\alpha$  is related to  $\varepsilon_2$ , n,  $\kappa$ , and the optical conductivity  $\sigma_0$ , by<sup>[2]</sup>

$$\begin{aligned} \alpha(E, N, r_{d(a)}, x, T) &\equiv \frac{\hbar q^2 \times |v(E)|^2}{n(E) \times \epsilon_{free \ space} \times cE} \times J(E^*) = \frac{E \times \epsilon_2(E)}{\hbar cn(E)} \equiv \frac{2E \times \kappa(E)}{\hbar c} \equiv \frac{4\pi \sigma_0(E)}{cn(E) \times \epsilon_{free \ space}} \\ \epsilon_1 &\equiv n^2 - \kappa^2 \ \text{and} \ \epsilon_2 \equiv 2n\kappa, \end{aligned}$$
(16)

where, since  $\mathbf{E} \equiv \hbar \omega$  is the photon energy, the effective photon energy:  $\mathbf{E}^* = \mathbf{E} - \mathbf{E}_{gn1(gp1)}(\mathbf{N}, \mathbf{r}_{d(a)}, \mathbf{x}, \mathbf{T})$  is thus defined as the reduced photon energy.

Here, -q,  $\hbar$ , |v(E)|,  $\omega$ ,  $\varepsilon_{\text{free space}}$ , c and J(E<sup>\*</sup>) respectively represent: the electron charge, Dirac's constant, matrix elements of the velocity operator between valence (conduction)-andconduction (valence) bands in n(p)-type semiconductors, photon frequency, permittivity of free space, velocity of light, and joint density of states. It should be noted that, if the three functions such as:  $|v(E)|^2$ , J(E<sup>\*</sup>) and n(E) are known, then the other optical dispersion functions as those given in Eq. (16) can thus be determined. Moreover, the normal-incidence reflectance, R(E), can be expressed in terms of  $\kappa(E)$  and n(E) as:

$$R(E, N, r_{d(a)}, x, T) = \frac{[n(E)-1]^2 + \kappa(E)^2}{[n(E)+1]^2 + \kappa(E)^2}.$$
(17)

From Equations (16, 17), if the two optical functions,  $\varepsilon_1$  and  $\varepsilon_2$ , (or n and  $\kappa$ ), are both known, the other ones defined above can thus be determined, noting also that:  $E_{gn1(gp1)}(N, r_{d(a)}, x, T) = E_{gn1(gp1)}$ , for a presentation simplicity.

Then, one has:

-at low values of 
$$E \gtrsim E_{gn1(gp1)}$$
,  
 $J_{n(p)}(E, N, r_{d(a)}, x, T) = \frac{1}{2\pi^2} \times \left(\frac{2m_r}{\hbar^2}\right)^{3/2} \times \frac{(E - E_{gn1(gp1)})^{a - (1/2)}}{E_{gn1(gp1)}^{a - (1/2)}} = \frac{1}{2\pi^2} \times \left(\frac{2m_r}{\hbar^2}\right)^{3/2} \times (E - E_{gn1(gp1)})^{1/2}$ , for a=1, (18)

and at large values of  $E > E_{gn1(gp1)}$ ,

$$J_{n(p)}(E, N, r_{d(a)}, x, T) = \frac{1}{2\pi^2} \times \left(\frac{2m_r}{\hbar^2}\right)^{3/2} \times \frac{(E - E_{gn1(gp1)})^{a - (1/2)}}{E_{gn1(gp1)}^{a - 1}} = \frac{1}{2\pi^2} \times \left(\frac{2m_r}{\hbar^2}\right)^{3/2} \times \frac{(E - E_{gn1(gp1)})^2}{E_{gn1(gp1)}^{3/2}},$$

$$(19)$$

Further, one notes that, as  $E \to \infty$ , Forouhi and Bloomer (FB) [4] claimed that  $\kappa(E \to \infty) \to a$  constant, while the  $\kappa(E)$  -expressions, proposed by Van Cong [2] quickly go to 0 as  $E^{-3}$ , and consequently, their numerical results of the optical functions such as:  $\sigma_0(E)$  and  $\alpha(E)$ , given in Eq. (16), both go to 0 as  $E^{-2}$ .

Now, an improved Forouhi-Bloomer parameterization model (FB-PM), used to determine the expressions of the optical coefficients in the degenerate  $n^+(p^+) - p(n) X(x)$ - crystalline alloy, is now proposed as follows. Then, if denoting the functions G(E) and F(E) and by:  $G(E) \equiv \sum_{i=1}^{4} \frac{A_i}{E^2 - B_i E + C_i} \text{ and } F(E) \equiv \sum_{i=1}^{4} \frac{A_i}{E^2 \times (1 + 10^{-4} \times \frac{E}{6}) - B_i E + C_i}, \text{ we propose:}$   $\kappa(E, N, r_{d(a)}, x, T) = G(E) \times E_{gni(gpi)}^{3/2} \times (E^* \equiv E - E_{gn1(gp1)})^{1/2}, \text{ for } E_{gni(gpi)} \leq E \leq 2.3 \text{ eV},$ 

$$= F(E) \times \left(E^* \equiv E - E_{gn1(gp1)}\right)^2, \text{ for } E \ge 2.3 \text{ eV},$$
(20)

being equal to 0 for  $E^* = 0$  (or for  $E = E_{gn1(gp1)}$ ), and also going to 0 as  $E^{-1}$  as  $E \to \infty$ , and further,

$$n(E, N, r_{d(a)}, x, T) = n_{\infty}(r_{d(a)}, x) + \sum_{i=1}^{4} \frac{x_i(E_{gn1(gp1)}) \times E + Y_i(E_{gn1(gp1)})}{E^2 - B_i E + C_i}.$$
(21)

going to a constant as  $E \to \infty$ , since  $n(E \to \infty, r_{d(a)}, x) \to n_{\infty}(r_{d(a)}, x) = \sqrt{\epsilon(r_{d(a)}, x)} \times \frac{\omega_T}{\omega_L}$ ,  $\omega_T = 5.1 \times 10^{13} \text{ s}^{-1}$  [5] and  $\omega_L = 8.9755 \times 10^{13} \text{ s}^{-1}$ .

Here, the other parameters are determined by:

$$\begin{split} X_{i} \big( E_{gn1(gp1)} \big) &= \frac{A_{i}}{Q_{i}} \times \Big[ -\frac{B_{i}^{2}}{2} + E_{gn1(gp1)} B_{i} - E_{gn1(gp1)}^{2} + C_{i} \Big], \\ Y_{i} \big( E_{gn1(gp1)} \big) &= \frac{A_{i}}{Q_{i}} \times \Big[ \frac{B_{i} \times (E_{gn1(gp1)}^{2} + C_{i})}{2} - 2E_{gn1(gp1)} C_{i} \Big], \\ Q_{i} &= \frac{\sqrt{4C_{i} - B_{i}^{2}}}{2}, \text{ where, for } i=(1, 2, 3, and 4), \\ A_{i} &= 1.154 \times A_{i(FB)} = 4.7314 \times 10^{-4}, 0.2314, 0.1118 \text{ and } 0.0116, \\ B_{i} &\equiv B_{i(FB)} = 5.871, 6.154, 9.679 \text{ and } 13.232, \text{ and } C_{i} &\equiv C_{i(FB)} = 8.619, 9.784, 23.803, \text{ and } 44.119. \end{split}$$

Then, as noted above, if the two optical functions, **n** and  $\kappa$ , are both known, the other ones defined in Equations (16, 17) can also be determined.

### NUMERICAL RESULTS

Now, some numerical results of those optical functions are investigated in the n(p)-type  $\mathbf{X}(\mathbf{x}) \equiv \mathbf{GaTe}_{1-\mathbf{x}}\mathbf{Sb}_{\mathbf{x}}$ - crystalline alloy, as follows.

#### A. Metal-insulator transition (MIT)-case

As discussed above, the physical conditions used for the MIT are found to be given by: T=0K,  $N^* = 0$  or  $N = N_{CDn(CDp)}$ , giving rise to:

$$\begin{split} & E_{gn1(gp1)}\big(N^*=0,r_{d(a)},x,T=0\big)=E_{gn1(gp1)}\big(r_{d(a)},x\big)=E_{gn0(gp0)}\big(r_{d(a)},x\big).\\ & \text{Then, in this MIT-case, if }E=E_{gn1(gp1)}\big(r_{d(a)},x\big)=E_{gn0(gp0)}\big(r_{d(a)},x\big), \text{ which can be defined as the critical photon energy: }E\equiv E_{CPE}\big(r_{d(a)},x\big), \text{ one obtains: }\kappa_{MIT}\big(r_{d(a)},x\big)=0 \text{ from Eq. (20), and from Eq. (16): }\epsilon_{2(MIT)}\big(r_{d(a)},x\big)=0, \sigma_{0(MIT)}\big(r_{d(a)},x\big)=0 \text{ and }\alpha_{MIT}\big(r_{d(a)},x\big)=0, \\ & \text{and the other functions such as : }n_{MIT}\big(r_{d(a)},x\big)=0, \\ & \text{model of the constraint of the eq. (16) decrease with increasing }r_{d(a)} \text{ and }E_{CPE}, \\ & \text{as those investigated in Table 1 in Appendix 1.} \end{split}$$

#### **B.** Optical coefficients, obtained as $E \rightarrow \infty$

(21),at any Τ, choice the real In Eq. the of refraction index:  $n(E \to \infty, \mathbf{r}_{d(a)}, x, T) = n_{\infty}(\mathbf{r}_{d(a)}, x) = \sqrt{\epsilon(\mathbf{r}_{d(a)}, x)} \times \frac{\omega_T}{\omega_L}, \quad \omega_T = 5.1 \times 10^{13} \, s^{-1}$  <sup>[5]</sup> and  $\omega_L = 8.9755 \times 10^{13} \, s^{-1}$ , was obtained from the Lyddane-Sachs-Teller relation<sup>[5]</sup>, from which T(L) represent the transverse (longitudinal) optical phonon modes. Then, from Equations (16, 17, 20), from such the asymptotic behavior ( $E \rightarrow \infty$ ), we obtain:  $\kappa_{\infty}(\mathbf{r}_{\mathsf{d}(\mathsf{a})}, x) \to 0 \text{ and } \varepsilon_{2,\infty}(\mathbf{r}_{\mathsf{d}(\mathsf{a})}, x) \to 0, \text{ as } E^{-1}, \text{ so that } \varepsilon_{1,\infty}(\mathbf{r}_{\mathsf{d}(\mathsf{a})}, x), \sigma_{0,\infty}(\mathbf{r}_{\mathsf{d}(\mathsf{a})}, x),$  $\alpha_{\infty}(\mathbf{r}_{d(a)}, \mathbf{x})$  and  $R_{\infty}(\mathbf{r}_{d(a)}, \mathbf{x})$  go to their appropriate limiting constants for T=0K, as those investigated in Table 2 in Appendix 1.

# C. Variations of some optical coefficients, obtained in P(B)-X(x)-system, as functions of E

In the P(B)-X(x)-system, at T=0K and N = N<sub>CDn(CDp</sub>)( $r_{P(B)}$ , x), our numerical results of n,  $\kappa$ ,  $\varepsilon_1$  and  $\varepsilon_2$  are obtained from Equations (21, 20, 16), respectively, and expressed as functions of  $E [\geq E_{CPE}(r_{P(B)}, x)]$  and for given x, as those reported in Tables 3n and 3p in Appendix 1.

#### D. Variations of various optical coefficients, as functions of N

In the X(x)-system, at E=3.2 eV and T=20 K, for given  $r_{d(a)}$  and x, and from Equations (12, 15, 21, 20, 16), respectively, we can determine the variations of  $\eta_{n(p)}$  (>> 1, degenerate case),  $E_{gn1(gp1)}$ , n,  $\kappa$ ,  $\varepsilon_1$  and  $\varepsilon_2$ , obtained as functions of N, being represented by the arrows:  $\nearrow$  and  $\searrow$ , as those tabulated in Tables 4n and 4p in Appendix 1.

#### E. Variations of various optical coefficients as functions of T

In the X(x)-system, at E=3.2 eV and N =  $10^{20}$  cm<sup>-3</sup>, for given  $r_{d(a)}$  and x, and from Equations (12, 15, 21, 20, 16), respectively, we can determine the variations of  $\eta_{n(p)}$  (>> 1, degenerate case),  $E_{gn1(gp1)}$ , n,  $\kappa$ ,  $\varepsilon_1$  and  $\varepsilon_2$ , obtained as functions of T, being represented by the arrows:  $\nearrow$  and  $\searrow$ , as those tabulated in Tables 5n and 5p in Appendix 1.

# **CONCLUDING REMARKS**

In the n(p)-type  $\mathbf{X}(\mathbf{x}) \equiv \mathbf{GaTe_{1-x}Sb_x}$ - crystalline alloy, by basing on our two recent works<sup>[1,2]</sup>, for a given x, and with an increasing  $\mathbf{r}_{d(a)}$ , the optical coefficients have been determined, as functions of the photon energy E, total impurity density N, the donor (acceptor) radius  $\mathbf{r}_{d(a)}$ , concentration x, and temperature T.

Those results have been affected by (i) the important new  $\varepsilon(\mathbf{r}_{d(a)}, \mathbf{x})$ -law, developed in Equations (8a, 8b), stating that, for a given x, due to the impurity-size effect,  $\varepsilon$  decreases ( $\searrow$ ) with an increasing ( $\nearrow$ )  $\mathbf{r}_{d(a)}$ , and then by (ii) the generalized Mott critical d(a)-density defined in the metal-insulator transition (MIT),  $N_{\text{CDn}(\text{NDp})}(\mathbf{r}_{d(a)}, \mathbf{x})$ , as observed in Equations (8c, 9a).

Further, we also showed that  $N_{CDn(NDp)}$  is just the density of carriers localized in exponential band tails, with a precision of the order of 2.87 × 10<sup>-7</sup>, as that given in Table 4 of Ref.<sup>[1]</sup>, according to a definition of the effective density of electrons (holes) given in parabolic conduction (valence) bands by:  $N^*(N, r_{d(a)}, x) \equiv N - N_{CDn(NDp)}(r_{d(a)}, x)$ , as defined in Eq. (9d).

In summary, due to the new  $\varepsilon(r_{d(a)}, x)$ -law and to the effective density of electrons (holes) given in parabolic conduction (valence) bands N<sup>\*</sup>(N, r<sub>d(a)</sub>, x), for a given x, and with an increasing r<sub>d(a)</sub>, the numerical results of all the optical coefficients, obtained in appropriated physical conditions (E, N, T), and calculated by using Equations (15, 16, 20, 21), are reported in Tables 1, 2, 3n, 3p, 4n, 4p, 5n, and 5p in Appendix 1.

# REFERENCES

- Van Cong, H. New critical impurity density in MIT, obtained in various n(p)-type degenerate InAs<sub>1-x</sub>P<sub>x</sub>(Sb<sub>x</sub>), GaTe<sub>1-x</sub>As<sub>x</sub>(Sb<sub>x</sub>, P<sub>x</sub>), CdTe<sub>1-x</sub>S<sub>x</sub>(Se<sub>x</sub>) crystalline alloys, being just that of carriers localized in exponential band tails. (II). WJERT, 2024; 10(4): 65-96.
- Van Cong, H. & Cayrol, M. Optical coefficients in the n(p)-type degenerate GaAs<sub>1-x</sub>P<sub>x</sub>crystalline alloy, due to the new static dielectric constant-law and the generalized Mott
  criterium in the metal-insulator transition. (1). To be published in WJERT, 2024; 10(10):
  205-226.
- Van Cong, H. Effects of donor size and heavy doping on optical, electrical and thermoelectric properties of various degenerate donor-silicon systems at low temperatures. American Journal of Modern Physics, 2018; 7: 136-165.
- Forouhi A. R. & Bloomer I. Optical properties of crystalline semiconductors and dielectrics. Phys. Rev., 1988; 38: 1865-1874.
- Aspnes, D.E. & Studna, A. A. Dielectric functions and optical parameters of Si, Se, GaP, GaAs, GaSb, InP, InAs, and InSb from 1.5 to 6.0 eV, Phys. Rev. B, 1983; 27: 985-1009.
- 6. Van Cong, H. et al. Optical bandgap in various impurity-Si systems from the metalinsulator transition study. Physica B, 2014; 436: 130-139.
- Van Cong, H. et al. Size effect on different impurity levels in semiconductors. Solid State Communications, 1984; 49: 697-699.
- 8. Van Cong, H. & Debiais, G. A simple accurate expression of the reduced Fermi energy for any reduced carrier density. J. Appl. Phys., 1993; 73: 1545-1546.

# **APPENDIX 1**

**Table 1:** In the MIT-case, T=0K, N=N<sub>CDn(p)</sub>( $r_{d(a)}$ , x), and the critical photon energy  $E_{CPE} = E = E_{gno(gpo)}(r_{d(a)}, x)$ , if  $E = E_{gn1(gp1)}(r_{d(a)}, x) = E_{CPE}(r_{d(a)}, x)$ , the numerical results of optical functions such as :  $n_{MIT}(r_{d(a)}, x)$ , obtained from Eq. (21), and those of other ones:  $\varepsilon_{1(MIT)}(r_{d(a)}, x)$  and  $R_{MIT}(r_{d(a)}, x)$ , from Eq. (16), decrease ( $\searrow$ ) with increasing ( $\nearrow$ )  $r_{d(a)}$  and  $E_{CPE}$ .

						=
Donor		Р	Te	Sb	Sn	
<b>r</b> <sub>d</sub> (nm) [4]	7	0.110	0.132	0.136	0.140	
At <b>x=0</b> ,						
E <sub>CPE</sub> in meV	7	1791.7	1796	1796.1	1796.6	
n <sub>MIT</sub>	7	3.315	3.178	3.174	3.161	
$\varepsilon_{1(MIT)}$	2	10.99	10.10	10.07	9.99	
R <sub>MIT</sub>	7	0.288	0.271	0.270	0.2697	
At <b>x=0.5</b> ,						
E <sub>CPE</sub> in meV	7	1300.9	1303	1303.07	1303.3	
n <sub>MIT</sub>	7	3.763	3.618	3.614	3.600	
$\varepsilon_{1(MIT)}$	7	14.16	13.09	13.06	12.96	
R <sub>MIT</sub>	7	0.336	0.321	0.3209	0.3195	
At <b>x=1</b> ,						
E <sub>CPE</sub> in meV	7	809.4	810	810.02	810.09	
n <sub>MIT</sub>	7	4.203	4.050	4.046	4.031	
$\varepsilon_{1(MIT)}$	7	17.66	16.40	16.37	16.25	
R <sub>MIT</sub>	7	0.379	0.365	0.364	0.363	
Acceptor		В	Ga	In	Cd	
r <sub>a</sub> (nm)	7	0.088	0.126	0.144	0.148	
At <b>x=0</b> ,						
E <sub>CPE</sub> in meV	7	1770.5	1796	1803	1807	
n <sub>MIT</sub>	7	3.917	3.178	3.086	3.045	

Cong.		Wo	rld Journal of l	Engineering Res	earch and Technology
$\varepsilon_{1(MIT)}$	7	15.34	10.10	9.522	9.271
R <sub>MIT</sub>	7	0.352	0.272	0.261	0.255
			At <b>x=0.5</b> ,		
E <sub>CPE</sub> in meV	7	1285.7	1303	1307.8	1310.3
n <sub>MIT</sub>	7	4.400	3.618	3.521	3.479
$\varepsilon_{1(MIT)}$	7	19.36	13.09	12.40	12.10
R <sub>MIT</sub>	7	0.396	0.321	0.311	0.306
At <b>x=1</b> ,					
$E_{CPE}$ in meV	7	798.2	810	813.3	815
n <sub>MIT</sub>	7	4.874	4.050	3.949	3.904
$\varepsilon_{1(MIT)}$	7	23.75	16.40	15.60	15.24
R <sub>MIT</sub>	7	0.435	0.365	0.355	0.351

**Table 2**: Here, as T=0K and N=N<sub>CDn(p)</sub>( $r_{d(a)}$ , x), and for  $E \to \infty$  the numerical results of  $n_{\infty}(r_{d(a)}, x)$ ,  $\varepsilon_{1,\infty}(r_{d(a)}, x)$ ,  $\sigma_{0,\infty}(r_{d(a)}, x)$ ,  $\alpha_{\infty}(r_{d(a)}, x)$  and  $R_{\infty}(r_{d(a)}, x)$  go to their appropriate limiting constants.

Donor	Р	Te	Sb	Sn
At <b>x=0</b> ,				
$n_{\infty}$ >	2.1277	1.9928	1.9886	1.9762
ε <sub>1,∞</sub> \	4.5269	3.9712	3.9547	3.9052
$\sigma_{0,\infty}$ in $\frac{10^5}{\Omega \times cm}$ $\searrow$	9.7087	9.0933	9.0743	9.0174
$\propto_{\infty}$ in $(10^9 \times cm^{-1})$	2.1602	2.1602	2.1602	2.1602
$R_{\infty}$ >	0.1230	0.1100	0.1094	0.1076
At <b>x=0.5</b> ,				
$n_{\infty}$ >	2.2695	2.1257	2.1212	2.1079
ε <sub>1,∞</sub> \	5.1508	4.5185	4.4997	4.4434
$\sigma_{0,\infty}$ in $\frac{10^5}{\Omega \times cm}$ $\searrow$	10.3560	9.6996	9.6794	9.6187

	•	
WWW.W	vier	t.org

Cong.	World	Journal of Engi	neering Resear	ch and Technology
$\alpha_{\infty}$ in $(10^9 \times cm^{-1})$	2.1602	2.1602	2.1602	2.1602
$R_{\infty}$ >	0.1508	0.1297	0.1290	0.1271
$n_{\infty}$ >	2.4030	2.2507	2.2460	2.2319
$\varepsilon_{1,\infty}$	5.7746	5.0658	5.0446	4.9816
$\sigma_{0,\infty}$ in $\frac{10^5}{\Omega \times cm}$	10.9652	10.2702	10.2488	10.1845
$\alpha_{\infty}$ in $(10^9 \times cm^{-1})$	2.1602	2.1602	2.1602	2.1602
$R_{\infty}$ >	0.1700	0.1480	0.1473	0.1453
Acceptor	В	Ga	In	Cd
		At <b>x=0</b> ,		
$n_{\infty}$ >	2.716	1.993	1.905	1.866
$\varepsilon_{1,\infty}$	7.374	3.971	3.629	3.483
$\sigma_{0,\infty}$ in $\frac{10^5}{\Omega \times cm}$ $\searrow$	12.39	9.093	8.693	8.517
$\alpha_{\infty}$ in (10 <sup>9</sup> × cm <sup>-1</sup> )	2.160	2.160	2.160	2.160
$R_{\infty}$ >	0.213	0.110	0.097	0.091
<b>x=0.5</b> ,				
$n_{\infty}$ >	2.897	2.126	2.032	1.991
$\varepsilon_{1,\infty}$	8.390	4.518	4.129	3.963
$\sigma_{0,\infty}$ in $\frac{10^5}{\Omega \times cm}$ $\searrow$	13.22	9.700	9.272	9.084
$\alpha_{\infty}$ in (10 <sup>9</sup> × cm <sup>-1</sup> )	2.160	2.160	2.160	2.160
$R_{\infty}$ >	0.237	0.130	0.116	0.110
At <b>x=1</b> ,				
$n_{\infty}$ >	3.067	2.251	2.152	2.108
$\varepsilon_{1,\infty}$	9.407	5.066	4.629	4.444
$\sigma_{0,\infty}$ in $\frac{10^5}{\Omega \times cm}$ $\searrow$	13.99	10.27	9.818	9.619
$\alpha_{\infty}$ in $(10^9 \times cm^{-1})$	2.160	2.160	2.160	2.160
$R_{\infty}$ >	0.258	0.148	0.133	0.127

**Table 3n:** In the P-X(x)-system, and at T=0K and N = N<sub>CDn</sub>(r<sub>p</sub>, x), according to the MIT, our numerical results of n,  $\kappa$ ,  $\varepsilon_1$  and  $\varepsilon_2$  are obtained from Equations (21, 20, 16), respectively, and expressed as functions of  $E \ [\geq E_{CPE}(r_p, x)]$  and x, noting that (i)  $\kappa = 0$  and  $\varepsilon_2 = 0$  at  $E = E_{CPE}(r_p, x)$ , and  $\kappa \to 0$  and  $\varepsilon_2 \to 0$  as  $E \to \infty$ .

E in eV	п	κ	ε	ε2	
		At x=0,			
$E_{CPE} = 1.7917$	2.1277	0	4.5269	0	
2	3.462	0.187	11.949	1.296	
2.5	3.992	0.190	15.898	1.516	
3	4.176	1.199	15.999	10.016	
3.5	3.640	1.520	10.938	11.062	
4	3.771	1.476	12.044	11.134	
4.5	4.085	2.387	10.992	19.502	
5	2.609	3.441	-5.032	17.955	
5.5	1.534	2.487	-3.832	7.632	
6	1.616	1.888	-0.952	6.103	
<b>10</b> <sup>22</sup>	2.1277	0	4.5269	0	
At x=0.5,	2.5(22	0	14.1710	0	
$E_{CPE} = 1.3009$	3.7632	0	14.1618	0	
2	4.383	0.212	19.166	1.860	
2.5	5.183	0.544	26.568	5.642	
3	5.034	2.371	19.719	23.874	
3.5	3.907	2.518	8.921	19.674	
4	4.070	2.205	11.705	17.950	
4.5	4.476	3.330	8.943	29.811	
5	2.471	4.574	-14.812	22.609	
5.5	1.133	3.189	-8.886	7.227	
6	1.303	2.354	-3.843	6.134	
<b>10</b> <sup>22</sup>	2.2695	0	5.1508	0	

=1,

Cong.		World Jou	Irnal of Engineering	g Research a	nd Technology
E <sub>CPE</sub> =0.8094	4.2030	0	17.6654	0	
2	5.479	0.136	30.005	1.489	
2.5	6.594	1.082	42.308	14.270	
3	5.921	3.942	19.516	46.676	
3.5	4.043	3.769	2.136	30.481	
4	4.270	3.081	8.738	26.315	
4.5	4.798	4.432	3.378	42.533	
5	2.198	5.870	-29.627	25.809	
5.5	0.579	3.979	-15.501	4.607	
6	0.863	2.872	-7.504	4.957	
<b>10</b> <sup>22</sup>	2.4030	0	5.7746		0
E in eV	n	κ	ε		ε2

**Table 3p:** In the B-X(x)-system, and at T=0K and N = N<sub>CDp</sub>(r<sub>B</sub>, x), according to the MIT, our numerical results of n,  $\kappa$ ,  $\varepsilon_1$  and  $\varepsilon_2$  are obtained from Equations (21, 20, 16), respectively, and expressed as functions of  $E [\geq E_{CPE}(r_B, x)]$  and x, noting that (i)  $\kappa = 0$  and  $\varepsilon_2 = 0$  at  $E = E_{CPE}(r_B, x)$ , and  $\kappa \to 0$  and  $\varepsilon_2 \to 0$  as  $E \to \infty$ .

E in eV	n	κ	ε	ε2
		At x=0,		
E <sub>CPE</sub> =1.7705	3.9167	0	15.3404	0
2	4.079	0.193	16.606	1.575
2.5	4.620	0.201	21.306	1.862
3	4.794	1.242	21.439	11.906
3.5	4.235	1.557	15.513	13.194
4	4.368	1.505	16.814	13.144
4.5	4.685	2.424	16.073	22.717
5	3.187	3.486	-1.995	22.226
5.5	2.102	2.516	-1.912	10.575
6	2.187	1.907	1.146	8.341

Cong.

World Journal of Engineering Research and Technology

10 <sup>22</sup>	2.7156	0	7.3743	0	
At x=0.5,					
E <sub>CPE</sub> =1.2857	4.3998	0	19.3582	0	
2	5.037	0.211	25.329	2.123	
2.5	5.846	0.558	33.868	6.527	
3	5.684	2.414	26.480	27.441	
3.5	4.536	2.553	14.055	23.159	
4	4.701	2.230	17.124	20.965	
4.5	5.110	3.362	14.807	34.357	
5	3.088	4.611	-11.731	28.481	
5.5	1.741	3.212	-7.287	11.185	
6	1.914	2.369	-1.949	9.070	
<b>10</b> <sup>22</sup>	2.8966	0	8.3905	0	
At x=1,					
E <sub>CPE</sub> =0.7982	4.8740	0	23.7557	0	
2	6.167	0.134	38.019	1.650	
2.5	7.289	1.096	51.934	15.984	
3	6.602	3.982	27.731	52.581	
3.5	4.706	3.801	7.696	35.772	
4	4.934	3.103	14.720	30.623	
4.5	5.466	4.459	9.991	48.745	
5	2.851	5.901	-26.697	33.657	
5.5	1.225	3.998	-14.485	9.800	
6	1.512	2.884	-6.032	8.725	
10 <sup>22</sup>	3.0670	0	9.4067	0	
E in eV	n	κ	$\varepsilon_1$	ε <sub>2</sub>	

# Cong.

**Table 4n:** In the X(x)-system, at E=3.2 eV and T=20 K, for given  $r_d$  and x, and from Equations (12, 15, 21, 20, 16), respectively, we can determine the variations of  $\eta_n \gg 1$ , degenerate case),  $E_{gn1}$ , n,  $\kappa$ ,  $\varepsilon_1$  and  $\varepsilon_2$ , obtained as functions of N, being represented by the arrows:  $\nearrow$  and  $\searrow$ , noting that both  $\eta_n$  and  $E_{gn1}$  increase with increasing N.

N (10 <sup>18</sup> cm	-3) 7	15	26	60	100	
			x=0			
For $\mathbf{r}_{\mathbf{d}} = \mathbf{r}_{\mathbf{T}\mathbf{d}}$	,					
$\eta_n\gg 1$	7	234	340	599	844	
E <sub>gn1</sub> in eV	7	1.672	1.711	1.854	2.026	
n	7	3.994	3.956	3.815	3.641	
κ	7	1.730	1.643	1.342	1.022	
ε <sub>1</sub>	2	12.958	12.951	12.751	12.210	
ε2	7	13.820	13.000	10.241	7.445	
For $\mathbf{r}_{\mathbf{d}} = \mathbf{r}_{\mathbf{S}\mathbf{b}}$	),					
$\eta_n\gg 1$	7	233	340	599	844	
E <sub>gn1</sub> in eV	7	1.674	1.713	1.857	2.029	
n	7	3.988	3.950	3.808	3.632	
κ	7	1.727	1.639	1.337	1.016	
$\varepsilon_1$	7	12.925	12.918	12.713	12.165	
ε2	7	13.776	12.948	10.180	7.382	
For $\mathbf{r}_{\mathbf{d}} = \mathbf{r}_{\mathbf{S}\mathbf{r}}$	 I,					
$\eta_n\gg 1$	7	233	340	599	844	
E <sub>gn1</sub> in eV	7	1.678	1.719	1.866	2.040	
n	7	3.972	3.932	3.787	3.609	
κ	7	1.717	1.627	1.320	0.997	
$\varepsilon_1$	7	12.826	12.81	7 12.598	12.031	
ε2	7	13.644	12.79	9.997	7.197	

		X	=0.5			
For $\mathbf{r}_{\mathbf{d}} = \mathbf{r}_{\mathbf{T}}$	e,					
$\eta_n\gg 1$	7	130	188	329	463	
E <sub>gn1</sub> in eV	7	0.918	0.845	0.720	0.642	
n	7	4.804	4.864	4.965	5.026	
κ	7	3.858	4.111	4.558	4.849	
$\varepsilon_1$	7	8.192	6.761	3.871	1.748	
ε2	7	37.071	39.999	45.266	48.746	
For $\mathbf{r}_{d} = \mathbf{r}_{st}$						
$\eta_n \gg 1$	7	130	188	329	463	
E <sub>gn1</sub> in eV	7	0.920	0.847	0.724	0.647	
n	7	4.798	4.858	4.957	5.018	
κ	7	3.852	4.102	4.544	4.830	
$\varepsilon_1$	7	8.183	6.770	3.925	1.846	
ε2	7	36.963	39.861	45.059	48.478	
For $\mathbf{r}_{\mathbf{d}} = \mathbf{r}_{\mathbf{S}_{\mathbf{f}}}$						
$\eta_n \gg 1$	7	130	188	329	463	
E <sub>gn1</sub> in eV	7	0.926	0.855	0.735	0.662	
n	7	4.780	4.839	4.935	4.993	
κ	7	3.832	4.076	4.503	4.775	
$\varepsilon_1$	7	8.158	6.795	4.081	2.132	
ε2	7	36.641	39.450	44.445	47.683	
			x=1			
For $\mathbf{r_d} = \mathbf{r_T}$	e,					
$\eta_n\gg 1$	7	93.7	135	236	332	2
E <sub>gn1</sub> in eV	7	0.785	0.801	0.850	5 0.92	20
n	7	5.038	5.026	4.98	1 4.92	28
κ	7	4.324	4.267	4.074	4 3.85	53

www wi	iert org
	CI COI S

Cong.			World Journal of Engineering Research and Technology				
ε <sub>1</sub>	7	6.686	7.04	5	8.210	9.437	
ε2	7	43.576	42.8	94	40.588	37.974	
For $\mathbf{r_d} = \mathbf{r_{SI}}$	b,						
$\eta_n \gg 1$	7	93.7	135	236	332		
E <sub>gn1</sub> in eV	7	0.785	0.802	0.857	0.922		
n	7	5.033	5.020	4.975	4.922		-
κ	7	4.322	4.264	4.070	3.847		
ε <sub>1</sub>	7	6.655	7.018	8.190	9.422		
ε2	7	43.506	42.815	40.494	4 37.868	3	
For $\mathbf{r}_{\mathbf{d}} = \mathbf{r}_{\mathbf{S}_{\mathbf{f}}}$	a,						
$\eta_n \gg 1$	7	93.7	135	236	332		
E <sub>gn1</sub> in eV	~	0.787	0.804	0.861	0.927		
n	7	5.017	5.004	4.958	4.903		-
κ	7	4.314	4.255	4.056	3.829		
$\varepsilon_1$	7	6.559	6.936	8.131	9.376		
ε2	7	43.297	42.582	40.213	37.554		
N (10 <sup>18</sup> cm	1 <sup>−3</sup> ) 7	15	26	60	100		-

**Table 4p:** In the X(x)-system, at E=3.2 eV and T=20 K, for given  $r_d$  and x, and from Equations (12, 15, 21, 20, 16), respectively, we can determine the variations of  $\eta_p \gg 1$ , degenerate case),  $E_{gp1}$ , n,  $\kappa$ ,  $\varepsilon_1$  and  $\varepsilon_2$ , obtained as functions of N, being represented by the arrows:  $\nearrow$  and  $\searrow$ , noting that both  $\eta_p$  and  $E_{gp1}$  increase with increasing N.



Cong.			World J	ournal of E	ngineering <b>R</b>	esearch and Technology
$\eta_p \gg 1$	7	199	312	578	826	
E <sub>gp1</sub> in eV	7	2.001	2.150	2.516	2.871	
n	7	3.666	3.511	3.112	2.723	
κ	7	1.066	0.818	0.346	0.080	
ε <sub>1</sub>	7	12.306	11.661	9.566	7.302	
ε2	7	7.820	5.743	2.155	0.434	
For $\mathbf{r}_{\mathbf{a}} = \mathbf{r}_{\mathbf{I}\mathbf{n}}$						
$\eta_p \gg 1$	7	186	302	570	820	
E <sub>gp1</sub> in eV	7	1.997	2.152	2.528	2.889	
n	7	3.582	3.421	3.012	2.594	
κ	7	1.073	0.814	0.335	0.072	
$\varepsilon_1$	7	11.683	11.042	8.958	6.725	
ε2	7	7.688	5.573	2.016	0.372	
For $\mathbf{r}_{\mathbf{a}} = \mathbf{r}_{\mathbf{C}\mathbf{c}}$						
$\eta_p\gg 1$	7	178	296	566	816	
E <sub>gp1</sub> in eV	7	1.993	2.151	2.532	2.896	
n	7	3.548	3.383	2.969	2.547	
κ	7	1.079	0.815	0.331	0.069	
$\varepsilon_1$	7	11.421	10.782	8.703	6.485	
ε2	7	7.659	5.517	1.965	0.349	
			x=0.5			
For $\mathbf{r}_{\mathbf{a}} = \mathbf{r}_{\mathbf{G}}$	a,					
$\eta_p \gg 1$	7	121	181	323	458	
E <sub>gp1</sub> in eV	7	1.403	1.473	1.653	1.831	
n	7	4.381	4.316	4.145	3.971	
κ	7	2.394	2.210	1.774	1.389	
$\varepsilon_1$		13.459 🗡	13.740	14.037 🔪	13.839	
ε2	7	20.978	19.077	14.702	11.035	

For $\mathbf{r}_{\mathbf{a}} = \mathbf{r}_{\mathbf{I}\mathbf{n}}$	1,						
$\eta_p\gg 1$		↗ 118		178	322	457	7
E <sub>gp1</sub> in eV	7	1.409	) 1	1.483	1.668	1.84	49
n	7	4.281		4.213	4.038	3.8	59
κ	7	2.376	5	2.186	1.740	1.35	52
ε <sub>1</sub>		12.68	30 🖊	12.972	13.273	<b>∖</b> 13.0	)64
ε2	7	20.34	.9	18.425	14.056	10.4	136
			For <b>r</b>	$r_{cd}$			
$\eta_n \gg 1$		↗ 116	)	177	321	۷	451
E <sub>gp1</sub> in eV	7	1.41	2	1.486	1.674	- 1	.857
n	7	4.23	7	4.169	3.990	) 3	3.810
κ	7	2.36	59	2.176	1.727	/ 1	1.336
$\varepsilon_1$		12.3	342 🖊	12.640	12.94	3 🖌 1	12.729
ε2	7	20.0	)80	18.147	13.78	80 1	10.182
 x=1							
For $\mathbf{r}_{a} = \mathbf{r}_{Ga}$	a,						
$\eta_p \gg 1$		<b>↗</b> 91		133	234	330	
E <sub>gp1</sub> in eV	7	0.955	i	1.024	1.193	1.35	54
n	7	4.899	)	4.840	4.694	4.55	51
κ	7	3.736	5	3.508	2.985	2.52	26
$\varepsilon_1$	7	10.03	7	11.117	13.125	14.3	325
ε2	7	36.60	07	33.964	28.024	22.9	994
$\Gamma_{a} = \Gamma_{ln}$	l,	Z 0∩		132	234	22	0
	-	70 0.057	1	1.027	1 107	1.2	50
Egp1 in eV		0.957		1.027	1.197	1.3	58
n	7	4.798	2	4.739	4.592	4.44	18
κ	7	3.729		3.500	2.974	2.51	15

Cong.			World Journal of Engineering Research and Technology				
$\varepsilon_1$	7	9.114	10.207	12.238	13.455		
ε2	7	33.781	33.170	27.320	22.378		
For $\mathbf{r}_{\mathbf{a}} = \mathbf{r}_{\mathbf{C}}$							
$\eta_p\gg 1$	7	89	131	233	329		
E <sub>gp1</sub> in eV	7	0.958	1.028	1.198	1.360		
n	7	4.753	4.694	4.547	4.402		
κ	7	3.725	3.496	2.970	2.510		
ε <sub>1</sub>	7	8.715	9.814	11.855	13.080		
ε2	7	35.416	32.818	27.008	22.104		
N (10 <sup>18</sup> cm	n <sup>-3</sup> ) /	15	26	60	100		

**Table 5n:** In the X(x)-system, at E=3.2 eV and N =  $10^{20}$  cm<sup>-3</sup>, for given r<sub>d</sub> and x, and from Equations (12, 15, 21, 20, 16), respectively, we can determine the variations of  $\eta_n \gg 1$ , degenerate case), E<sub>gn1</sub>, n,  $\kappa$ ,  $\varepsilon_1$  and  $\varepsilon_2$ , obtained as functions of T, being represented by the arrows:  $\nearrow$  and  $\searrow$ , noting that both  $\eta_n$  and E<sub>gn1</sub> decrease with increasing T.

T in K	7	20	50	100	300
			x=0		
For $\mathbf{r}_{\mathbf{d}} = \mathbf{r}_{\mathbf{T}_{\mathbf{d}}}$	e,				
$\eta_n \gg 1$	7	844	338	169	9 56
E <sub>gn1</sub> in eV	7	2.026	2.021	2.011	1.956
n	7 3	.641	3.645	3.656	3.712
κ	↗ 1.02	22	1.030	1.048	1.147
$\varepsilon_1$	7	12.210	12.227	12.267	12.463
ε2	7	7.445	7.508	7.665	8.512
For $\mathbf{r}_{\mathbf{d}} = \mathbf{r}_{\mathbf{S}\mathbf{k}}$	),				
$\eta_n \gg 1$	7	844	338	169	56
E <sub>gn1</sub> in eV	7	2.029	2.025	2.014	1.960

Cong.			World Jo	ournal of E	ngineering Re	search and Technology
n	7	3.633	3.638	3.648	3.704	
κ	7	1.016	1.023	1.042	1.140	
ε <sub>1</sub>	7	12.165	12.182	12.223	12.420	
ε2	7	7.382	7.445	7.601	8.444	
						-
For $\mathbf{r}_{\mathbf{d}} = \mathbf{r}_{\mathbf{Sr}}$	1,					
$\eta_n\gg 1$	7	844	337	169	56	
E <sub>gn1</sub> in eV	7	2.040	2.036	2.025	1.971	
n	7	3.609	3.613	3.624	3.680	
κ	7	0.997	1.004	1.023	1.120	
ε <sub>1</sub>	7	12.031	12.048	12.090	12.291	
ε2	7	7.197	7.259	7.413	8.243	
			x=0.5			
For $\mathbf{r}_{\mathbf{d}} = \mathbf{r}_{\mathbf{T}_{\mathbf{d}}}$	в,					
$\eta_n\gg 1$	7	463	185	92.6	31	
E <sub>gn1</sub> in eV	7	0.642	0.638	0.626	0.559	
n	7	5.026	5.029	5.038	5.090	
κ	7	4.849	4.865	4.909	5.169	
$\varepsilon_1$	7	1.748	1.623	1.284	-0.806	
ε2	7	48.746	48.943	49.472	52.620	
						-
For $\mathbf{r}_{\mathbf{d}} = \mathbf{r}_{\mathbf{S}\mathbf{k}}$	),					
$\eta_n\gg 1$	7	463	185	92.6	31	
Egn1 in eV	7	0.647	0.643	0.631	0.564	
n	7	5.018	5.021	5.030	5.082	
κ	7	4.830	4.847	4.891	5.149	
<i>ε</i> <sub>1</sub>	7	1.846	1.722	1.385	-0.690	
ε2	7	48.478	48.674	49.202	52.339	
						-
For $\mathbf{r}_d = \mathbf{r}_{Sr}$	1,	162	195	02 6	21	
י יי n <sup>יי</sup> חוי	И	403	103	92.0	51	

E <sub>gn1</sub> in eV	7	0.662	0.658	0.646	0.579	
n	7	4.993	4.996	5.005	5.057	
κ	7	4.775	4.791	4.835	5.092	
$\varepsilon_1$	7	2.132	2.010	1.681	-0.351	
ε <sub>2</sub>	7	47.683	47.877	48.400	51.505	
			x=1			
For $\mathbf{r}_{d} = \mathbf{r}_{Te}$	2,	222	100			
$\eta_n \gg 1$	7	332	133	66	22	
E <sub>gn1</sub> in eV	7	0.920	0.916	0.903	0.824	
n	7	4.928	4.931	4.942	5.007	
κ	7	3.853	3.868	3.910	4.186	
$\varepsilon_1$	7	9.437	9.358	9.129	7.546	
ε <sub>2</sub>	7	37.974	38.148	38.649	41.920	
						-
For $\mathbf{r}_{\mathbf{d}} = \mathbf{r}_{\mathbf{St}}$	),					
$\eta_n \gg 1$	7	332	133	66	22	
E <sub>gn1</sub> in eV	7	0.922	0.917	0.905	0.825	
n	7	4.922	4.925	4.936	5.001	
κ	7	3.847	3.862	3.904	4.180	
$\varepsilon_1$	2	9.422	9.343	9.115	7.536	
ε2	7	37.868	38.042	38.542	41.808	
						-
For $\mathbf{r}_{d} = \mathbf{r}_{Sr}$	1,	222	122		22	
$\eta_n \gg 1$	7	332	133	66	22	
E <sub>gn1</sub> in eV	7	0.927	0.923	0.910	0.831	
n	7	4.903	4.907	4.917	4.982	
κ	7	3.829	3.844	3.887	4.162	
$\varepsilon_1$	7	9.376	9.298	9.072	7.506	
ε2	7	37.554	37.727	38.224	41.472	
T in K	7	20	50	100	300	

# Cong.

**Table 5p:** In the X(x)-system, at E=3.2 eV and N =  $10^{20}$  cm<sup>-3</sup>, for given r<sub>a</sub> and x, and from Equations (12, 15, 21, 20, 16), respectively, we can determine the variations of  $\eta_p$  ( $\gg 1$ , degenerate case),  $E_{gp1}$ , n,  $\kappa$ ,  $\varepsilon_1$  and  $\varepsilon_2$ , obtained as functions of T, being represented by the arrows:  $\nearrow$  and  $\searrow$ , noting that both  $\eta_p$  and  $E_{gp1}$  decrease with increasing T.

T in K	7	20	50	100	300	
			x=0			
For $\mathbf{r}_{\mathbf{a}} = \mathbf{r}_{\mathbf{G}}$	a,					
$\eta_p\gg 1$	7	826	331	165	55	
E <sub>gp1</sub> in eV	7	2.871	2.866	2.856	2.801	
n	7	2.703	2.708	2.721	2.785	
κ	7	0.080	0.082	0.088	0.118	
ε <sub>1</sub>	7	7.302	7.329	7.396	7.744	
ε2	7	0.434	0.446	0.477	0.656	
For $\mathbf{r}_{\mathbf{a}} = \mathbf{r}_{\mathbf{I}\mathbf{r}}$						
$\eta_p\gg 1$	7	820	328	164	55	
E <sub>gp1</sub> in eV	7	2.889	2.884	2.874	2.819	
n	7	2.594	2.599	2.612	2.676	
κ	7	0.072	0.074	0.079	0.107	
ε <sub>1</sub>	7	6.725	6.751	6.816	7.151	
ε2	7	0.372	0.383	0.411	0.574	
For $\mathbf{r}_{\mathbf{a}} = \mathbf{r}_{\mathbf{C}}$	d,					
$\eta_p \gg 1$	7	816	327	163	54	
E <sub>gp1</sub> in eV	7	2.896	2.891	2.881	2.826	
n	7	2.547	2.552	2.565	2.629	
κ	7	0.069	0.070	0.075	0.103	
$\varepsilon_1$	7	6.485	6.510	6.573	6.904	
ε2	7	0.349	0.360	0.387	0.544	

x=0.5						
For $\mathbf{r}_{\mathbf{a}} = \mathbf{r}_{\mathbf{G}}$	a,					
$\eta_p \gg 1$	7	458	183	92	30	
E <sub>gp1</sub> in eV	7	1.831	1.827	1.815	1.748	
n	7	3.971	3.975	3.987	4.053	
κ	7	1.389	1.398	1.422	1.563	
ε <sub>1</sub>	7	13.839	13.848	13.873	13.985	
ε2	7	11.035	11.117	11.339	12.669	
For $\mathbf{r}_{\mathbf{a}} = \mathbf{r}_{\mathbf{I}\mathbf{r}}$						-
$\eta_p\gg 1$	7	457	183	91	30	
E <sub>gp1</sub> in eV	7	1.849	1.845	1.834	1.766	
n	7	3.859	3.863	3.875	3.941	
κ	7	1.352	1.361	1.384	1.523	
ε1	7	13.064	13.073	13.099	13.213	
ε2	7	10.436	10.515	10.726	12.008	
For $\mathbf{r}_{\mathbf{a}} = \mathbf{r}_{\mathbf{C}}$	d,					-
$\eta_p\gg 1$	7	456	182	91	30	
E <sub>gp1</sub> in eV	7	1.857	1.853	1.841	1.774	
n	7	3.810	3.814	3.826	3.892	
κ	7	1.336	1.345	1.368	1.506	
ε <sub>1</sub>	7	12.729	12.739	12.764	12.880	
ε2	7	10.182	10.259	10.467	11.727	
 x=1						
For $\mathbf{r}_{\mathbf{a}} = \mathbf{r}_{\mathbf{G}}$	a,					
$\eta_p\gg 1$	7	330	132	66	22	
E <sub>gp1</sub> in eV	7	1.354	1.349	1.337	1.257	
n	7	4.551	4.554	4.566	4.637	

Cong.			World Jo	urnal of Eng	gineering Res	earch and Technology
κ	7	2.526	2.538	2.573	2.797	
ε <sub>1</sub>	7	14.325	14.300	14.228	13.680	
ε2	7	22.994	23.123	23.496	25.947	
For $\mathbf{r}_{\mathbf{a}} = \mathbf{r}_{\mathbf{I}\mathbf{n}}$	l,					
$\eta_p\gg 1$	7	330	132	66	22	
Egp1 in eV	7	1.358	1.353	1.341	1.261	
n	7	4.448	4.452	4.463	4.535	
κ	7	2.515	2.527	2.562	2.786	
$\varepsilon_1$	7	13.455	13.430	13.357	12.802	
ε2	7	22.378	22.504	22.869	25.269	
For $\mathbf{r}_{\mathbf{a}} = \mathbf{r}_{\mathbf{C}}$	□,					
$\eta_p \gg 1$	7	329	132	66	22	
Egp1 in eV	7	1.360	1.355	1.343	1.263	
n	7	4.402	4.406	4.418	4.489	
κ	7	2.510	2.522	2.557	2.781	
$\varepsilon_1$	7	13.080	13.055	12.981	12.424	
ε2	7	22.104	22.230	22.591	24.968	
T in K	7	20	50	100	300	