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# OPTICAL COEFFICIENTS IN THE N(P)-TYPE DEGENERATE CdS(1-x) Te(x)-CRYSTALLINE ALLOY, DUE TO THE NEW STATIC DIELECTRIC CONSTANT-LAW AND THE GENERALIZED MOTT CRITERIUM IN THE METAL-INSULATOR TRANSITION. (4)

Prof. Dr. Huynh Van Cong\*

Université de Perpignan Via Domitia, Laboratoire de Mathématiques et Physique (LAMPS),

EA

4217, Département de Physique, 52, Avenue Paul Alduy, F-66 860 Perpignan, France.

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#### \*Corresponding Author Prof. Dr. Huynh Van Cong

Université de Perpignan Via Domitia, Laboratoire de Mathématiques et Physique (LAMPS), EA 4217, Département de Physique, 52, Avenue Paul Alduy, F-66 860 Perpignan, France.

#### **ABTRACT**

In the n(p)-type  $CdS_{1-x}Te_x$ - crystalline alloy, with  $0 \le x \le 1$ , basing on our two recent works<sup>[1,2]</sup>, for a given x, and with an increasing  $r_{d(a)}$ , the optical coefficients have been determined, as functions of the photon energy E, total impurity density N, the donor (acceptor) radius  $r_{d(a)}$ , concentration x, and temperature T. Those results have been affected by (i) the important new  $\varepsilon(r_{d(a)}, x)$ -law, developed in Equations (8a, 8b), stating that, for a given x, due to the impurity-size effect,  $\varepsilon$  decreases (\(\Sigma\)) with an increasing (\(\sigma\))  $r_{d(a)}$ , and then by (ii) the generalized Mott critical d(a)-density defined in the metal-insulator transition (MIT),  $N_{CDn(NDp)}(r_{d(a)}, x)$ , as observed in Equations (8c, 9a). Furthermore, we also showed that  $N_{CDn(NDp)}$  is just the density of

carriers localized in exponential band tails, with a precision of the order of  $2.84 \times 10^{-7}$ , as that given in Table 4 of Ref. [1], according to a definition of the effective density of electrons (holes) given in parabolic conduction (valence) bands by:  $N^*(N, r_{d(a)}, x) \equiv N - N_{CDn(NDp)}(r_{d(a)}, x)$ , as defined in Eq. (9d). In summary, due to the new  $\epsilon(r_{d(a)}, x)$ -law and to the effective density of electrons (holes) given in parabolic conduction (valence) bands  $N^*(N, r_{d(a)}, x)$ , for a given x, and with an increasing  $r_{d(a)}$ , the numerical

results of all the optical coefficients, obtained in appropriated physical conditions (E, N, T), and calculated by using Equations (15, 16, 20, 21), are reported in Tables 1, 2, 3n, 3p, 4n, 4p, 5n, and 5p in Appendix 1.

**KEYWORS:**  $CdS_{1-x}Te_x$  - crystalline alloy; impurity-size effect; Mott critical impurity density in the MIT, optical coefficients.

#### INTRODUCTION

Here, basing on our two recent works<sup>[1,2]</sup> and also other ones<sup>[3-8]</sup>, all the optical coefficients given in the n(p)-type  $\mathbf{X}(\mathbf{x}) \equiv \mathbf{CdS_{1-x}Te_x}$  - crystalline alloy, with  $0 \le x \le 1$ , are investigated, as functions of the photon energy E, total impurity density N, the donor (acceptor) radius  $\mathbf{r_{d(a)}}$ , concentration x, and temperature T.

Then, for a given x, and with an increasing  $r_{d(a)}$ , the numerical results of all the optical coefficients, obtained in appropriated physical conditions (E, N, T), and calculated by using Equations (15, 16, 20, 21), are reported in Tables 1, 2, 3n, 3p, 4n, 4p, 5n, and 5p in Appendix 1.

#### **ENERGY BAND STUCTURE PARAMETERS**

First of all, in the  $n^+(p^+) - p(n) \mathbf{X}(\mathbf{x}) \equiv \mathbf{CdS_{1-x}Te_x}$ - crystalline alloy at T=0 K, we denote the donor (acceptor) d(a)-radius by  $\mathbf{r_{d(a)}}$ , and also the intrinsic one by:  $\mathbf{r_{do(ao)}} = \mathbf{r_{S(Cd)}} = 0.104$  nm (0.148 nm).

#### A. Effect of x- concentration

Here, the intrinsic energy-band-structure parameters [1], are expressed as functions of x, are given in the following.

(i)-The unperturbed relative effective electron (hole) mass in conduction (valence) bands are given by.

$$m_{c(v)}(x)/m_o = 0.095(0.82) \times x + 0.197(0.801) \times (1 - x)$$
(1)

(ii)-The unperturbed relative static dielectric constant of the intrinsic of the single crystalline X- alloy is found to be defined by:

$$\varepsilon_{o}(x) = 10.31 \times x + 9 \times (1 - x).$$
(2)

(iii)-Finally, the unperturbed band gap at 0 K is found to be given by:

$$E_{go}(x) = 1.62 \times x + 2.58 \times (1 - x).$$

(3)

Therefore, we can define the effective donor (acceptor)-ionization energy in absolute values as.

$$E_{do(ao)}(x) = \frac{13600 \times [m_{C(v)}(x)/m_0]}{[\epsilon_0(x)]^2} \text{ meV}, \tag{4}$$

and then, the isothermal bulk modulus, by:

$$B_{do(ao)}(x) \equiv \frac{E_{do(ao)}(x)}{\left(\frac{4\pi}{3}\right) \times \left(r_{do(ao)}\right)^3}.$$
 (5)

#### B. Effect of Impurity $r_{d(a)}$ -size, with a given x

Here, the changes in all the energy-band-structure parameters, expressed in terms of the effective relative dielectric constant  $\varepsilon(r_{d(a)}, x)$ , developed as follows.

At  $r_{d(a)} = r_{do(ao)}$ , the needed boundary conditions are found to be, for the impurity-atom volume  $V = (4\pi/3) \times \left(r_{d(a)}\right)^3$ ,  $V_{do(ao)} = (4\pi/3) \times \left(r_{do(ao)}\right)^3$ , for the pressure  $p, p_o = 0$ , and for the deformation potential energy (or the strain energy)  $\sigma, \sigma_o = 0$ . Further, the two important equations<sup>[1, 7]</sup>, used to determine the  $\sigma$ -variation,  $\Delta \sigma \equiv \sigma - \sigma_o = \sigma$ , are defined by:  $\frac{dp}{dv} = \frac{B}{v}$  and  $p = \frac{d\sigma}{dv}$ . giving:  $\frac{d}{dv}(\frac{d\sigma}{dv}) = \frac{B}{v}$ . Then, by an integration, one gets.

$$\begin{split} \left[\Delta\sigma(r_{d(a)},x)\right]_{n(p)} &= B_{do(ao)}(x) \times (V-V_{do(ao)}) \times \ln \\ (\frac{v}{v_{do(ao)}}) &= E_{do(ao)}(x) \times \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln \left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 \geq 0 \\ (6) &= E_{do(ao)}(x) \times \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln \left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 \geq 0 \end{split}$$

Furthermore, we also showed that, as  $r_{d(a)} > r_{do(ao)}$  ( $r_{d(a)} < r_{do(ao)}$ ), the compression (dilatation) gives rise to the increase (the decrease) in the energy gap  $E_{gn(gp)}(r_{d(a)},x)$ , and the effective donor (acceptor)-ionization energy  $E_{d(a)}(r_{d(a)},x)$  in absolute values, obtained in the effective Bohr model, which is represented respectively by:  $\pm \left[\Delta\sigma(r_{d(a)},x)\right]_{n(p)}$ ,

$$\begin{split} &E_{gno(gpo)}(r_{d(a)},x)-E_{go}(x)=E_{d(a)}(r_{d(a)},x)-E_{do(ao)}(x)=E_{do(ao)}(x)\times\left[\left(\frac{\epsilon_0(x)}{\epsilon(r_{d(a)})}\right)^2-1\right]=\\ &+\left[\Delta\sigma(r_{d(a)},x)\right]_{n(p)}, \text{ for } r_{d(a)}\geq r_{do(ao)}, \text{ and for } r_{d(a)}\leq r_{do(ao)}, \end{split}$$

$$E_{gno(gpo)}(r_{d(a)}, x) - E_{go}(x) = E_{d(a)}(r_{d(a)}, x) - E_{do(ao)}(x) = E_{do(ao)}(x) \times \left[ \left( \frac{\varepsilon_0(x)}{\varepsilon(r_{d(a)})} \right)^2 - 1 \right] = -\left[ \Delta \sigma(r_{d(a)}, x) \right]_{n(p)}$$
(7)

Therefore, from Equations (6) and (7), one obtains the expressions for relative dielectric constant  $\varepsilon(\mathbf{r}_{d(a)}, \mathbf{x})$  and energy band gap  $\mathbf{E}_{gn(gp)}(\mathbf{r}_{d(a)}, \mathbf{x})$ , as.

$$\text{(i)-for } r_{d(a)} \geq r_{do(ao)}, \quad \text{since } \epsilon(r_{d(a)}, x) = \frac{\epsilon_0(x)}{\sqrt{1 + \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3}} \leq \epsilon_o(x), \text{ being a new } \epsilon(x)$$

 $\varepsilon(\mathbf{r}_{\mathbf{d}(\mathbf{a})},\mathbf{x})$ -law,

$$\begin{split} E_{gno(gpo)}\big(r_{d(a)},x\big) - E_{go}(x) &= E_{d(a)}\big(r_{d(a)},x\big) - E_{do(ao)}(x) = E_{do(ao)}(x) \times \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \\ \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 &\geq 0, \\ (8a) \end{split}$$

according to the increase in both  $E_{gn(gp)}(r_{d(a)},x)$  and  $E_{d(a)}(r_{d(a)},x)$ , with increasing  $r_{d(a)}$  and for a given x, and

$$\text{(ii)-for } r_{d(a)} \leq r_{do(ao)} \text{ , since } \epsilon(r_{d(a)},x) = \frac{\epsilon_0(x)}{\sqrt{1 - \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3}} \ \geq \ \epsilon_0(x) \text{ , with a}$$

$$\text{condition, given by: } \left[ \left( \frac{r_{d(a)}}{r_{do(ao)}} \right)^3 - 1 \right] \times \ln \left( \frac{r_{d(a)}}{r_{do(ao)}} \right)^3 < 1, \text{ being a new } \epsilon(r_{d(a)}, x) \text{-law,}$$

$$\begin{split} E_{gno(gpo)}\big(r_{d(a)},x\big) - E_{go}(x) &= E_{d(a)}\big(r_{d(a)},x\big) - E_{do(ao)}(x) = -E_{do(ao)}(x) \times \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \\ &\ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 \\ &\leq 0\,, \end{split} \tag{8b}$$

corresponding to the decrease in both  $E_{gn(gp)}(r_{d(a)},x)$  and  $E_{d(a)}(r_{d(a)},x)$ , with decreasing  $r_{d(a)}$  and for a given x; therefore, the effective Bohr radius  $a_{Bn(Bp)}(r_{d(a)},x)$  is defined by.

$$a_{Bn(Bp)}(r_{d(a)},x) \equiv \frac{\epsilon(r_{d(a)},x) \times \hbar^2}{m_{c(v)}(x) \times q^2} = 0.53 \times 10^{-8} \text{ cm} \times \frac{\epsilon(r_{d(a)},x)}{m_{c(v)}(x)/m_0}. \tag{8c}$$

Furthermore, it is interesting to remark that the critical total donor (acceptor)-density in the metal-insulator transition (MIT) at T=0 K,  $N_{CDn(NDp)}(r_{d(a)},x)$ , was given by the Mott's criterium, with an empirical parameter,  $M_{n(p)}$ , as.

$$N_{CDn(CDp)}(r_{d(a)}, x)^{1/3} \times a_{Bn(Bp)}(r_{d(a)}, x) = M_{n(p)}, M_{n(p)} = 0.25,$$
(9a)

depending thus on our new  $\varepsilon(r_{d(a)}, x)$ -law.

This excellent one can be explained from the definition of the reduced effective Wigner-Seitz (WS) radius  $r_{sn(sp)}$ , characteristic of interactions, by.

$$r_{sn(sp)}(N, r_{d(a)}, x) \equiv \left(\frac{3}{4\pi N}\right)^{1/3} \times \frac{1}{a_{Bn(Bp)}(r_{d(a)}, x)} = 1.1723 \times 10^8 \times \left(\frac{1}{N}\right)^{1/3} \times \frac{m_{C(v)}(x)/m_0}{\epsilon(r_{d(a)}, x)}$$
(9b)

being equal to, in particular, at  $N=N_{CDn(CDp)}(r_{d(a)},x)$ :  $r_{sn(sp)}(N_{CDn(CDp)}(r_{d(a)},x), r_{d(a)},x)=$  **2.4814**, for any  $(r_{d(a)},x)$ -values. So, from Eq. (9b), one also has.

$$N_{CDn(CDp)}(r_{d(a)}, x)^{1/3} \times a_{Bn(Bp)}(r_{d(a)}, x) = \left(\frac{3}{4\pi}\right)^{\frac{1}{3}} \times \frac{1}{2.4814} = 0.25 = (WS)_{n(p)} = M_{n(p)}$$
(9c)

Thus, the above Equations (9a, 9b, 9c) confirm our new  $\varepsilon(r_{d(a)}, x)$ -law, given in Equations (8a, 8b).

Furthermore, by using  $M_{n(p)} = 0.25$ , according to the empirical Heisenberg parameter  $\mathcal{H}_{n(p)} = 0.47137$ , as those given in Equations (8, 15) of the Ref.<sup>[1]</sup>, we have also showed that  $N_{\text{CDn(CDp)}}$  is just the density of electrons (holes) localized in the exponential conduction (valence)-band tail, with a precision of the order of  $2.84 \times 10^{-7}$ . Therefore, the density of electrons (holes) given in parabolic conduction (valence) bands can be defined, as that given in compensated materials, by.

$$N^*(N, r_{d(a)}, x) \equiv N - N_{CDn(NDp)}(r_{d(a)}, x).$$
(9d)

#### C. Effect of temperature T, with given x and $r_{d(a)}$

Here, the intrinsic band gap  $E_{gni(gpi)}(r_{d(a)}, x, T)$  at any T is given by:

$$E_{gni(gpi)}(r_{d(a)},x,T) \text{ in eV} = E_{gno(gpo)}(r_{d(a)},x) - 10^{-4} \times T^2 \times \left\{ \frac{4.3779 \times x}{T+94 \text{ K}} + \frac{7.0043 \times (1-x)}{T+94 \text{ K}} \right\}, \tag{10}$$

suggesting that, for given x and  $r_{d(a)}$ ,  $E_{gni(gpi)}$  decreases with an increasing T.

Then, in the following, for the study of optical phenomena, one denote the conduction (valence)-band density of states by  $N_{c(v)}(T,x)$  as.

$$N_{c(v)}(T,x) = 2 \times g_{c(v)}(x) \times \left(\frac{m_{\Gamma}(x) \times k_{B}T}{2\pi\hbar^{2}}\right)^{\frac{3}{2}} (cm^{-3}), \qquad g_{v}(x) \equiv 1 \times x + 1 \times (1-x) = 1,$$
(11)

where  $m_r(x)/m_o$  is the reduced effective mass  $m_r(x)/m_o$ , defined by.

$$m_r(x) \equiv [m_c(x) \times m_v(x)]/[m_c(x) + m_v(x)].$$

#### D. Heavy Doping Effect, with given T, x and $r_{d(a)}$

Here, as given in our previous works<sup>[1,2]</sup>, the Fermi energy  $E_{Fn}(-E_{Fp})$ , and the band gap narrowing are reported in the following.

First, the reduced Fermi energy  $\eta_{n(p)}$  or the Fermi energy  $E_{Fn}(-E_{Fp})$ , obtained for any T and any effective d(a)-density,  $N^*(N,r_{d(a)},x)=N^*$ , defined in Eq. (9d), for a simplicity of presentation, being investigated in our previous paper<sup>[8]</sup>, with a precision of the order of  $2.11 \times 10^{-4}$ , is found to be given by.

$$\eta_{n(p)}(u) \equiv \frac{E_{Fn}(u)}{k_BT} \big(\frac{-E_{Fp}(u)}{k_BT}\big) = \frac{G(u) + Au^BF(u)}{1 + Au^B} \quad , \quad A = 0.0005372 \quad \text{ and } \quad B = 4.82842262, \label{eq:eta_n(p)}$$
 (12)

where u is the reduced electron density,  $u(N,r_{d(a)},x,T)\equiv \frac{N^*}{N_{c(v)}(T,x)}$  ,

$$F(u) = au^{\frac{2}{3}} \Big( 1 + bu^{-\frac{4}{3}} + cu^{-\frac{8}{3}} \Big)^{-\frac{2}{3}}, \ \ a = \left[ (3\sqrt{\pi}/4) \times u \right]^{2/3}, \ \ b = \frac{1}{8} \Big( \frac{\pi}{a} \Big)^2 \ , \ c = \frac{62.3739855}{1920} \Big( \frac{\pi}{a} \Big)^4,$$

and 
$$G(u) \simeq Ln(u) + 2^{-\frac{3}{2}} \times u \times e^{-du}; \ d = 2^{3/2} \left[ \frac{1}{\sqrt{27}} - \frac{3}{16} \right] > 0.$$
 Therefore, from Eq. (12), the

Fermi energies are expressed as functions of variables:  $N, r_{d(a)}, x, and T$ .

Here, one notes that: (i) as  $u\gg 1$ , according to the HD [d(a)- X(x)- alloy] ER-case, or to the degenerate case, Eq. (12) is reduced to the function F(u), and in particular at T=0 and as  $N^*=0$ , according to the metal-insulator transition (MIT), one has:  $+E_{Fn}(-E_{Fp})=\frac{\hbar^2}{2\times m_r(x)}\times (3\pi^2N^*)^{2/3}=0$ , and (ii)  $\frac{E_{Fn}(u\ll 1)}{k_BT}(\frac{-E_{Fp}(u\ll 1)}{k_BT})\ll -1$ , to the LD [a(d)- X(x)- alloy] BR-case, or to the non-degenerate case, Eq. (12) is reduced to the function G(u), noting that the notations: **HD(LD)** and **ER(BR)** denote the heavily doped (lightly doped)-cases and emitter (base)-regions, respectively.

Now, in Eq. (9b), in which one replaces  $m_{c(v)}(x)$  by  $m_r(x)$ , the effective Wigner-Seitz radius becomes as.

$$r_{sn(sp)}(N, r_{d(a)}, x) = 1.1723 \times 10^8 \times \left(\frac{g_{c(v)}(x)}{N^*}\right)^{1/3} \times \frac{m_r(x)}{\varepsilon(r_{d(a)}, x)},$$
(13a)

the correlation energy of an effective electron gas,  $E_{cn(cp)}(N, r_{d(a)}, x)$ , is given as.

$$E_{cn(cp)}\big(N, r_{d(a)}, x\big) = \frac{-0.87553}{0.0908 + r_{sn(sp)}} + \frac{\frac{0.87553}{0.0908 + r_{sn(sp)}} + \left(\frac{2[1 - \ln(2)]}{\pi^2}\right) \times \ln(r_{sn(sp)}) - 0.093288}{1 + 0.03847728 \times r_{sn(sp)}^{1.67378876}}$$

$$(13b)$$

Then, taking into account various spin-polarized chemical potential-energy contributions such as: exchange energy of an effective electron (hole) gas, majority-carrier correlation energy of an effective electron (hole) gas, minority hole (electron) correlation energy, majority electron (hole)-ionized d(a) interaction screened Coulomb potential energy, and finally minority hole (electron)-ionized d(a) interaction screened Coulomb potential energy, the band gap narrowings are given in the following.

In the n-type HD X(x)- alloy, the BGN is found to be given by.

$$\begin{split} \Delta E_{gn}(N,r_{d},x) &\simeq a_{1} \times \frac{\varepsilon_{0}(x)}{\varepsilon(r_{d},x)} \times N_{r}^{1/3} + a_{2} \times \frac{\varepsilon_{0}(x)}{\varepsilon(r_{d},x)} \times N_{r}^{\frac{1}{3}} \times (2.503 \times [-E_{cn}(r_{sn}) \times r_{sn}]) + a_{3} \times \\ \left[\frac{\varepsilon_{0}(x)}{\varepsilon(r_{d},x)}\right]^{5/4} &\times \sqrt{\frac{m_{v}}{m_{r}}} \times N_{r}^{1/4} + a_{4} \times \sqrt{\frac{\varepsilon_{0}(x)}{\varepsilon(r_{d},x)}} \times N_{r}^{1/2} \times 2 + a_{5} \times \left[\frac{\varepsilon_{0}(x)}{\varepsilon(r_{d},x)}\right]^{\frac{3}{2}} \times N_{r}^{\frac{1}{6}} \\ , & N_{r} \equiv \left(\frac{N^{*}}{N_{CDn}(r_{d},x)}\right) \end{split}$$

where  $a_1 = 3.8 \times 10^{-3} (eV)$  ,  $a_2 = 6.5 \times 10^{-4} (eV)$  ,  $a_3 = 2.8 \times 10^{-3} (eV)$  ,  $a_4 = 5.597 \times 10^{-3} (eV)$  and  $a_5 = 8.1 \times 10^{-4} (eV)$ , and in the p-type HD X(x)- alloy, as.

$$\begin{split} \Delta E_{gp}(N,r_{a},x) &\simeq a_{1} \times \frac{\epsilon_{0}(x)}{\epsilon(r_{a},x)} \times N_{r}^{1/3} + a_{2} \times \frac{\epsilon_{0}(x)}{\epsilon(r_{a},x)} \times N_{r}^{\frac{1}{3}} \times \left(2.503 \times [-E_{cp}(r_{sp}) \times r_{sp}]\right) + a_{3} \times \\ \left[\frac{\epsilon_{0}(x)}{\epsilon(r_{a},x)}\right]^{5/4} &\times \sqrt{\frac{m_{c}}{m_{r}}} \times N_{r}^{1/4} + 2a_{4} \times \sqrt{\frac{\epsilon_{0}(x)}{\epsilon(r_{a},x)}} \times N_{r}^{1/2} + a_{5} \times \left[\frac{\epsilon_{0}(x)}{\epsilon(r_{a},x)}\right]^{\frac{3}{2}} \times N_{r}^{\frac{1}{6}} \\ , & N_{r} \equiv \left(\frac{N^{*}}{N_{CDp}(r_{a},x)}\right) \end{split} , \label{eq:delta_eq}$$

where 
$$a_1=3.15\times 10^{-3} (eV)$$
 ,  $a_2=5.41\times 10^{-4} (eV)$  ,  $a_3=2.32\times 10^{-3} (eV)$  ,  $a_4=4.12\times 10^{-3} (eV)$  and  $a_5=9.8\times 10^{-5} (eV)$ .

One also remarks that, as  $N^* = 0$ , according to the MIT,  $\Delta E_{gn(gp)}(N, r_{d(a)}, x) = 0$ .

#### **OPTICAL BAND GAP**

Here, the optical band gap is found to be defined by:

$$\begin{split} E_{gn1(gp1)}\big(N,r_{d(a)},x,T\big) &\equiv E_{gni(gpi)}(r_{d(a)},x,T) - \Delta E_{gn(gp)}(N,r_{d(a)},x) + (-)E_{Fn(Fp)}\big(N,r_{d(a)},x,T\big) \\ , & (15) \end{split}$$

where  $E_{gin(gip)}$ ,  $[+E_{Fn}, -E_{Fp}] \ge 0$ , and  $\Delta E_{gn(gp)}$  are respectively determined in Equations [10, 12, 14n(p)], respectively. So, as noted above, at the MIT, Eq. (15) thus becomes:  $E_{gn1(gp1)}(r_{d(a)},x) = E_{gno(gpo)}(r_{d(a)},x)$ , according to:  $N = N_{CDn(NDp)}(r_{d(a)},x)$ .

#### **OPTICAL COEFFICIENTS**

The optical properties of any medium can be described by the complex refraction index  $\mathbb N$  and the complex dielectric function  $\epsilon$ ,  $\mathbb N \equiv n-i\kappa$  and  $\epsilon \equiv \epsilon_1-i\epsilon_2$ , where  $i^2=-1$  and  $\epsilon \equiv \mathbb N^2$ . Therefore, the real and imaginary parts of  $\epsilon$  denoted by  $\epsilon_1$  and  $\epsilon_2$  can thus be expressed in terms of the refraction index n and the extinction coefficient  $\kappa$  as:  $\epsilon_1 \equiv n^2 - \kappa^2$  and  $\epsilon_2 \equiv 2n\kappa$ . One notes that the optical absorption coefficient  $\alpha$  is related to  $\epsilon_2$ , n,  $\kappa$ , and the optical conductivity  $\sigma_0$ , by [2]

$$\alpha(E,N,r_{d(a)},x,T)\equiv\frac{\hbar q^2\times |v(E)|^2}{n(E)\times \epsilon_{free\,space}\times cE}\times J(E^*)=\frac{E\times \epsilon_2(E)}{\hbar cn(E)}\equiv\frac{2E\times K(E)}{\hbar c}\equiv\frac{4\pi\sigma_0(E)}{cn(E)\times \epsilon_{free\,space}},\;\epsilon_1\equiv n^2-\kappa^2\;\text{and}\;\;\epsilon_2\equiv 2n\kappa,$$
 (16)

where, since  $E \equiv \hbar \omega$  is the photon energy, the effective photon energy:  $E^* = E - E_{gn1(gp1)} \big( N, r_{d(a)}, x, T \big) \text{ is thus defined as the reduced photon energy.}$ 

Here, -q,  $\hbar$ , |v(E)|,  $\omega$ ,  $\epsilon_{free\,space}$ , c and  $J(E^*)$  respectively represent: the electron charge, Dirac's constant, matrix elements of the velocity operator between valence (conduction)-and-conduction (valence) bands in n(p)-type semiconductors, photon frequency, permittivity of free space, velocity of light, and joint density of states. It should be noted that, if the three functions such as:  $|v(E)|^2$ ,  $J(E^*)$  and n(E) are known, then the other optical dispersion functions as those given in Eq. (16) can thus be determined. Moreover, the normal-incidence reflectance, R(E), can be expressed in terms of  $\kappa(E)$  and n(E) as.

$$R(E, N, r_{d(a)}, x, T) = \frac{[n(E)-1]^2 + \kappa(E)^2}{[n(E)+1]^2 + \kappa(E)^2}$$
(17)

From Equations (16, 17), if the two optical functions,  $\varepsilon_1$  and  $\varepsilon_2$ , (or n and  $\kappa$ ), are both known, the other ones defined above can thus be determined, noting also that:  $E_{gn1(gp1)}(N, r_{d(a)}, x, T) = E_{gn1(gp1)}$ , for a presentation simplicity.

Then, one has

-at low values of  $E \gtrsim E_{gn1(gp1)}$ ,

$$J_{n(p)}\big(E,N,r_{d(a)},x,T\big) = \frac{1}{2\pi^2} \times \left(\frac{2m_r}{\hbar^2}\right)^{3/2} \times \frac{(E-E_{gn1(gp1)})^{a-(1/2)}}{E_{gn1(gpi)}^{a-1}} = \frac{1}{2\pi^2} \times \left(\frac{2m_r}{\hbar^2}\right)^{3/2} \times (E-E_{gn1(gp1)})^{1/2}, \quad \text{for} \quad a=1, \eqno(18)$$

and at large values of  $E > E_{gn1(gp1)}$ ,

$$\begin{split} J_{n(p)}\big(E,N,r_{d(a)},x,T\big) &= \frac{1}{2\pi^2} \times \left(\frac{2m_r}{\hbar^2}\right)^{3/2} \times \frac{(E-E_{gn1(gp1)})^{3-(1/2)}}{E_{gni(gpi)}^{a-1}} = \frac{1}{2\pi^2} \times \left(\frac{2m_r}{\hbar^2}\right)^{3/2} \times \frac{(E-E_{gn1(gp1)})^2}{E_{gni(gpi)}^{3/2}}, \quad \text{for} \\ a=&5/2. \ (19) \end{split}$$

Further, one notes that, as  $E \to \infty$ , Forouhi and Bloomer (FB) [4] claimed that  $\kappa(E \to \infty) \to a$  constant, while the  $\kappa(E)$  -expressions, proposed by Van Cong [2] quickly go to 0 as  $E^{-3}$ , and consequently, their numerical results of the optical functions such as:  $\sigma_0(E)$  and  $\alpha(E)$ , given in Eq. (16), both go to 0 as  $E^{-2}$ .

Now, an improved Forouhi-Bloomer parameterization model (FB-PM), used to determine the expressions of the optical coefficients in the degenerate  $n^+(p^+) - p(n) X(x)$ - crystalline alloy, is now proposed as follows. Then, if denoting the functions G(E) and F(E) and by:  $G(E) \equiv \sum_{i=1}^4 \frac{A_i}{E^2 - B_i E + C_i} \text{ and } F(E) \equiv \sum_{i=1}^4 \frac{A_i}{E^2 \times (1+10^{-4} \times \frac{E}{c}) - B_i E + C_i}, \text{ we propose.}$ 

$$\kappa \big(E,N,r_{d(a)},x,T\big) \,=\, G(E) \times E_{\mathrm{gni}(\mathrm{gpi})}^{3/2} \times \big(E^* \equiv \,E - E_{\mathrm{gn1}(\mathrm{gp1})}\big)^{1/2} \qquad \qquad , \qquad \qquad \text{for} \qquad \qquad \label{eq:kappa}$$

 $E_{gni(gpi)} \le E \le 2.3 \text{ eV},$ 

$$= F(E) \times \left(E^* \equiv E - E_{gn1(gp1)}\right)^2 \qquad , \qquad \text{for} \qquad E \ge 2.3 \text{ eV} \qquad , \tag{20}$$

being equal to 0 for  $E^* = 0$  (or for  $E = E_{gn1(gp1)}$ ), and also going to 0 as  $E^{-1}$  as  $E \to \infty$ , and further,

$$n(E, N, r_{d(a)}, x, T) = n_{\infty}(r_{d(a)}, x) + \sum_{i=1}^{4} \frac{x_i(E_{gn1(gp1)}) \times E + Y_i(E_{gn1(gp1)})}{E^2 - B_i E + C_i}$$
(21)

going to a constant as  $E \to \infty$ , since  $n(E \to \infty, r_{d(a)}, x) \to n_{\infty}(r_{d(a)}, x) = \sqrt{\epsilon(r_{d(a)}, x)} \times \frac{\omega_T}{\omega_L}$ ,  $\omega_T = 5.1 \times 10^{13} \ s^{-1}$  [5] and  $\omega_L = 8.9755 \times 10^{13} \ s^{-1}$ .

Here, the other parameters are determined by:

$$\begin{split} &X_i \big( E_{gn1(gp1)} \big) = \frac{A_i}{Q_i} \times \Big[ -\frac{B_i^2}{2} + E_{gn1(gp1)} B_i - E_{gn1(gp1)}^2 + C_i \Big], \\ &Y_i \big( E_{gn1(gp1)} \big) = \frac{A_i}{Q_i} \times \Big[ \frac{B_i \times (E_{gn1(gp1)}^2 + C_i)}{2} - 2 E_{gn1(gp1)} C_i \Big], \quad Q_i = \frac{\sqrt{4 C_i - B_i^2}}{2}, \text{ where, for } i = (1, \ 2, \ 3, \ and \ 4), \\ &A_i = 1.154 \times A_{i(FB)} = 4.7314 \times 10^{-4}, \quad 0.2314, \\ &0.1118 \text{ and } 0.0116, \\ &B_i \equiv B_{i(FB)} = 5.871, \\ &6.154, \\ &9.679 \text{ and } 13.232, \text{ and } C_i \equiv C_{i(FB)} = 8.619, \\ &9.784, \\ &23.803, \text{ and } 44.119. \end{split}$$

Then, as noted above, if the two optical functions,  $\mathbf{n}$  and  $\kappa$ , are both known, the other ones defined in Equations (16, 17) can also be determined.

#### NUMERICAL RESULTS

Now, some numerical results of those optical functions are investigated in the n(p)-type  $\mathbf{X}(\mathbf{x}) \equiv \mathbf{CdS}_{1-\mathbf{x}}\mathbf{Te}_{\mathbf{x}}$ - crystalline alloy, as follows.

#### A. Metal-insulator transition (MIT)-case

As discussed above, the physical conditions used for the MIT are found to be given by: T=0K,  $N^*=0$  or  $N=N_{CDn(CDp)}$ , giving rise to:

$$E_{gn1(gp1)}\big(N^* = 0, r_{d(a)}, x, T = 0\big) = E_{gn1(gp1)}\big(r_{d(a)}, x\big) = E_{gno(gpo)}\big(r_{d(a)}, x\big).$$

Then, in this MIT-case, if  $E = E_{gn1(gp1)}(r_{d(a)},x) = E_{gno(gpo)}(r_{d(a)},x)$ , which can be defined as the **critical photon energy**:  $E \equiv E_{CPE}(r_{d(a)},x)$ , one obtains:  $\kappa_{MIT}(r_{d(a)},x) = 0$  from Eq. (20), and from Eq. (16):  $\epsilon_{2(MIT)}(r_{d(a)},x) = 0$ ,  $\sigma_{O(MIT)}(r_{d(a)},x) = 0$  and  $\alpha_{MIT}(r_{d(a)},x) = 0$ , and the other functions such as:  $n_{MIT}(r_{d(a)},x)$  from Eq. (21), and  $\epsilon_{1(MIT)}(r_{d(a)},x)$  and  $R_{MIT}(r_{d(a)},x)$  from Eq. (16) decrease with increasing  $r_{d(a)}$  and  $E_{CPE}$ , as those investigated in Table 1 in Appendix 1.

#### B. Optical coefficients, obtained as $E \rightarrow \infty$

T. the of In choice the real refraction index:  $n(E \to \infty, r_{d(a)}, x, T) = n_{\infty}(r_{d(a)}, x) = \sqrt{\epsilon(r_{d(a)}, x)} \times \frac{\omega_T}{\omega_T}, \quad \omega_T = 5.1 \times 10^{13} \, s^{-1}$  [5]  $\omega_L = 8.9755 \times 10^{13} \text{ s}^{-1}$ , was obtained from the Lyddane-Sachs-Teller relation<sup>[5]</sup>, from which T(L) represent the transverse (longitudinal) optical phonon modes. Then, from Equations (16, 17, 20), from such the asymptotic behavior ( $E \rightarrow \infty$ ), we obtain:  $\kappa_{\infty}(\mathbf{r}_{\mathsf{d}(\mathsf{a})}, \chi) \to 0 \text{ and } \varepsilon_{2,\infty}(\mathbf{r}_{\mathsf{d}(\mathsf{a})}, \chi) \to 0 \,, \text{ as } E^{-1} \,, \text{ so that } \varepsilon_{1,\infty}(\mathbf{r}_{\mathsf{d}(\mathsf{a})}, \chi) \,, \, \sigma_{0,\infty}(\mathbf{r}_{\mathsf{d}(\mathsf{a})}, \chi) \,,$  $\alpha_{\infty}(\mathbf{r}_{d(a)},\mathbf{x})$  and  $R_{\infty}(\mathbf{r}_{d(a)},\mathbf{x})$  go to their appropriate limiting constants, as those investigated in Table 2 in Appendix 1.

### C. Variations of some optical coefficients, obtained in P(Ga)-X(x)-system, as functions of E

In the P(Ga)-X(x)-system, at T=0K and N =  $N_{CDn(CDp)}(r_{P(Ga)},x)$ , our numerical results of n,  $\kappa$ ,  $\epsilon_1$  and  $\epsilon_2$  are obtained from Equations (21, 20, 16), respectively, and expressed as functions of E [ $\geq E_{CPE}(r_{P(Ga)},x)$ ] and for given x, as those reported in Tables 3n and 3p in Appendix 1.

#### D. Variations of various optical coefficients, as functions of N

In the X(x)-system, at E=3.2 eV and T=20 K, for given  $r_{d(a)}$  and x, and from Equations (12, 15, 21, 20, 16), respectively, we can determine the variations of  $\eta_{n(p)}(\gg 1$ , degenerate case),  $E_{gn1(gp1)}$ , n,  $\kappa$ ,  $\varepsilon_1$  and  $\varepsilon_2$ , obtained as functions of N, being represented by the arrows:  $\nearrow$  and  $\searrow$ , as those tabulated in Tables 4n and 4p in Appendix 1.

#### E. Variations of various optical coefficients as functions of T

In the X(x)-system, at E=3.2 eV and N =  $10^{20}$  cm<sup>-3</sup>, for given  $r_{d(a)}$  and x, and from Equations (12, 15, 21, 20, 16), respectively, we can determine the variations of  $\eta_{n(p)}(\gg 1$ , degenerate case),  $E_{gn1(gp1)}$ , n,  $\kappa$ ,  $\varepsilon_1$  and  $\varepsilon_2$ , obtained as functions of T, being represented by the arrows:  $\nearrow$  and  $\searrow$ , as those tabulated in Tables 5n and 5p in Appendix 1.

#### **CONCLUDING REMARKS**

In the n(p)-type  $\mathbf{X}(\mathbf{x}) \equiv \mathbf{CdS_{1-x}Te_x}$ - crystalline alloy, by basing on our two recent works<sup>[1,2]</sup>, for a given x, and with an increasing  $\mathbf{r_{d(a)}}$ , the optical coefficients have been determined, as

functions of the photon energy E, total impurity density N, the donor (acceptor) radius  $r_{d(a)}$ , concentration x, and temperature T.

Those results have been affected by (i) the important new  $\varepsilon(\mathbf{r}_{d(a)},\mathbf{x})$ -law, developed in Equations (8a, 8b), stating that, for a given x, due to the impurity-size effect,  $\varepsilon$  decreases ( $\Sigma$ ) with an increasing ( $\nearrow$ )  $\mathbf{r}_{d(a)}$ , and then by (ii) the generalized Mott critical d(a)-density defined in the metal-insulator transition (MIT),  $\mathbf{N}_{\text{CDn}(NDp)}(\mathbf{r}_{d(a)},\mathbf{x})$ , as observed in Equations (8c, 9a).

Further, we also showed that  $N_{CDn(NDp)}$  is just the density of carriers localized in exponential band tails, with a precision of the order of  $2.84 \times 10^{-7}$ , as that given in Table 4 of Ref.<sup>[1]</sup>, according to a definition of the effective density of electrons (holes) given in parabolic conduction (valence) bands by:  $N^*(N, r_{d(a)}, x) \equiv N - N_{CDn(NDp)}(r_{d(a)}, x)$ , as defined in Eq. (9d).

In summary, due to the new  $\varepsilon(r_{d(a)},x)$ -law and to the effective density of electrons (holes) given in parabolic conduction (valence) bands  $N^*(N,r_{d(a)},x)$ , for a given x, and with an increasing  $r_{d(a)}$ , the numerical results of all the optical coefficients, obtained in appropriated physical conditions (E, N, T), and calculated by using Equations (15, 16, 20, 21), are investigated in Tables 1, 2, 3n, 3p, 4n, 4p, 5n, and 5p in Appendix 1.

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#### **APPENDIX 1**

**Table 1.** In the MIT-case, T=0K,  $N=N_{CDn(p)}(r_{d(a)},x)$ , and the critical photon energy  $E_{CPE}=E=E_{gno(gpo)}(r_{d(a)},x)$ , if  $E=E_{gn1(gp1)}(r_{d(a)},x)=E_{CPE}(r_{d(a)},x)$ , the numerical results of optical functions such as :  $n_{MIT}(r_{d(a)},x)$ , obtained from Eq. (21), and those of other ones:  $\epsilon_{1(MIT)}(r_{d(a)},x)$  and  $R_{MIT}(r_{d(a)},x)$ , from Eq. (16), decrease ( $\searrow$ ) with increasing ( $\nearrow$ )  $r_{d(a)}$  and  $E_{CPE}$ .

| Donor                              |   | S       | Se        | Т      | e     | Sn    |      |   |
|------------------------------------|---|---------|-----------|--------|-------|-------|------|---|
| r <sub>d</sub> (nm) [4]            | , | 0.104   | 0.114     | 0.1    | .32   | 0.140 |      |   |
| At <b>x=0</b> ,                    |   |         |           |        |       |       | <br> |   |
| $E_{\mathtt{CPE}}$ in meV          | 7 | 2580    | 2583      | 2605   | 5 20  | 522   |      |   |
| $n_{MIT}$                          | 7 | 2.401   | 2.364     | 2.16   | 4 2.  | 057   |      |   |
| $\varepsilon_{1(MIT)}$             | 7 | 5.766   | 5.589     | 4.683  | 3 4.2 | 231   |      |   |
| $R_{MIT}$                          | > | 0.170   | 0.164     | 0.135  | 5 0.  | 119   |      |   |
| At <b>x=0.5</b> ,                  |   |         |           |        |       |       |      |   |
| $E_{\mathtt{CPE}}$ in $\text{meV}$ | 7 | 2100    | 2102      | 2116   | 2127  |       |      |   |
| $n_{MIT}$                          | 7 | 2.761   | 2.724     | 2.521  | 2.415 |       |      |   |
| $\varepsilon_{1(MIT)}$             | 7 | 7.625   | 7.418     | 6.358  | 5.832 |       |      |   |
| $R_{MIT}$                          | > | 0.219   | 0.214     | 0.187  | 0.172 |       |      |   |
| At <b>x=1</b> ,                    |   |         |           |        |       |       |      |   |
| $E_{\mathtt{CPE}}$ in meV          | 7 | 1620    | 1621      | 1629   | 1636  | ;     |      |   |
| $\mathbf{n}_{\mathbf{MIT}}$        | 7 | 3.119   | 3.081     | 2.876  | 2.769 | )     |      |   |
| $\varepsilon_{1(MIT)}$             | 7 | 9.730   | 9.492     | 8.272  | 7.669 |       |      |   |
| $R_{MIT}$                          | 7 | 0.265   | 0.260     | 0.234  | 0.220 |       |      |   |
| Acceptor                           |   | Ga      | Mg        | 9      | In    | Cd    |      | _ |
| r <sub>a</sub> (nm)                | , | 0.12    | 26 0.140  | 0.1    | 144   | 0.148 |      |   |
| At <b>x=0</b> ,                    |   |         |           |        |       |       | <br> |   |
| $E_{CPE}$ in meV                   | 7 | 2555    | 2576      | 2579   | 25    | 80    |      |   |
| n <sub>MIT</sub>                   | 7 | 2.506   | 2.414     | 2.405  | 2.4   | 101   |      |   |
| $\varepsilon_{1(MIT)}$             | > | 6.281 5 | .830 5.78 | 82 5.7 | 66    |       |      |   |

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| $R_{MIT}$                          | 7   | 0.184  | 0.172 | 0.170 | 0.1697 |  |
|------------------------------------|-----|--------|-------|-------|--------|--|
| At <b>x=0.5</b> ,                  |     |        |       |       |        |  |
| E <sub>CPE</sub> in me             | V > | 2078   | 2097  | 2099  | 2100   |  |
| n <sub>MIT</sub>                   | >   | 2.867  | 2.775 | 2.765 | 2.761  |  |
| $arepsilon_{1(MIT)}$               | >   | 8.223  | 7.699 | 7.644 | 7.625  |  |
| $R_{MIT}$                          | >   | 0.233  | 0.221 | 0.220 | 0.219  |  |
| At <b>x=1</b> ,                    |     |        |       |       |        |  |
| $\mathbf{E}_{\mathtt{CPE}}$ in meV | 7   | 1601   | 1617  | 1619  | 1620   |  |
| $n_{MIT}$                          | >   | 3.227  | 3.133 | 3.123 | 3.119  |  |
| $\varepsilon_{1(MIT)}$             | 7   | 10.414 | 9.815 | 9.752 | 9.730  |  |
| $R_{MIT}$                          | 7   | 0.277  | 0.266 | 0.265 | 0.2647 |  |
|                                    |     |        |       |       |        |  |

**Table 2.** Here, as  $E \to \infty$ , the numerical results of  $n_{\infty}(\mathbf{r}_{\mathsf{d}(\mathsf{a})},x)$ ,  $\varepsilon_{1,\infty}(\mathbf{r}_{\mathsf{d}(\mathsf{a})},x)$ ,  $\sigma_{0,\infty}(\mathbf{r}_{\mathsf{d}(\mathsf{a})},x)$ ,  $\alpha_{\infty}(\mathbf{r}_{\mathsf{d}(\mathsf{a})},x)$  and  $R_{\infty}(\mathbf{r}_{\mathsf{d}(\mathsf{a})},x)$  go to their appropriate limiting constants.

| Donor  | S      | Se     | Te     | Sn      |
|--|--------|--------|--------|---------|
| r <sub>d</sub> (nm) [4]                                | 0.104  | 0.114  | 0.132  | 2 0.140 |
|  |        |        |        |         |
| At <b>x=0</b> ,  |        |        |        |         |
| $n_{\infty}$   | 1.7046 | 1.6693 | 1.4827 | 1.3867  |
| $\varepsilon_{1,\infty}$                               | 2.906  | 2.7867 | 2.1983 | 1.9229  |
| $\sigma_{0,\infty}$ in $\frac{10^5}{\Omega \times cm}$ | 7.7784 | 7.6173 | 6.7656 | 6.3275  |
| $\alpha_{\infty}$ in $(10^9 \times cm^{-1})$           | 2.160  | 2.160  | 2.160  | 2.160   |
| R <sub>∞</sub> ∨                                       | 0.068  | 0.063  | 0.038  | 0.026   |
|  |        |        |        |         |
| At $x=0.5$ ,   |        |        |        |         |
| $n_{\infty}$   | 1.765  | 1.729  | 1.536  | 1.436   |
| $\varepsilon_{1,\infty}$                               | 3.117  | 2.989  | 2.358  | 2.063   |
| $\sigma_{0,\infty}$ in $\frac{10^5}{\Omega \times cm}$ | 8.056  | 7.889  | 7.007  | 6.554   |
| $\alpha_{\infty}$ in $(10^9 \times cm^{-1})$           | 2.160  | 2.160  | 2.160  | 2.160   |
| R <sub>∞</sub> ∨                                       | 0.077  | 0.071  | 0.045  | 0.032   |

| At <b>x=1</b> ,   |            |          |        |       |
|---|------------|----------|--------|-------|
| $n_{\infty}$ $\searrow$   | 1.824      | 1.787    | 1.587  | 1.484 |
| $\varepsilon_{1,\infty}$  | 3.329      | 3.192    | 2.518  | 2.203 |
| $\sigma_{0,\infty}$ in $\frac{10^5}{\Omega \times cm}$            | 8.320      | 8.153    | 7.241  | 6.772 |
| $\alpha_{\infty}$ in $(10^9 \times cm^{-1})$                      | 2.160      | 2.160    | 2.160  | 2.160 |
| $R_{\infty}$  | 0.085      | 0.080    | 0.051  | 0.038 |
|   |            |          |        |       |
| Acceptor  | Ga         | Mg       | In     | Cd    |
| $r_{\rm a}  ({\rm nm})$   | 0.126      | 0.140    | 0.144  | 0.148 |
|   |            |          |        |       |
| At <b>x=0</b> ,   |            |          |        |       |
|   | 1.794 1.7  |          |        |       |
|   | 3.218 2.94 | 14 2.915 | 2.906  |       |
| $\sigma_{0,\infty}$ in $\frac{10^5}{\Omega \times cm}$            | 8.186 7.8  | 29 7.791 | 7.778  |       |
| $\alpha_{\infty}$ in $(10^9 \times cm^{-1})$                      | 2.160 2.16 | 50 2.160 | 2.160  |       |
| R <sub>∞</sub> ∨  | 0.081 0.00 | 59 0.068 | 0.0679 |       |
| At <b>x=0.5</b> ,   |            |          |        |       |
| $n_{\infty}$  | 1.858      | 1.777    | 1.768  | 1.766 |
| $\varepsilon_{1,\infty}$  | 3.453      | 3.158    | 3.127  | 3.117 |
| $\sigma_{0,\infty}$ in $\frac{10^5}{\Omega \times cm}$ $\searrow$ | 8.479      | 8.109    | 8.069  | 8.056 |
| $\alpha_{\infty}$ in $(10^9 \times cm^{-1})$                      | 2.160      | 2.160    | 2.160  | 2.160 |
| R <sub>∞</sub> >  | 0.090      | 0.078    | 0.077  | 0.120 |
|   |            |          |        |       |
| At $\mathbf{x}=1$ , $n_{\infty}$                                  | 1.920      | 1.836    | 1.827  | 1.824 |
| ε <sub>1,∞</sub> Σ  | 3.687      |          | 3.340  | 3.329 |
| $\sigma_{0,\infty}$ in $\frac{10^5}{0.000}$                       |            | 8.379    |        | 8.325 |
| 11×cm   |            |          |        |       |
| $\alpha_{\infty}$ in $(10^9 \times cm^{-1})$                      |            |          | 2.160  | 2.160 |
| R <sub>∞</sub> ∨  | 0.099      | 0.087    | 0.086  | 0.085 |
|   |            |          |        |       |

**Table 3n.** In the P-X(x)-system, and at T=0K and N = N<sub>CDn</sub>(r<sub>p</sub>,x), according to the MIT, our numerical results of n,  $\kappa$ ,  $\epsilon_1$  and  $\epsilon_2$  are obtained from Equations (21, 20, 16), respectively, and expressed as functions of  $E [\geq E_{CPE}(r_p,x)]$  and x, noting that (i)  $\kappa = 0$  and  $\epsilon_2 = 0$  at  $E = E_{CPE}(r_p,x)$ , and  $\kappa \to 0$  and  $\epsilon_2 \to 0$  as  $E \to \infty$ .

| E in eV            | n      | κ     | $arepsilon_1$ | $arepsilon_2$ |
|--------------------|--------|-------|---------------|---------------|
| At x=0,            |        |       |               |               |
| $E_{CPE}=2.5810$   | 2.3878 | 0     | 5.7015        | 0             |
| 3                  | 2.662  | 0.144 | 7.064         | 0.768         |
| 3.5                | 2.746  | 0.440 | 7.348         | 2.415         |
| 4                  | 2.892  | 0.609 | 7.992         | 3.525         |
| 4.5                | 3.123  | 1.198 | 8.315         | 7.484         |
| 5                  | 3.357  | 1.956 | 1.730         | 9.221         |
| 5.5                | 1.671  | 1.541 | 0.418         | 5.151         |
| 6                  | 1.666  | 1.246 | 1.222         | 4.151         |
|                    |        |       |               |               |
| 1022               | 1.6917 | 0     | 2.86          | 20 0          |
| At x=0.5,          |        |       |               |               |
| $E_{CPE}=2.1006$   | 2.7476 | 0     | 7.5493        | 0             |
| 3                  | 3.367  | 0.664 | 10.898        | 4.474         |
| 3.5                | 3.123  | 1.020 | 8.712         | 6.368         |
| 4                  | 3.250  | 1.092 | 9.372         | 7.098         |
| 4.5                | 3.522  | 1.873 | 8.897         | 13.197        |
| 5                  | 2.345  | 2.810 | -2.399        | 13.177        |
| 5.5                | 1.427  | 2.090 | -2.331        | 5.966         |
| 6                  | 1.467  | 1.621 | -0.475        | 4.756         |
|                    |        |       |               |               |
| 1022               | 1.7522 | 0     | 3.070         | 0             |
| At x=1,            |        |       |               |               |
| $E_{CPE} = 1.6204$ | 3.1053 | 0     | 9.6431        | 0             |
| 2                  | 3.396  | 0.217 | 11.487        | 1.477         |

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|                  |        |           |                    |                |              |
| 2.5              | 4.015  | 0.293     | 16.038             | 2.352          |              |
| 3                | 4.105  | 1.563     | 14.405             | 12.836         |              |
| 3.5              | 3.380  | 1.840     | 8.042              | 12.437         |              |
| 4                | 3.519  | 1.714     | 9.449              | 12.065         |              |
| 4.5              | 3.862  | 2.698     | 7.633              | 20.842         |              |
| 5                | 2.209  | 3.818     | -9.698             | 16.868         |              |
| 5.5              | 1.044  | 2.722     | -6.321             | 5.684          |              |
| 6                | 1.154  | 2.045     | -2.850             | 4.718          |              |
|                  |        |           |                    |                |              |
| 10 <sup>22</sup> | 1.8107 | 0         | 3.2786             | 0              |              |
| E in eV          | n      | κ         | $\varepsilon_1$    | $arepsilon_2$  |              |

**Table 3p.** In the Ga-X(x)-system, and at T=0K and N = N<sub>CDp</sub>(r<sub>Ga</sub>,x), according to the MIT, our numerical results of n,  $\kappa$ ,  $\epsilon_1$  and  $\epsilon_2$  are obtained from Equations (21, 20, 16), respectively, and expressed as functions of  $E [\geq E_{CPE}(r_{Ga},x)]$  and x, noting that (i)  $\kappa = 0$  and  $\epsilon_2 = 0$  at  $E = E_{CPE}(r_{Ga},x)$ , and  $\kappa \to 0$  and  $\epsilon_2 \to 0$  as  $E \to \infty$ .

| E in eV            | n      | κ     | $arepsilon_1$ | $arepsilon_2$ |
|--------------------|--------|-------|---------------|---------------|
| At x=0,            |        |       |               |               |
| $E_{CPE} = 2.5551$ | 2.5062 | 0     | 6.2810        | 0             |
| 3                  | 2.798  | 0.162 | 7.802         | 0.910         |
| 3.5                | 2.868  | 0.465 | 8.012         | 2.667         |
| 4                  | 3.012  | 0.632 | 8.676         | 3.807         |
| 4.5                | 3.245  | 1.231 | 9.013         | 7.987         |
| 5                  | 2.458  | 1.998 | 2.052         | 9.824         |
| 5.5                | 1.761  | 1.568 | 0.639         | 5.523         |
| 6                  | 1.757  | 1.265 | 1.486         | 4.445         |
|                    |        |       |               |               |
| 10 <sup>22</sup>   | 1.7940 | 0     | 3.2185        | 0             |

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|----------------------|------|---------|--------|-------------|-----|------------------|---|
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| At $x=0.5$ ,              |        |       |               |               |
|---------------------------|--------|-------|---------------|---------------|
| $E_{CPE} = 2.0781$        | 2.8675 | 0     | 8.2229        | 0             |
| 2.5                       | 3.214  | 0.067 | 10.323        | 0.433         |
| 3                         | 3.504  | 0.698 | 11.794        | 4.893         |
| 3.5                       | 3.241  | 1.053 | 9.394         | 6.823         |
| 4                         | 3.368  | 1.118 | 10.094        | 7.531         |
| 4.5                       | 3.643  | 1.909 | 9.626         | 13.905        |
| 5                         | 2.444  | 2.854 | -2.170        | 13.950        |
| 5.5                       | 1.515  | 2.118 | -2.188        | 6.419         |
| 6                         | 1.558  | 1.640 | -0.261        | 5.109         |
|                           |        |       |               |               |
| 1022                      | 1.8581 | 0     | 3.4527        | 0             |
|                           |        |       |               |               |
| At x=1,                   |        |       |               |               |
| $E_{\text{CPE}} = 1.6006$ | 3.2271 | 0     | 10.4143       | 0             |
| 2                         | 3.536  | 0.219 | 12.456        | 1.548         |
| 2.5                       | 4.166  | 0.306 | 17.262        | 2.552         |
| 3                         | 4.243  | 1.609 | 15.415        | 13.651        |
| 3.5                       | 3.495  | 1.878 | 8.689         | 13.132        |
| 4                         | 3.636  | 1.743 | 10.182        | 12.671        |
| 4.5                       | 3.982  | 2.735 | 8.371         | 21.785        |
| 5                         | 2.308  | 3.863 | -9.595        | 17.830        |
| 5.5                       | 1.132  | 2.750 | -6.281        | 6.228         |
| 6                         | 1.245  | 2.063 | -2.706        | 5.140         |
|                           |        |       |               |               |
| 1022                      | 1.9201 | 0     | 3.6870        | 0             |
| E in eV                   | n      | κ     | $arepsilon_1$ | $arepsilon_2$ |

**Table 4n.** In the X(x)-system, at E=3.2 eV and T=20 K, for given  $\mathbf{r_d}$  and x, and from Equations (12, 15, 21, 20, 16), respectively, we can determine the variations of  $\eta_n(\gg 1, \text{degenerate case})$ ,  $E_{gn1}$ , n,  $\kappa$ ,  $\varepsilon_1$  and  $\varepsilon_2$ , obtained as functions of N, being represented by the arrows:  $\nearrow$  and  $\searrow$ , noting that both  $\eta_n$  and  $E_{gn1}$  increase with increasing N.

| $N (10^{18} \text{ cm}^{-3})$ $\nearrow$ 15 | 26        | 60                | 100   |  |
|---|-----------|-------------------|-------|--|
|   | x=0       |                   |       |  |
| For $\mathbf{r_d} = \mathbf{r_{Se}}$ ,      |           |                   |       |  |
| $\eta_n \gg 1$ $\nearrow$ 226               | 334       | 594               | 840   |  |
| E <sub>gn1</sub> in eV 		 ∠ 2.909           | 3.078     | 3.492             | 3.887 |  |
| n > 2.335                                   | 2.130     | 1.608             | 1.080 |  |
| κ 0.063                                     | 0.011 7   | 0.063             | 0.350 |  |
| ε <sub>1</sub> 5.448                        | 4.537     | 2.582             | 1.045 |  |
| $\varepsilon_2$ 0.294                       | √ 0.047 ≯ | 0.203             | 0.756 |  |
| For $\mathbf{r_d} = \mathbf{r_{Te}}$ ,      |           |                   |       |  |
| $\eta_n \gg 1$ $\nearrow$ 211               | 322       | 585               | 833   |  |
| E <sub>gn1</sub> in eV                      | 3.090     | 3.513             | 3.915 |  |
| n > 2.142                                   | 1.929     | 1.393             | 0.855 |  |
| κ 0.061 ν                                   | 0.009 7   | 0.073             | 0.379 |  |
| ε <sub>1</sub> 4.585                        | 3.722     | 1.936             | 0.587 |  |
| $\varepsilon_2$ 0.260 $\searrow$            | 0.035 7   | 0.203             | 0.648 |  |
| For $\mathbf{r_d} = \mathbf{r_{Sn}}$ ,      |           |                   |       |  |
| $\eta_n \gg 1$ $\nearrow$ 197               | 310       | 577               | 825   |  |
| E <sub>gn1</sub> in eV   ≥ 2.911            | 3.092     | 3.523             | 3.929 |  |
| n > 2.049                                   | 1.830     | 1.285             | 0.740 |  |
| κ 0.062                                     | 0.0086    | <b>&gt;</b> 0.077 | 0.394 |  |
| ε <sub>1</sub> \ \ 4.197                    | 3.349     | 1.644             | 0.392 |  |
| $\varepsilon_2$ 0.254                       | 0.031 🗡   | 0.199             | 0.583 |  |
|   | x=0.5     |                   |       |  |

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| For $\mathbf{r_d} = \mathbf{r_{Se}}$ , |   |        |        |        |               |  |
|--|---|--------|--------|--------|---------------|--|
| $\eta_n\gg 1$                          | 7 | 128    | 187    | 328    | 462           |  |
| $E_{gn1}$ in eV                        | 7 | 2.224  | 2.298  | 2.485  | 2.669         |  |
| n                                      | 7 | 3.168  | 3.089  | 2.883  | 2.675         |  |
| κ                                      | > | 0.705  | 0.603  | 0.379  | 0.209         |  |
| $\varepsilon_1$                        | 7 | 9.539  | 9.178  | 8.171  | 7.113         |  |
| $arepsilon_2$                          | 7 | 4.469  | 3.725  | 2.184  | 1.117         |  |
| For $\mathbf{r_d} = \mathbf{r_{Te}}$ , |   |        |        |        |               |  |
| $\eta_n\gg 1$                          | 7 | 126    | 185    | 326    | 461           |  |
| $E_{gn1}$ in eV                        | 7 | 2.247  | 2.326  | 2.523  | 2.715         |  |
| n                                      | 7 | 2.950  | 2.865  | 2.648  | 2.428         |  |
| κ                                      | > | 0.672  | 0.566  | 0.340  | 0.174         |  |
| $arepsilon_1$                          | 7 | 8.251  | 7.891  | 6.895  | 5.867         |  |
| $arepsilon_2$                          | > | 3.968  | 3.246  | 1.798  | 0.845         |  |
| For $\mathbf{r_d} = \mathbf{r_{Sn}}$ , |   |        |        |        |               |  |
| $\eta_n\gg 1$                          | 7 | 123    | 183    | 325    | 459           |  |
| $E_{gn1}$ in eV                        | 7 | 2.261  | 2.342  | 2.544  | 2.704         |  |
| n                                      | 7 | 2.836  | 2.749  | 2.525  | 2.300         |  |
| κ                                      | > | 0.654  | 0.546  | 0.319  | 0.156         |  |
| $\varepsilon_1$                        | 7 | 7.618  | 7.258  | 6.273  | 5.266         |  |
| $arepsilon_2$                          | 7 | 3.709  | 3.002  | 1.611  | 0.720         |  |
|  |   |        | x=1    |        |               |  |
| For $\mathbf{r_d} = \mathbf{r_{Se}}$ , |   |        |        |        |               |  |
| $\eta_n\gg 1$                          | 7 | 93     | 135    | 236    | 332           |  |
| $E_{\tt gn1}$ in eV                    | 7 | 1.593  | 1.612  | 1.673  | 1.744         |  |
| n                                      | 7 | 3.863  | 3.846  | 3.787  | 3.718         |  |
| κ                                      | > | 1.913  | 1.870  | 1.728  | 1.572         |  |
| $arepsilon_1$                          | 7 | 11.266 | 11.295 | 11.355 | <b>11.354</b> |  |

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| $arepsilon_2$                          | 7   | 14.785 | 14.383 | 13.092  | 11.693  |
|--|-----|--------|--------|---------|---------|
|  |     |        |        |         |         |
| For $\mathbf{r_d} = \mathbf{r_{Te}}$ , |     |        |        |         |         |
| $\eta_n\gg 1$                          | 7   | 93     | 134.6  | 235     | 5.6 331 |
| $E_{\tt gn1}$ in eV                    | 7   | 1.629  | 1.656  | 1.738   | 1.826   |
| n                                      | 7   | 3.630  | 3.603  | 3.524   | 3.437   |
| κ                                      | >   | 1.830  | 1.766  | 1.584   | 1.399   |
| $\varepsilon_1$                        | 7   | 9.828  | 9.865  | 9.909 💃 | 9.856   |
| $arepsilon_2$                          | 7   | 13.286 | 12.728 | 11.168  | 9.621   |
|  |     |        |        |         |         |
| For $\mathbf{r_d} = \mathbf{r_{Sn}}$ , |     |        |        |         |         |
| $\eta_n\gg 1$                          | 7   | 92.5   | 134.2  | 235.4   | 331.3   |
| $E_{\text{gn1}}$ in eV                 | 7   | 1.647  | 1.679  | 1.770   | 1.866   |
| n                                      | 7   | 3.509  | 3.478  | 3.389   | 3.294   |
| κ                                      | 7   | 1.787  | 1.714  | 1.515   | 1.318   |
| $\varepsilon_1$                        | 7   | 9.122  | 9.162  | 9.194   | 9.113   |
| $arepsilon_2$                          | 7   | 12.541 | 11.923 | 10.271  | 8.686   |
|  |     |        |        |         |         |
| $N (10^{18} \text{ cm}^{-3})$          | ) 7 | 15     | 26     | 60      | 100     |

**Table 4p.** In the X(x)-system, at E=3.2 eV and T=20 K, for given  $\mathbf{r_d}$  and x, and from Equations (12, 15, 21, 20, 16), respectively, we can determine the variations of  $\eta_p(\gg 1, \text{degenerate case})$ ,  $E_{gp1}$ , n,  $\kappa$ ,  $\varepsilon_1$  and  $\varepsilon_2$ , obtained as functions of N, being represented by the arrows:  $\nearrow$  and  $\searrow$ , noting that both  $\eta_p$  and  $E_{gp1}$  increase with increasing N.

| N (10 <sup>18</sup> cm <sup>-3</sup>   | ) / | 75    | 80    | 85    | 100   |  |
|--|-----|-------|-------|-------|-------|--|
|  |     |       | x=0   |       |       |  |
|  |     |       |       |       |       |  |
| For $\mathbf{r_a} = \mathbf{r_{Ga}}$ , | ı   |       |       |       |       |  |
| $\eta_p\gg 1$                          | 7   | 115   | 133   | 150   | 196   |  |
| $E_{\text{gp1}}$ in eV                 | 7   | 1.788 | 1.818 | 1.847 | 1.924 |  |
| n                                      | 7   | 3.681 | 3.652 | 3.623 | 3.546 |  |

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|--|---|--------|-----------------|----------------|--------------|----------------------------|
|  |   |        |                 |                |              |                            |
| κ                                      | 7 | 1.477  | 1.415           | 1.357          | 1.207        |                            |
| $arepsilon_1$                          | 7 | 11.373 | 11.334          | 11.288         | 11.117       | 7                          |
| $\varepsilon_2$                        | 7 | 10.879 | 10.333          | 9.837          | 8.560        |                            |
|  |   |        |                 |                |              |                            |
| For $\mathbf{r_a} = \mathbf{r_{In}}$ , |   |        |                 |                |              |                            |
| $\eta_p\gg 1$                          | 7 | 22     | 55              | 79             | 138          | 3                          |
| E <sub>gp1</sub> in eV                 | 7 | 1.652  | 1.700           | 6 1.74         | 1.84         | 14                         |
| n                                      | 7 | 3.728  |                 | 3.676          | 3.636        | 3.539                      |
| κ                                      | 7 | 1.776  |                 | 1.654          | 1.565        | 1.362                      |
| $arepsilon_1$                          | 7 | 10.744 |                 | 10.774         | 10.769       | 10.671                     |
| $\varepsilon_2$                        | 7 | 13.243 |                 | 12.163         | 11.379       | 9.642                      |
|  |   |        |                 |                |              |                            |
| For $\mathbf{r_a} = \mathbf{r_{cd}}$ , |   |        |                 |                |              |                            |
| ·P                                     |   |        | 51              | 76             | 135          |                            |
| E <sub>gp1</sub> in eV                 | 7 | 1.642  | 1.700           | 1.742          | 1.841        |                            |
| n                                      | 7 | 3.735  | 3.679           | 3.638          | 3.540        |                            |
| κ                                      | 7 | 1.799  | 1.667           | 1.575          | 1.369        |                            |
| $arepsilon_1$                          |   | 10.712 | <b>№</b> 10.752 | <b>1</b> 0.751 | 10.657       |                            |
| $\varepsilon_2$                        | 7 | 13.443 | 12.269          | 11.460         | 9.693        |                            |
|  |   |        |                 |                |              |                            |
|  |   |        | x=0.5           |                |              |                            |
|  |   |        |                 |                |              |                            |
| For $\mathbf{r_a} = \mathbf{r_{Ga}}$ , |   | 20.4   | 227             | 240            | 200          |                            |
| $\eta_p\gg 1$                          | 7 | 204    | 227             | 249            | 308          |                            |
| E <sub>gp1</sub> in eV                 | 7 | 2.417  | 2.456           | 2.492          | 2.593        |                            |
| n                                      | 7 | 3.088  | 3.045           | 3.005          | 2.891        |                            |
| κ                                      | 7 | 0.454  | 0.411           | 0.371          | 0.273        |                            |
| $arepsilon_1$                          | 7 | 9.329  | 9.106           | 8.891          | 8.282        |                            |
| $\varepsilon_2$                        | 7 | 2.803  | 2.501           | 2.232          | 1.577        |                            |
|  |   |        |                 |                |              |                            |
| For $\mathbf{r_a} = \mathbf{r_{In}}$ , |   | 100    | 4.70            | <b></b> .      | • • •        |                            |
| $\eta_p\gg 1$                          | 7 | 122    | 150             | 176            | 245          |                            |
| E <sub>gp1</sub> in eV                 | 7 | 2.300  | 2.348           | 2.392          | 2.508        |                            |

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|  |   |        |         |              |             |                         |
| n                                      | > | 3.127  | 3.074   | 3.026        | 2.897       |                         |
| κ                                      | 7 | 0.601  | 0.538   | 0.484        | 0.355       |                         |
| $arepsilon_1$                          | > | 9.415  | 9.163   | 8.924        | 8.268       |                         |
| $\varepsilon_2$                        | > | 3.757  | 3.310   | 2.931        | 2.056       |                         |
|  |   |        |         |              |             |                         |
| For $\mathbf{r_a} = \mathbf{r_{Cd}}$ , |   |        |         |              |             |                         |
| $\eta_p\gg 1$                          | 7 | 118    | 147     | 173          | 243         |                         |
| E <sub>gp1</sub> in eV                 | 7 | 2.294  | 2.343   | 2.387        | 2.505       |                         |
| n                                      | 7 | 3.130  | 3.077   | 3.028        | 2.898       |                         |
| κ                                      | 7 | 0.608  | 0.544   | 0.489        | 0.358       |                         |
| $arepsilon_1$                          | 7 | 9.425  | 9.170   | 8.931        | 8.272       |                         |
| $arepsilon_2$                          | > | 3.805  | 3.350   | 2.964        | 2.078       |                         |
|  |   |        | x=1     |              |             |                         |
| For $\mathbf{r_a} = \mathbf{r_{Ga}}$ , |   |        |         |              |             |                         |
| $\eta_p\gg 1$                          | 7 | 168    | 184     | 198          | 239         |                         |
| $E_{gp1}$ in eV                        | 7 | 1.876  | 1.902   | 1.926        | 1.995       |                         |
| n                                      | 7 | 3.720  | 3.694   | 3.670        | 3.599       |                         |
| κ                                      | 7 | 1.298  | 1.249   | 1.202        | 1.076       |                         |
| $arepsilon_1$                          | > | 12.152 | 12.088  | 12.020       | 11.798      |                         |
| $arepsilon_2$                          | > | 9.663  | 9.230   | 8.826        | 7.748       |                         |
| For $\mathbf{r_a} = \mathbf{r_{In}}$ , |   |        |         |              |             |                         |
| $\eta_p\gg 1$                          | 7 | 123    | 141     | 157          | 203         |                         |
| $E_{gp1}$ in eV                        | 7 | 1.820  | 1.850   | 1.877        | 1.953       |                         |
| n                                      | 7 | 3.683  | 3.654   | 3.626        | 3.550       |                         |
| κ                                      | 7 | 1.411  | 1.351   | 1.297        | 1.152       |                         |
| $arepsilon_1$                          | 7 | 11.576 | 11.525  | 11.469       | 11.272      |                         |
| $arepsilon_2$                          | ٧ | 10.393 | 9.876   | 9.404        | 8.181       |                         |
| For $\mathbf{r_a} = \mathbf{r_{Cd}}$ , |   |        |         |              |             |                         |
| $\eta_p\gg 1$                          |   | 122    | 139     | 156          | 201         |                         |

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| $E_{gp1}$ in eV               | 7   | 1.818  | 1.847  | 1.875  | 1.951  |
|-------------------------------|-----|--------|--------|--------|--------|
| n                             | 7   | 3.683  | 3.653  | 3.625  | 3.548  |
| κ                             | >   | 1.416  | 1.356  | 1.301  | 1.155  |
| $arepsilon_1$                 | >   | 11.558 | 11.508 | 11.452 | 11.256 |
| $arepsilon_2$                 | >   | 10.428 | 9.907  | 9.431  | 8.201  |
|                               |     |        |        |        |        |
| $N (10^{18} \text{ cm}^{-3})$ | ) 7 | 15     | 26     | 60     | 100    |

**Table 5n.** In the X(x)-system, at E=3.2 eV and N =  $10^{20}$  cm<sup>-3</sup>, for given  $r_d$  and x, and from Equations (12, 15, 21, 20, 16), respectively, we can determine the variations of  $\eta_n(\gg 1$ , degenerate case),  $E_{gn1}$ , n,  $\kappa$ ,  $\varepsilon_1$  and  $\varepsilon_2$ , obtained as functions of T, being represented by the arrows:  $\nearrow$  and  $\searrow$ , noting that both  $\eta_n$  and  $E_{gn1}$  decrease with increasing T.

| T in K                               | 7      | 20    | 50    | 100   | 300   |
|--------------------------------------|--------|-------|-------|-------|-------|
|                                      |        |       | x=0   |       |       |
| For $\mathbf{r_d} = \mathbf{r_{Se}}$ |        |       |       |       |       |
| $\eta_n \gg 1$                       | ,<br>, | 840   | 336   | 168   | 56    |
| $E_{gn1}$ in eV                      | >      | 3.887 | 3.877 | 3.853 | 3.729 |
| n                                    | 7      | 1.080 | 1.094 | 1.126 | 1.295 |
| κ                                    | 7      | 0.350 | 0.340 | 0.316 | 0.207 |
| $\varepsilon_1$                      | 7      | 1.045 | 1.080 | 1.169 | 1.633 |
| $\varepsilon_2$                      | >      | 0.756 | 0.744 | 0.713 | 0.537 |
|                                      |        |       |       |       |       |
| For $\mathbf{r_d} = \mathbf{r_{Te}}$ | ,,     |       |       |       |       |
| $\eta_n\gg 1$                        | 7      | 833   | 333   | 166   | 55    |
| $E_{gn1}$ in eV                      | 7      | 3.915 | 3.905 | 3.881 | 3.757 |
| n                                    | 7      | 0.855 | 0.868 | 0.901 | 1.070 |
| κ                                    | >      | 0.379 | 0.369 | 0.344 | 0.230 |
| $arepsilon_1$                        | 7      | 0.587 | 0.618 | 0.694 | 1.092 |
| $\varepsilon_2$                      | >      | 0.648 | 0.641 | 0.621 | 0.493 |
|                                      |        |       |       |       |       |
| For $\mathbf{r_d} = \mathbf{r_{Sn}}$ | ,      |       |       |       |       |

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|--------------------------------------|---------------|-------|-------|-----------|--------------|---------------------------|
|                                      |               |       |       |           |              |                           |
| $\eta_n\gg 1$                        | 7             | 825   | 330   | 165       | 55           |                           |
| $E_{gn1}$ in eV                      | >             | 3.929 | 3.919 | 3.8       | 95 3.77      | 71                        |
| n                                    | 7             | 0.740 | 0.753 | 0.73      | 86 0.95      | 55                        |
| κ                                    | 7             | 0.394 | 0.384 | 0.3       | 59 0.24      | 42                        |
| $arepsilon_1$                        | 7             | 0.392 | 0.420 | 0.489     | 0.854        |                           |
| $arepsilon_2$                        | 7             | 0.583 | 0.578 | 0.564     | 0.462        |                           |
| x=0.5                                |               |       |       |           |              |                           |
|                                      |               |       |       |           |              |                           |
| For $\mathbf{r_d} = \mathbf{r_{Se}}$ | ,             |       |       |           |              |                           |
| $\eta_n\gg 1$                        | 7             | 462   | 185   | 92        | 31           |                           |
| $E_{gn1}$ in eV                      | >             | 2.669 | 2.661 | 2.642     | 2.540        |                           |
| n                                    | 7             | 2.675 | 2.684 | 2.706     | 2.821        |                           |
| κ                                    | 7             | 0.209 | 0.215 | 0.231     | 0.322        |                           |
| $arepsilon_1$                        | 7             | 7.113 | 7.159 | 7.272     | 7.857        |                           |
| $\varepsilon_2$                      | 7             | 1.117 | 1.155 | 1.250     | 1.819        |                           |
| For $\mathbf{r_d} = \mathbf{r_{Te}}$ | ······        |       |       |           |              |                           |
| $\eta_n\gg 1$                        | 7             | 461   | 184   | 92        | 31           |                           |
| $E_{gn1}$ in eV                      | >             | 2.715 | 2.707 | 2.688     | 2.587        |                           |
| n                                    | 7             | 2.428 | 2.437 | 2.460     | 2.576        |                           |
| κ                                    | 7             | 0.174 | 0.180 | 0.194     | 0.279        |                           |
| $arepsilon_1$                        | 7             | 5.867 | 5.909 | 6.014     | 6.558        |                           |
| $arepsilon_2$                        | 7             | 0.845 | 0.876 | 0.956     | 1.436        |                           |
| For $\mathbf{r_d} = \mathbf{r_{Sn}}$ | ,             |       |       |           |              |                           |
| $\eta_n\gg 1$                        | >             | 459 1 | 84    | 92        | 30.6         |                           |
| $E_{gn1}$ in eV                      | 7             | 2.740 | 2.732 | 2.713     | 2.612        |                           |
| n                                    | 7             | 2.300 | 2.309 | 2.332     | 2.448        |                           |
| κ                                    | <u>&gt;</u> ( | ).156 | 0.162 | 0.176     | 0.256        |                           |
| $\varepsilon_1$                      | 7 5           | 5.266 | 5.306 | 5.407     | 5.928        |                           |
| $\varepsilon_2$                      | 7             | 0.720 | 0.748 | 0.820     | 1.256        |                           |

x=1

| For $\mathbf{r_d} = \mathbf{r_{Se}}$ , |   |        |        |        |                           |    |
|--|---|--------|--------|--------|---------------------------|----|
| $\eta_n\gg 1$                          | 7 | 332    | 133    | 66     | 22                        |    |
| $E_{\tt gn1}$ in eV                    | 7 | 1.744  | 1.737  | 1.722  | 1.644                     |    |
| n                                      | 7 | 3.718  | 3.724  | 3.739  | 3.814                     |    |
| κ                                      | 7 | 1.572  | 1.585  | 1.618  | 1.794                     |    |
| $arepsilon_1$                          | 7 | 11.354 | 11.357 | 11.362 | <b>11.33</b> <sup>2</sup> | ļ. |
| $arepsilon_2$                          | 7 | 11.693 | 11.809 | 12.101 | 13.690                    | )  |
| For $\mathbf{r_d} = \mathbf{r_{Te}}$ , |   |        |        |        |                           |    |
| $\eta_n\gg 1$                          | 7 | 331    | 132.6  | 66.3   | 22                        |    |
| $E_{gn1}$ in eV                        | > | 1.826  | 1.820  | 1.805  | 1.726                     |    |
| n                                      | 7 | 3.437  | 3.443  | 3.458  | 3.535                     |    |
| κ                                      | 7 | 1.399  | 1.412  | 1.443  | 1.609                     |    |
| $arepsilon_1$                          | 7 | 9.856  | 9.863  | 9.877  | 9.908                     |    |
| $\varepsilon_2$                        | 7 | 9.621  | 9.823  | 9.980  | 11.38                     | 0  |
| For $\mathbf{r_d} = \mathbf{r_{Sn}}$ , |   |        |        |        |                           |    |
| $\eta_n\gg 1$                          | 7 | 331    | 132.5  | 66.2   | 22                        |    |
| $E_{\tt gn1}$ in eV                    | 7 | 1.866  | 1.860  | 1.845  | 1.767                     |    |
| n                                      | 7 | 3.294  | 3.300  | 3.315  | 3.393                     |    |
| κ                                      | 7 | 1.318  | 1.330  | 1.360  | 1.522                     |    |
| $\varepsilon_1$                        | 7 | 9.113  | 9.121  | 9.140  | 9.194                     |    |
| $arepsilon_2$                          | 7 | 8.686  | 8.781  | 9.021  | 10.330                    |    |
| T in K                                 | 7 | 20     | 50     | 100    | 300                       |    |

**Table 5p.** In the X(x)-system, at E=3.2 eV and N =  $10^{20}$  cm<sup>-3</sup>, for given  $r_a$  and x, and from Equations (12, 15, 21, 20, 16), respectively, we can determine the variations of  $\eta_p(\gg 1, \text{degenerate case})$ ,  $E_{gp1}$ , n,  $\kappa$ ,  $\varepsilon_1$  and  $\varepsilon_2$ , obtained as functions of T, being represented by the arrows:  $\nearrow$  and  $\searrow$ , noting that both  $\eta_p$  and  $E_{gp1}$  decrease with increasing T.

| T in K                                 | 7 | 20     | 50     | 100    | 300   |
|--|---|--------|--------|--------|-------|
|  |   |        | x=0    |        |       |
| For $\mathbf{r_a} = \mathbf{r_{Ga}}$ , | , |        |        |        |       |
| $\eta_p\gg 1$                          | > | 501    | 200    | 100    | 33    |
| $E_{gp1}$ in eV                        | > | 3.405  | 3.394  | 3.371  | 3.247 |
| n                                      | 7 | 1.845  | 1.858  | 1.888  | 2.046 |
| κ                                      | 7 | 0.031  | 0.028  | 0.022  | 0.002 |
| $\varepsilon_1$                        | 7 | 3.404  | 3.450  | 3.566  | 4.186 |
| $\varepsilon_2$                        | 7 | 0.115  | 0.105  | 0.082  | 0.007 |
| For $\mathbf{r_a} = \mathbf{r_{In}}$ , |   |        |        |        |       |
| $\eta_p\gg 1$                          | > | 351    | 140    | 70     | 23    |
| E <sub>gp1</sub> in eV                 | 7 | 3.173  | 3.163  | 3.139  | 3.015 |
| n                                      | 7 | 2.051  | 2.063  | 2.093  | 2.245 |
| κ                                      | 7 | 0.0005 | 0.0009 | 0.003  | 0.025 |
| $arepsilon_1$                          | 7 | 4.207  | 4.257  | 4.380  | 5.042 |
| $\varepsilon_2$                        | 7 | 0.002  | 0.004  | 0.011  | 0.114 |
| For $\mathbf{r_a} = \mathbf{r_{Cd}}$ , | , |        |        |        |       |
| $\eta_p\gg 1$                          | > | 345    | 138    | 69     | 23    |
| E <sub>gp1</sub> in eV                 | 7 | 3.163  | 3.153  | 3.129  | 3.005 |
| n                                      | 7 | 2.061  | 2.073  | 2.102  | 2.255 |
| κ                                      | 7 | 0.001  | 0.0016 | 0.0037 | 0.028 |
| $arepsilon_{	exttt{1}}$                | 7 | 4.246  | 4.296  | 4.420  | 5.083 |
| $\varepsilon_2$                        | 7 | 0.004  | 0.0066 | 0.015  | 0.127 |
|  |   |        |        |        |       |

| or | IØ. |
|----|-----|

| For $\mathbf{r_a} = \mathbf{r_{Ga}}$   | ,           |        |           |        |       |       |     |
|--|-------------|--------|-----------|--------|-------|-------|-----|
| $\eta_p\gg 1$                          | 7           | 308    | 123       |        | 62    |       | 20  |
| $E_{gp1}$ in $eV$                      | 7           | 2.593  | 2.585     | 2.566  | 2.4   | 464   |     |
| n                                      | 7           | 2.891  | 2.900     | 2.922  | 3.0   | 36    |     |
| κ                                      | <b>→</b> 0. | .273   | 0.280 0.2 | .98    | 0.401 |       |     |
| $\varepsilon_1$                        | 7           | 8.282  | 8.330     | 8      | .449  | 9.    | 055 |
| $\varepsilon_2$                        | 7           | 1.5    | 1.623     | 1.741  | 2     | 2.435 |     |
| For $\mathbf{r_a} = \mathbf{r_{In}}$ , | ,           |        |           |        |       |       |     |
| $\eta_p\gg 1$                          | >           | 245    | 98        | 49     | 1     | 16    |     |
| $E_{gp1}$ in eV                        | >           | 2.508  | 2.500     | 2.481  | 2     | .379  |     |
| n                                      | 7           | 2.897  | 2.906     | 2.928  | 3     | .040  |     |
| κ                                      | 7           | 0.355  | 0.363     | 0.383  | 0     | .500  |     |
| $\varepsilon_1$                        | 7           | 8.268  | 8.314     | 8.426  | 8     | .995  |     |
| $\varepsilon_2$                        | 7           | 2.056  | 2.101     | 2.246  | 3     | .040  |     |
| For $\mathbf{r_a} = \mathbf{r_{Cd}}$   | ,           |        |           |        |       |       |     |
| $\eta_p\gg 1$                          | 7           | 243    | 97        | 48     | 16    | 5     |     |
| $E_{gp1}$ in eV                        | >           | 2.505  | 2.497     | 2.477  | 2.3   | 375   |     |
| n                                      | 7           | 2.898  | 2.907     | 2.929  | 3.0   | 42    |     |
| κ                                      | 7           | 0.358  | 0.367     | 0.387  | 0.5   | 04    |     |
| $arepsilon_1$                          | 7           | 8.272  | 8.318     | 8.429  | 8.9   | 97    |     |
| $\varepsilon_2$                        | 7           | 2.078  | 2.132     | 2.269  | 3.0   | 67    |     |
|  |             |        | x=1       |        |       |       |     |
| For $\mathbf{r_a} = \mathbf{r_{Ga}}$   | ··          |        |           |        |       |       |     |
| $\eta_p\gg 1$                          | `<br>\      | 239    | 96        | 48     | 20.   | 6     |     |
| E <sub>gp1</sub> in eV                 | >           | 1.995  | 1.989     | 1.974  | 2.1   |       |     |
| n                                      | 7           | 3.600  | 3.606     | 3.621  | 3.43  | 34    |     |
| κ                                      | 7           | 1.076  | 1.087     | 1.114  | 0.85  | 52    |     |
| $arepsilon_1$                          | 7           | 11.798 | 11.820    | 11.871 | 11.0  | 070   |     |
|  |             |        |           |        |       |       |     |

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|--|---------------|--------|--|--------|--------|--|--|
| $arepsilon_2$                          | 7 7           | 7.748  | 7.840  | 8.071  | 5.851  |  |  |
| For $\mathbf{r_a} = \mathbf{r_{In}}$ , |               |        |  |        |        |  |  |
| $\eta_p\gg 1$                          | 7             | 203    | 81   | 40     | 13.45  |  |  |
| $E_{gp1}$ in eV                        | >             | 1.953  | 1.947  | 1.932  | 1.853  |  |  |
| n                                      | 7 3           | 3.550  | 3.556  | 3.571  | 3.651  |  |  |
| κ                                      | <b>&gt;</b> 1 | .152   | 1.164  | 1.192  | 1.345  |  |  |
| $arepsilon_1$                          | <b>&gt;</b> 1 | 1.272  | 11.290   | 11.333 | 11.519 |  |  |
| $arepsilon_2$                          | <b>≯</b> 8    | .181   | 8.275  | 8.513  | 9.818  |  |  |
| For $\mathbf{r_a} = \mathbf{r_{Cd}}$   | ,             |        |  |        |        |  |  |
| $\eta_p\gg 1$                          | >             | 201    | 80   | 40     | 13.35  |  |  |
| $E_{gp1}$ in eV                        | >             | 1.951  | 1.945  | 1.930  | 1.851  |  |  |
| n                                      | 7             | 3.548  | 3.555  | 3.570  | 3.649  |  |  |
| κ                                      | 7             | 1.155  | 1.167  | 1.195  | 1.348  |  |  |
| $arepsilon_1$                          | 7             | 11.256 | 11.274   | 11.317 | 11.501 |  |  |
| $arepsilon_2$                          | 7             | 8.201  | 8.296  | 8.533  | 9.840  |  |  |
| T in K                                 | 7             | 20     | 50   | 100    | 300    |  |  |