

World Journal of Engineering Research and Technology WJERT

www.wjert.org





OPTICAL COEFFICIENTS IN THE N(P)-TYPE DEGENERATE CdSe(1-x) S(x)-CRYSTALLINE ALLOY, DUE TO THE NEW STATIC DIELECTRIC CONSTANT-LAW AND THE GENERALIZED MOTT CRITERIUM IN THE METAL-INSULATOR TRANSITION (15)

Prof. Dr. Huynh Van Cong*

Université de Perpignan Via Domitia, Laboratoire de Mathématiques et Physique (LAMPS), EA 4217, Département de Physique, 52, Avenue Paul Alduy, F-66 860 Perpignan, France.

Article Received on 21/09/2024

Article Revised on 11/10/2024

Article Accepted on 01/11/2024



*Corresponding Author Prof. Dr. Huynh Van Cong

Université de Perpignan Via Domitia, Laboratoire de Mathématiques et Physique (LAMPS), EA 4217, Département de Physique, 52, Avenue Paul Alduy, F-66 860 Perpignan, France.

ABTRACT

In the n(p)-type $\mathbf{CdSe_{1-x}S_{x^{-}}}$ crystalline alloy, with $0 \le x \le 1$, basing on our two recent works^[1,2], for a given x, and with an increasing $\mathbf{r_{d(a)}}$, the optical coefficients have been determined, as functions of the photon energy E, total impurity density N, the donor (acceptor) radius $\mathbf{r_{d(a)}}$, concentration x, and temperature T.

Those results have been affected by (i) the important new $\varepsilon(\mathbf{r}_{d(a)}, \mathbf{x})$ law, developed in Equations (8a, 8b), stating that, for a given x, due to
the impurity-size effect, ε decreases (Σ) with an increasing (\nearrow) $\mathbf{r}_{d(a)}$,
and then by (ii) the generalized Mott critical d(a)-density defined in the
metal-insulator transition (MIT), $\mathbf{N}_{\text{CDn}(\text{NDp})}(\mathbf{r}_{d(a)}, \mathbf{x})$, as observed in

Equations (8c, 9a). Furthermore, we also showed that $N_{CDn(NDp)}$ is just the density of carriers localized in exponential band tails, with a precision of the order of **2.88** × **10**⁻⁷, as that given in Table 4 of Ref.^[1], according to a definition of the effective density of electrons (holes) given in parabolic conduction (valence) bands by: $N^*(N, r_{d(a)}, x) \equiv N - N_{CDn(NDp)}(r_{d(a)}, x)$, as defined in Eq. (9d).

In summary, due to the new $\varepsilon(r_{d(a)},x)$ -law and to the effective density of electrons (holes) given in parabolic conduction (valence) bands $N^*(N,r_{d(a)},x)$, for a given x, and with an

increasing $r_{d(a)}$, the numerical results of all the optical coefficients, obtained in appropriated physical conditions (E, N, T), and calculated by using Equations (15, 16, 20, 21), are reported in Tables 1, 2, 3n, 3p, 4n, 4p, 5n, and 5p in Appendix 1.

KEYWORS: $CdSe_{1-x}S_x$ - crystalline alloy; impurity-size effect; Mott critical impurity density in the MIT, optical coefficients.

INTRODUCTION

Here, basing on our two recent works^[1,2] and also other ones^[3-8], all the optical coefficients given in the n(p)-type $\mathbf{X}(\mathbf{x}) \equiv \mathbf{CdSe_{1-x}S_x}$ - crystalline alloy, with $0 \le x \le 1$, are investigated, as functions of the photon energy E, total impurity density N, the donor (acceptor) radius $\mathbf{r}_{d(a)}$, concentration x, and temperature T.

Then, for a given x, and with an increasing $r_{d(a)}$, the numerical results of all the optical coefficients, obtained in appropriated physical conditions (E, N, T), and calculated by using Equations (15, 16, 20, 21), are reported in Tables 1, 2, 3n, 3p, 4n, 4p, 5n, and 5p in Appendix 1.

ENERGY BAND STUCTURE PARAMETERS

First of all, in the $n^+(p^+) - p(n) X(x)$ - crystalline alloy at T=0 K, we denote the donor (acceptor) d(a)-radius by $r_{d(a)}$, and also the intrinsic one by: $r_{do(ao)} = r_{Se(Cd)} = 0.114$ nm (0.148 nm).

A. Effect of x- concentration

Here, the intrinsic energy-band-structure parameters [1], are expressed as functions of x, are given in the following.

(i)-The unperturbed relative effective electron (hole) mass in conduction (valence) bands are given by:

$$m_{c(v)}(x)/m_0 = 0.197 (0.801) \times x + 0.11 (0.45) \times (1 - x).$$
 (1)

(ii)-The unperturbed relative static dielectric constant of the intrinsic of the single crystalline X- alloy is found to be defined by:

$$\varepsilon_0(x) = 9 \times x + 10.2 \times (1 - x). \tag{2}$$

(iii)-Finally, the unperturbed band gap at 0 K is found to be given by:

$$E_{go}(x) = 2.58 \times x + 1.84 \times (1 - x).$$
 (3)

Therefore, we can define the effective donor (acceptor)-ionization energy in absolute values as:

$$E_{do(ao)}(x) = \frac{{}^{13600 \times [m_{C(v)}(x)/m_0]}}{[\epsilon_0(x)]^2} \text{ meV}, \tag{4}$$

and then, the isothermal bulk modulus, by:

$$B_{do(ao)}(x) \equiv \frac{E_{do(ao)}(x)}{\left(\frac{4\pi}{3}\right) \times \left(r_{do(ao)}\right)^3}.$$
 (5)

B. Effect of Impurity $r_{d(a)}$ -size, with a given x

Here, the changes in all the energy-band-structure parameters, expressed in terms of the effective relative dielectric constant $\varepsilon(r_{d(a)}, x)$, developed as follows.

At $r_{d(a)} = r_{do(ao)}$, the needed boundary conditions are found to be, for the impurity-atom volume $V = (4\pi/3) \times \left(r_{d(a)}\right)^3$, $V_{do(ao)} = (4\pi/3) \times \left(r_{do(ao)}\right)^3$, for the pressure $p, p_o = 0$, and for the deformation potential energy (or the strain energy) $\sigma, \sigma_o = 0$. Further, the two important equations^[1,7], used to determine the σ -variation, $\Delta \sigma \equiv \sigma - \sigma_o = \sigma$, are defined by: $\frac{dp}{dv} = \frac{B}{v}$ and $p = \frac{d\sigma}{dv}$. giving: $\frac{d}{dv}(\frac{d\sigma}{dv}) = \frac{B}{v}$. Then, by an integration, one gets:

$$\left[\Delta\sigma(r_{d(a)},x)\right]_{n(p)} \hspace{0.5cm} = \hspace{0.5cm} B_{do(ao)}(x) \hspace{0.5cm} \times (V- \hspace{0.5cm} V_{do(ao)} \hspace{0.5cm}) \times \hspace{0.5cm} \ln$$

Furthermore, we also shown that, as $r_{d(a)} > r_{do(ao)}$ ($r_{d(a)} < r_{do(ao)}$), the compression (dilatation) gives rise to the increase (the decrease) in the energy gap $E_{gn(gp)}(r_{d(a)},x)$, and the effective donor (acceptor)-ionization energy $E_{d(a)}(r_{d(a)},x)$ in absolute values, obtained in the effective Bohr model, which is represented respectively by: $\pm \left[\Delta \sigma(r_{d(a)},x) \right]_{n(p)}$,

$$\begin{split} E_{gno(gpo)}(r_{d(a)},x) - E_{go}(x) &= E_{d(a)}(r_{d(a)},x) - E_{do(ao)}(x) = E_{do(ao)}(x) \times \left[\left(\frac{\epsilon_0(x)}{\epsilon(r_{d(a)})} \right)^2 - 1 \right] \\ &= + \left[\Delta \sigma(r_{d(a)},x) \right]_{n(p)} \end{split}$$

for $r_{d(a)} \ge r_{do(ao)}$, and for $r_{d(a)} \le r_{do(ao)}$,

$$\begin{split} E_{gno(gpo)}(\mathbf{r}_{d(a)},\mathbf{x}) - E_{go}(\mathbf{x}) &= E_{d(a)}(\mathbf{r}_{d(a)},\mathbf{x}) - E_{do(ao)}(\mathbf{x}) = E_{do(ao)}(\mathbf{x}) \times \left[\left(\frac{\epsilon_0(\mathbf{x})}{\epsilon(\mathbf{r}_{d(a)})} \right)^2 - 1 \right] \\ &= - \left[\Delta \sigma(\mathbf{r}_{d(a)},\mathbf{x}) \right]_{n(p)} \end{split} \tag{7}$$

Therefore, from Equations (6) and (7), one obtains the expressions for relative dielectric constant $\varepsilon(r_{d(a)},x)$ and energy band gap $E_{gn(gp)}(r_{d(a)},x)$, as:

$$\text{(i)-for } r_{d(a)} \geq r_{do(ao)} \text{, since } \epsilon(r_{d(a)}, x) = \frac{\epsilon_0(x)}{\sqrt{1 + \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3}} \leq \epsilon_0(x) \text{, being a new}$$

 $\varepsilon(\mathbf{r}_{\mathbf{d}(\mathbf{a})},\mathbf{x})$ -law,

$$\begin{split} E_{gno(gpo)}\big(r_{d(a)},x\big) - E_{go}(x) &= E_{d(a)}\big(r_{d(a)},x\big) - E_{do(ao)}(x) = E_{do(ao)}(x) \times \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \\ &\ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 \geq 0, \end{split} \tag{8a}$$

according to the increase in both $E_{gn(gp)}(r_{d(a)},x)$ and $E_{d(a)}(r_{d(a)},x)$, with increasing $r_{d(a)}$ and for a given x, and

$$\text{(ii)-for } r_{d(a)} \leq r_{do(ao)}, \text{ since } \epsilon(r_{d(a)},x) = \frac{\epsilon_0(x)}{\sqrt{1 - \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3}} \geq \epsilon_0(x), \text{ with a physical } \epsilon_0(x)$$

$$\text{condition:} \left[\left(\frac{r_{d(a)}}{r_{do(ao)}} \right)^3 - 1 \right] \times \ln \left(\frac{r_{d(a)}}{r_{do(ao)}} \right)^3 < 1, \text{ being a new } \epsilon(r_{d(a)}, x) \text{-law},$$

$$\begin{split} E_{gno(gpo)}\big(r_{d(a)},x\big) - E_{go}(x) &= E_{d(a)}\big(r_{d(a)},x\big) - E_{do(ao)}(x) = -E_{do(ao)}(x) \times \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 &\leq 0, \quad (8b) \end{split}$$

corresponding to the decrease in both $E_{gn(gp)}(r_{d(a)},x)$ and $E_{d(a)}(r_{d(a)},x)$, with decreasing $r_{d(a)}$ and for a given x. It is interesting to note that, in the p-type case, since $r_a=r_B=0.088$ nm $\ll r_{ao}=r_{Cd}=0.148$ nm , the above physical condition is not satisfactory as: $\left[\left(\frac{r_B}{r_{Cd}}\right)^3-1\right]\times \ln\left(\frac{r_B}{r_{Cd}}\right)^3=1.2317701>1$. Thus, the B-acceptor can not be taken in the present p-type case.

Therefore, the effective Bohr radius $a_{Bn(Bp)}(r_{d(a)},x)$ is defined by:

$$a_{Bn(Bp)}(r_{d(a)},x) \equiv \frac{\epsilon(r_{d(a)},x) \times \hbar^2}{m_{c(v)}(x) \times q^2} = 0.53 \times 10^{-8} \text{ cm} \times \frac{\epsilon(r_{d(a)},x)}{m_{c(v)}(x)/m_0}. \tag{8c}$$

Furthermore, it is interesting to remark that the critical total donor (acceptor)-density in the metal-insulator transition (MIT) at T=0 K, $N_{CDn(NDp)}(r_{d(a)},x)$, was given by the Mott's criterium, with an empirical parameter, $M_{n(p)}$, as:

$$N_{CDn(CDp)}(r_{d(a)}, x)^{1/3} \times a_{Bn(Bp)}(r_{d(a)}, x) = M_{n(p)}, M_{n(p)} = 0.25,$$
 (9a)

depending thus on our new $\varepsilon(r_{d(a)}, x)$ -law.

This excellent one can be explained from the definition of the reduced effective Wigner-Seitz (WS) radius $r_{sn(sp)}$, characteristic of interactions, by:

$$r_{sn(sp)}(N, r_{d(a)}, x) \equiv \left(\frac{3}{4\pi N}\right)^{1/3} \times \frac{1}{a_{Bn(Bp)}(r_{d(a)}, x)} = 1.1723 \times 10^8 \times \left(\frac{1}{N}\right)^{1/3} \times \frac{m_{C(v)}(x)/m_0}{\epsilon(r_{d(a)}, x)}, (9b)$$

being equal to, in particular, at $N=N_{CDn(CDp)}(r_{d(a)},x)$: $r_{sn(sp)}(N_{CDn(CDp)}(r_{d(a)},x), r_{d(a)},x)=$ **2.4814**, for any $(r_{d(a)},x)$ -values. So, from Eq. (9b), one also has:

$$N_{CDn(CDp)}(r_{d(a)}, x)^{1/3} \times a_{Bn(Bp)}(r_{d(a)}, x) = \left(\frac{3}{4\pi}\right)^{\frac{1}{3}} \times \frac{1}{2.4814} = 0.25 = (WS)_{n(p)} = M_{n(p)}.$$
(9c)

Thus, the above Equations (9a, 9b, 9c) confirm our new $\varepsilon(r_{d(a)}, x)$ -law, given in Equations (8a, 8b).

Furthermore, by using $M_{n(p)} = 0.25$, according to the empirical Heisenberg parameter $\mathcal{H}_{n(p)} = 0.47137$, as those given in Equations (8, 15) of the Ref.^[1], we have also showed that $N_{\text{CDn(CDp)}}$ is just the density of electrons (holes) localized in the exponential conduction (valence)-band tail, with a precision of the order of 2.88×10^{-7} . Therefore, the density of electrons (holes) given in parabolic conduction (valence) bands can be defined, as that given in compensated materials, by:

$$N^*(N, r_{d(a)}, x) \equiv N - N_{CDn(NDp)}(r_{d(a)}, x). \tag{9d}$$

C. Effect of temperature T, with given x and $r_{d(a)}$

Here, the intrinsic band gap $E_{gni(gpi)}(r_{d(a)}, x, T)$ at any T is given by:

$$E_{gni(gpi)}(r_{d(a)},x,T) \text{ in eV} = E_{gno(gpo)}(r_{d(a)},x) - 10^{-4} \times T^2 \times \left\{ \frac{3.065 \times x}{T + 94 \text{ K}} + \frac{5.405 \times (1-x)}{T + 204 \text{ K}} \right\}, \tag{10}$$

suggesting that, for given x and $r_{d(a)}$, $E_{gni(gpi)}$ decreases with an increasing T.

Then, in the following, for the study of optical phenomena, one denote the conduction (valence)-band density of states by $N_{c(v)}(T,x)$ as:

$$N_{c(v)}(T,x) = 2 \times g_{c(v)}(x) \times \left(\frac{m_{r(x)} \times k_{B}T}{2\pi \hbar^{2}}\right)^{\frac{3}{2}} (cm^{-3}), g_{v}(x) \equiv 1 \times x + 1 \times (1-x) = 1,$$
 (11)

where $m_r(x)/m_o$ is the reduced effective mass $m_r(x)/m_o$, defined by :

$$m_r(x) \equiv [m_c(x) \times m_v(x)]/[m_c(x) + m_v(x)].$$

D. Heavy Doping Effect, with given T, x and $r_{d(a)}$

Here, as given in our previous works^[1,2], the Fermi energy $E_{Fn}(-E_{Fp})$, and the band gap narrowing are reported in the following.

First, the reduced Fermi energy $\eta_{n(p)}$ or the Fermi energy $E_{Fn}(-E_{Fp})$, obtained for any T and any effective d(a)-density, $N^*(N,r_{d(a)},x)=N^*$, defined in Eq. (9d), for a simplicity of presentation, being investigated in our previous paper^[8], with a precision of the order of 2.11×10^{-4} , is found to be given by:

$$\eta_{n(p)}(u) \equiv \frac{E_{Fn}(u)}{k_B T} (\frac{-E_{Fp}(u)}{k_B T}) = \frac{G(u) + A u^B F(u)}{1 + A u^B}, A = 0.0005372 \text{ and } B = 4.82842262, \tag{12}$$

where u is the reduced electron density, $u(N,r_{d(a)},x,T)\equiv \frac{N^*}{N_{c(v)}(T,x)} \ ,$

$$F(u) = au^{\frac{2}{3}} \left(1 + bu^{-\frac{4}{3}} + cu^{-\frac{8}{3}}\right)^{-\frac{2}{3}}, a = \left[(3\sqrt{\pi}/4) \times u\right]^{2/3}, \ b = \frac{1}{8} \left(\frac{\pi}{a}\right)^2, \ c = \frac{62.3739855}{1920} \left(\frac{\pi}{a}\right)^4,$$

and $G(u) \simeq Ln(u) + 2^{-\frac{3}{2}} \times u \times e^{-du}; d = 2^{3/2} \left[\frac{1}{\sqrt{27}} - \frac{3}{16} \right] > 0$. Therefore, from Eq. (12), the

Fermi energies are expressed as functions of variables : N, $r_{d(a)}$, x, and T.

Here, one notes that: (i) as $u\gg 1$, according to the HD [d(a)- X(x)- alloy] ER-case, or to the degenerate case, Eq. (12) is reduced to the function F(u), and in particular at T=0 and as $N^*=0$, according to the metal-insulator transition (MIT), one has: $+E_{Fn}(-E_{Fp})=\frac{\hbar^2}{2\times m_r(x)}\times (3\pi^2N^*)^{2/3}=0$, and (ii) $\frac{E_{Fn}(u\ll 1)}{k_BT}(\frac{-E_{Fp}(u\ll 1)}{k_BT})\ll -1$, to the LD [a(d)- X(x)- alloy] BR-case, or to the non-degenerate case, Eq. (12) is reduced to the function G(u), noting that the notations: **HD(LD)** and **ER(BR)** denote the heavily doped (lightly doped)-cases and emitter (base)-regions, respectively.

Now, in Eq. (9b), in which one replaces $m_{c(v)}(x)$ by $m_r(x)$, the effective Wigner-Seitz radius becomes as:

$$r_{sn(sp)}(N, r_{d(a)}, x) = 1.1723 \times 10^8 \times \left(\frac{g_{c(v)}(x)}{N^*}\right)^{1/3} \times \frac{m_r(x)}{\varepsilon(r_{d(a)}, x)},$$
 (13a)

the correlation energy of an effective electron gas, $E_{cn(cp)}(N, r_{d(a)}, x)$, is given as:

$$E_{cn(cp)}\big(N,r_{d(a)},x\big) = \frac{_{-0.87553}}{_{0.0908+r_{sn(sp)}}} + \frac{\frac{_{0.87553}}{_{0.0908+r_{sn(sp)}}} + \left(\frac{_{2[1-ln(2)]}}{\pi^2}\right) \times ln(r_{sn(sp)}) - 0.093288}{_{1+0.03847728\times r_{sn(sp)}^{1.67378876}}}\,. \tag{13b}$$

Then, taking into account various spin-polarized chemical potential-energy contributions such as: exchange energy of an effective electron (hole) gas, majority-carrier correlation energy of an effective electron (hole) gas, minority hole (electron) correlation energy, majority electron (hole)-ionized d(a) interaction screened Coulomb potential energy, and finally minority hole (electron)-ionized d(a) interaction screened Coulomb potential energy, the band gap narrowings are given in the following.

In the n-type HD X(x)- alloy, the BGN is found to be given by:

$$\begin{split} &\Delta E_{gno}(N,r_{d},x) = a_{1} \times \frac{\epsilon_{0}(x)}{\epsilon(r_{d},x)} \times N_{r}^{1/3} + a_{2} \times \frac{\epsilon_{0}(x)}{\epsilon(r_{d},x)} \times N_{r}^{\frac{1}{3}} \times (2.503 \times [-E_{cn}(r_{sn}) \times r_{sn}]) + \\ &a_{3} \times \left[\frac{\epsilon_{0}(x)}{\epsilon(r_{d},x)}\right]^{5/4} \times \sqrt{\frac{m_{v}}{m_{r}}} \times N_{r}^{1/4} + a_{4} \times \sqrt{\frac{\epsilon_{0}(x)}{\epsilon(r_{d},x)}} \times N_{r}^{1/2} \times 2 + a_{5} \times \left[\frac{\epsilon_{0}(x)}{\epsilon(r_{d},x)}\right]^{\frac{3}{2}} \times N_{r}^{\frac{1}{6}} \\ &N_{r} \equiv \left(\frac{N^{*}}{N_{CDn}(r_{d},x)}\right), \end{split}$$

$$\Delta E_{gn}(N, r_d, x) = \Delta E_{gno}(N, r_d, x) \times \{3.5 \times x + 2.2 \times (1 - x)\}, \tag{14n}$$

where
$$a_1=3.8\times 10^{-3} (eV)$$
 , $a_2=6.5\times 10^{-4} (eV)$, $a_3=2.8\times 10^{-3} (eV)$ $a_4=5.597\times 10^{-3} (eV)$ and $a_5=8.1\times 10^{-4} (eV)$, and in the p-type HD X(x)- alloy, as:

$$\begin{split} \Delta E_{gpo}(N,r_{a},x) &= a_{1} \times \frac{\varepsilon_{0}(x)}{\varepsilon(r_{a},x)} \times N_{r}^{1/3} + a_{2} \times \frac{\varepsilon_{0}(x)}{\varepsilon(r_{a},x)} \times N_{r}^{\frac{1}{3}} \times \left(2.503 \times \left[-E_{cp}(r_{sp}) \times r_{sp}\right]\right) + \\ a_{3} \times \left[\frac{\varepsilon_{0}(x)}{\varepsilon(r_{a},x)}\right]^{5/4} \times \sqrt{\frac{m_{c}}{m_{r}}} \times N_{r}^{1/4} + 2a_{4} \times \sqrt{\frac{\varepsilon_{0}(x)}{\varepsilon(r_{a},x)}} \times N_{r}^{1/2} + a_{5} \times \left[\frac{\varepsilon_{0}(x)}{\varepsilon(r_{a},x)}\right]^{\frac{3}{2}} \times N_{r}^{\frac{1}{6}} \end{split}$$

$$N_r \equiv \left(\frac{N^*}{N_{CDp}(r_a.x)}\right),$$

$$\Delta E_{gp}(N, r_a, x) = \Delta E_{gpo}(N, r_a, x) \times \{33 \times x + 22 \times (1 - x)\}, \tag{14p}$$

where
$$a_1=3.15\times 10^{-3} (eV)$$
 , $a_2=5.41\times 10^{-4} (eV)$, $a_3=2.32\times 10^{-3} (eV)$, $a_4=4.12\times 10^{-3} (eV)$ and $a_5=9.8\times 10^{-5} (eV)$.

One also remarks that, as $N^* = 0$, according to the MIT, $\Delta E_{gn(gp)}(N, r_{d(a)}, x) = 0$.

OPTICAL BAND GAP

Here, the optical band gap is found to be defined by:

$$\begin{split} E_{gn1(gp1)}\big(N, r_{d(a)}, x, T\big) &\equiv \\ E_{gni(gpi)}(r_{d(a)}, x, T) - \Delta E_{gn(gp)}(N, r_{d(a)}, x) + (-)E_{Fn(Fp)}\big(N, r_{d(a)}, x, T\big), \end{split} \tag{15}$$

where $E_{gin(gip)}$, $[+E_{Fn}, -E_{Fp}] \ge 0$, and $\Delta E_{gn(gp)}$ are respectively determined in Equations [10, 12, 14n(p)], respectively. So, as noted above, at the MIT, Eq. (15) thus becomes: $E_{gn1(gp1)}(r_{d(a)},x) = E_{gno(gpo)}(r_{d(a)},x)$, according to: $N = N_{CDn(NDp)}(r_{d(a)},x)$.

OPTICAL COEFFICIENTS

The optical properties of any medium can be described by the complex refraction index N and the complex dielectric function ϵ , $\mathbb{N} \equiv n - i \kappa$ and $\epsilon \equiv \epsilon_1 - i \epsilon_2$, where $i^2 = -1$ and $\epsilon \equiv \mathbb{N}^2$. Therefore, the real and imaginary parts of ϵ denoted by ϵ_1 and ϵ_2 can thus be expressed in terms of the refraction index n and the extinction coefficient κ as: $\epsilon_1 \equiv n^2 - \kappa^2$ and $\epsilon_2 \equiv 2n\kappa$. One notes that the optical absorption coefficient α is related to ϵ_2 , n, κ , and the optical conductivity σ_0 , by [2]

$$\begin{split} \alpha(E,N,r_{d(a)},x,T) &\equiv \frac{\hbar q^2 \times |v(E)|^2}{n(E) \times \epsilon_{free} \, space \times cE} \times J(E^*) = \frac{E \times \epsilon_2(E)}{\hbar c n(E)} \equiv \frac{2E \times \kappa(E)}{\hbar c} \equiv \frac{4\pi \sigma_0(E)}{c n(E) \times \epsilon_{free} \, space} \,, \\ \epsilon_1 &\equiv n^2 - \kappa^2 \, \text{and} \, \, \epsilon_2 \equiv 2n\kappa, \end{split} \tag{16}$$

where, since $E \equiv \hbar \omega$ is the photon energy, the effective photon energy: $E^* = E - E_{gn1(gp1)} \big(N, r_{d(a)}, x, T \big) \text{ is thus defined as the reduced photon energy.}$

Here, -q, \hbar , |v(E)|, ω , $\epsilon_{free\,space}$, c and $J(E^*)$ respectively represent: the electron charge, Dirac's constant, matrix elements of the velocity operator between valence (conduction)-and-conduction (valence) bands in n(p)-type semiconductors, photon frequency, permittivity of free space, velocity of light, and joint density of states. It should be noted that, if the three functions such as: $|v(E)|^2$, $J(E^*)$ and n(E) are known, then the other optical dispersion functions as those given in Eq. (16) can thus be determined. Moreover, the normal-incidence reflectance, R(E), can be expressed in terms of $\kappa(E)$ and n(E) as:

$$R(E, N, r_{d(a)}, x, T) = \frac{[n(E)-1]^2 + \kappa(E)^2}{[n(E)+1]^2 + \kappa(E)^2}.$$
(17)

From Equations (16, 17), if the two optical functions, ε_1 and ε_2 , (or n and κ), are both known, the other ones defined above can thus be determined, noting also that: $\mathbf{E}_{\mathbf{gn1}(\mathbf{gp1})}(\mathbf{N}, \mathbf{r_{d(a)}}, \mathbf{x}, \mathbf{T}) = \mathbf{E}_{\mathbf{gn1}(\mathbf{gp1})}$, for a presentation simplicity.

Then, one has:

-at low values of $E \gtrsim E_{gn1(gp1)}$,

$$\begin{split} J_{n(p)}\big(E,N,r_{d(a)},x,T\big) &= \frac{1}{2\pi^2} \times \left(\frac{2m_r}{\hbar^2}\right)^{3/2} \times \frac{(E-E_{gn1(gp1)})^{a-(1/2)}}{E_{gn1(gpi)}^{a-1}} = \frac{1}{2\pi^2} \times \left(\frac{2m_r}{\hbar^2}\right)^{3/2} \times \\ &(E-E_{gn1(gp1)})^{1/2} \end{split} , \text{ for } a=1, \end{split} \label{eq:continuous}$$

and at large values of $E > E_{gn1(gp1)}$,

$$\begin{split} J_{n(p)}\big(E,N,r_{d(a)},x,T\big) &= \frac{1}{2\pi^2} \times \left(\frac{2m_r}{\hbar^2}\right)^{3/2} \times \frac{(E-E_{gn1(gp1)})^{a-(1/2)}}{E_{gn1(gpi)}^{a-1}} = \frac{1}{2\pi^2} \times \left(\frac{2m_r}{\hbar^2}\right)^{3/2} \times \\ \frac{(E-E_{gn1(gp1)})^2}{E_{gni(gpi)}^{3/2}} &\qquad \qquad , \text{ for } a=5/2. \end{split} \label{eq:jn(p)}$$

Further, one notes that, as $E \to \infty$, Forouhi and Bloomer (FB)^[4] claimed that $\kappa(E \to \infty) \to a$ constant, while the $\kappa(E)$ -expressions, proposed by Van Cong^[2] quickly go to 0 as E^{-3} , and consequently, their numerical results of the optical functions such as: $\sigma_0(E)$ and $\alpha(E)$, given in Eq. (16), both go to 0 as E^{-2} .

Now, an improved Forouhi-Bloomer parameterization model (FB-PM), used to determine the expressions of the optical coefficients in the degenerate $n^+(p^+) - p(n) \mathbf{X}(\mathbf{x}) \equiv \mathbf{CdSe_{1-x}S_x}$ -crystalline alloy, is now proposed as follows. Then, if denoting the functions G(E) and F(E) and by: $G(E) \equiv \sum_{i=1}^4 \frac{A_i}{E^2 - B_i E + C_i}$ and $F(E) \equiv \sum_{i=1}^4 \frac{A_i}{E^2 \times (1+10^{-4} \times \frac{E}{r}) - B_i E + C_i}$, we propose:

$$\kappa \big(E,N,r_{d(a)},x,T\big) = G(E) \times E_{gni(gpi)}^{3/2} \times \big(E^* \equiv E - E_{gn1(gp1)}\big)^{1/2}, \text{ for }$$

 $E_{gni(gpi)} \le E \le 2.3 \text{ eV},$

$$= F(E) \times \left(E^* \equiv E - E_{gn1(gp1)}\right)^2, \text{ for } E \ge 2.3 \text{ eV}, \tag{20}$$

being equal to 0 for $E^* = 0$ (or for $E = E_{gn1(gp1)}$), and also going to 0 as E^{-1} as $E \to \infty$, and further,

$$n(E,N,r_{d(a)},x,T) = n_{\infty}(r_{d(a)},x) + \sum_{i=1}^{4} \frac{x_i(\epsilon_{gn1(gp1)}) \times \epsilon + y_i(\epsilon_{gn1(gp1)})}{\epsilon^2 - B_i \epsilon + C_i}. \tag{21}$$

going to a constant as $E \to \infty$, since $n(E \to \infty, r_{d(a)}, x) \to n_{\infty}(r_{d(a)}, x) = \sqrt{\epsilon(r_{d(a)}, x)} \times \frac{\omega_T}{\omega_L}$, $\omega_T = 5.1 \times 10^{13} \text{ s}^{-1}$ [5] and $\omega_L = 8.9755 \times 10^{13} \text{ s}^{-1}$.

Here, the other parameters are determined by:

Then, as noted above, if the two optical functions, \mathbf{n} and κ , are both known, the other ones defined in Equations (16, 17) can also be determined.

NUMERICAL RESULTS

Now, some numerical results of those optical functions are investigated in the n(p)-type $\mathbf{X}(\mathbf{x}) \equiv \mathbf{CdSe_{1-x}S_{x^-}}$ crystalline alloy, as follows.

A. Metal-insulator transition (MIT)-case

As discussed above, the physical conditions used for the MIT are found to be given by: $T=0K, \qquad N^*=0 \qquad \text{or} \qquad N=N_{CDn(CDp)} \qquad , \qquad \text{giving} \qquad \text{rise} \qquad \text{to:} \\ E_{gn1(gp1)}\big(N^*=0,r_{d(a)},x,T=0\big)=E_{gn1(gp1)}\big(r_{d(a)},x\big)=E_{gno(gpo)}\big(r_{d(a)},x\big).$

Then, in this MIT-case, if $E = E_{gn1(gp1)}(r_{d(a)},x) = E_{gno(gpo)}(r_{d(a)},x)$, which can be defined as the critical photon energy: $E \equiv E_{CPE}(r_{d(a)},x)$, one obtains: $\kappa_{MIT}(r_{d(a)},x) = 0$ from Eq. (20), and from Eq. (16): $\epsilon_{2(MIT)}(r_{d(a)},x) = 0$, $\sigma_{O(MIT)}(r_{d(a)},x) = 0$ and $\alpha_{MIT}(r_{d(a)},x) = 0$, and the other functions such as: $n_{MIT}(r_{d(a)},x)$ from Eq. (21), and $\epsilon_{1(MIT)}(r_{d(a)},x)$ and $R_{MIT}(r_{d(a)},x)$ from Eq. (16) decrease with increasing $r_{d(a)}$ and E_{CPE} , as those investigated in Table 1 in Appendix 1.

B. Optical coefficients, obtained as $E \rightarrow \infty$

In Eq. (21), at any T, the choice of the real refraction index: $n\left(E\to\infty, r_{d(a)}, x, T\right) = n_{\infty}(r_{d(a)}, x) = \sqrt{\epsilon(r_{d(a)}, x)} \times \frac{\omega_T}{\omega_L} , \quad \omega_T = 5.1 \times 10^{13} \ s^{-1} \quad ^{[5]} \quad \text{and} \quad \omega_T = 5.1 \times 10^{13} \ s^{-1} \quad ^{[5]} \quad \text{and} \quad \omega_T = 5.1 \times 10^{13} \ s^{-1} \quad ^{[5]} \quad \text{and} \quad \omega_T = 5.1 \times 10^{13} \ s^{-1} \quad ^{[5]} \quad \text{and} \quad \omega_T = 5.1 \times 10^{13} \ s^{-1} \quad ^{[5]} \quad \text{and} \quad \omega_T = 5.1 \times 10^{13} \ s^{-1} \quad ^{[5]} \quad \text{and} \quad \omega_T = 5.1 \times 10^{13} \ s^{-1} \quad ^{[5]} \quad \text{and} \quad \omega_T = 5.1 \times 10^{13} \ s^{-1} \quad ^{[5]} \quad \text{and} \quad \omega_T = 5.1 \times 10^{13} \ s^{-1} \quad ^{[5]} \quad \text{and} \quad \omega_T = 5.1 \times 10^{13} \ s^{-1} \quad ^{[5]} \quad \text{and} \quad \omega_T = 5.1 \times 10^{13} \ s^{-1} \quad ^{[5]} \quad \text{and} \quad \omega_T = 5.1 \times 10^{13} \ s^{-1} \quad ^{[5]} \quad \text{and} \quad \omega_T = 5.1 \times 10^{13} \ s^{-1} \quad ^{[5]} \quad \text{and} \quad \omega_T = 5.1 \times 10^{13} \ s^{-1} \quad ^{[5]} \quad \text{and} \quad \omega_T = 5.1 \times 10^{13} \ s^{-1} \quad ^{[5]} \quad \text{and} \quad \omega_T = 5.1 \times 10^{13} \ s^{-1} \quad ^{[5]} \quad \text{and} \quad \omega_T = 5.1 \times 10^{13} \ s^{-1} \quad ^{[5]} \quad \text{and} \quad \omega_T = 5.1 \times 10^{13} \ s^{-1} \quad ^{[5]} \quad \omega_T = 5.1 \times 10^{13} \ s$

 $\omega_L=8.9755\times 10^{13}~s^{-1}$, was obtained from the Lyddane-Sachs-Teller relation^[5], from which T(L) represent the transverse (longitudinal) optical phonon modes. Then, from Equations (16, 17, 20), from such the asymptotic behavior ($E\to\infty$), we obtain: $\kappa_\infty(r_{d(a)},x)\to 0$ and $\epsilon_{2,\infty}(r_{d(a)},x)\to 0$, as E^{-1} , so that $\epsilon_{1,\infty}(r_{d(a)},x)$, $\sigma_{0,\infty}(r_{d(a)},x)$, $\alpha_\infty(r_{d(a)},x)$ and $R_\infty(r_{d(a)},x)$ go to their appropriate limiting constants for T=0K, as those investigated in Table 2 in Appendix 1.

C. Variations of some optical coefficients, obtained in P(Ga)-X(x)-system, as functions of E

In the P(Ga)-X(x)-system, at T=0K and N = $N_{CDn(CDp)}(r_{P(Ga)},x)$, our numerical results of n, κ , ϵ_1 and ϵ_2 are obtained from Equations (21, 20, 16), respectively, and expressed as functions of $E [\geq E_{CPE}(r_{P(Ga)},x)]$ and for given x, as those reported in Tables 3n and 3p in Appendix 1.

D. Variations of various optical coefficients, as functions of N

In the X(x)-system, at E=3.2 eV and T=20 K, for given $r_{d(a)}$ and x, and from Equations (12, 15, 21, 20, 16), respectively, we can determine the variations of $\eta_{n(p)}(\gg 1$, degenerate case), $E_{gn1(gp1)}$, n, κ , ε_1 and ε_2 , obtained as functions of N, being represented by the arrows: \nearrow and \searrow , as those tabulated in Tables 4n and 4p in Appendix 1.

E. Variations of various optical coefficients as functions of T

In the X(x)-system, at E=3.2 eV and N = 10^{20} cm⁻³, for given $r_{d(a)}$ and x, and from Equations (12, 15, 21, 20, 16), respectively, we can determine the variations of $\eta_{n(p)}(\gg 1$, degenerate case), $E_{gn1(gp1)}$, n, κ , ε_1 and ε_2 , obtained as functions of T, being represented by the arrows: \nearrow and \searrow , as those tabulated in Tables 5n and 5p in Appendix 1.

CONCLUDING REMARKS

In the n(p)-type $\mathbf{X}(\mathbf{x}) \equiv \mathbf{CdSe_{1-x}S_x}$ – crystalline alloy, by basing on our two recent works^[1,2], for a given x, and with an increasing $\mathbf{r_{d(a)}}$, the optical coefficients have been determined, as functions of the photon energy E, total impurity density N, the donor (acceptor) radius $\mathbf{r_{d(a)}}$, concentration x, and temperature T.

Those results have been affected by (i) the important new $\varepsilon(r_{d(a)},x)$ -law, developed in Equations (8a, 8b), stating that, for a given x, due to the impurity-size effect, ε decreases (Σ)

with an increasing (\nearrow) $\mathbf{r}_{d(a)}$, and then by (**ii**) the generalized Mott critical d(a)-density defined in the metal-insulator transition (MIT), $\mathbf{N}_{\text{CDn(NDp)}}(\mathbf{r}_{d(a)}, \mathbf{x})$, as observed in Equations (8c, 9a).

Further, we also showed that $N_{CDn(NDp)}$ is just the density of carriers localized in exponential band tails, with a precision of the order of 2.88×10^{-7} , as that given in Table 4 of Ref.^[1], according to a definition of the effective density of electrons (holes) given in parabolic conduction (valence) bands by: $N^*(N, r_{d(a)}, x) \equiv N - N_{CDn(NDp)}(r_{d(a)}, x)$, as defined in Eq. (9d).

In summary, due to the new $\varepsilon(r_{d(a)},x)$ -law and to the effective density of electrons (holes) given in parabolic conduction (valence) bands $N^*(N,r_{d(a)},x)$, for a given x, and with an increasing $r_{d(a)}$, the numerical results of all the optical coefficients, obtained in appropriated physical conditions (E, N, T), and calculated by using Equations (15, 16, 20, 21), are reported in Tables 1, 2, 3n, 3p, 4n, 4p, 5n, and 5p in Appendix 1.

REFERENCES

- 1. Van Cong, H. Critical density in MIT, obtained in n(p)-type degenerate $InSb_{1-x}P_x(As_x)$, $GaSb_{1-x}P_x(As_x, Te_x)$, $CdSe_{1-x}S_x(Te_x)$ crystalline alloys, and explained by that of carriers localized in exponential band tails (III). WJERT, 2024; 10(4): 191-220.
- 2. Van Cong, H. Optical coefficients in the n(p)-type degenerate CdTe_{1-x}Se_x- crystalline alloy, due to the new static dielectric constant-law and the generalized Mott criterium in the metal-insulator transition (10). WJERT, 2024; 10(11): 150-178.
- 3. Van Cong, H. Effects of donor size and heavy doping on optical, electrical and thermoelectric properties of various degenerate donor-silicon systems at low temperatures. American Journal of Modern Physics, 2018; 7: 136-165.
- 4. Forouhi A. R. & Bloomer I. Optical properties of crystalline semiconductors and dielectrics. Phys. Rev., 1988; 38: 1865-1874.
- 5. Aspnes, D.E. & Studna, A. A. Dielectric functions and optical parameters of Si, Se, GaP, GaAs, GaSb, InP, InAs, and InSb from 1.5 to 6.0 eV, Phys. Rev. B, 1983; 27: 985-1009.
- 6. Van Cong, H. et al. Optical bandgap in various impurity-Si systems from the metal-insulator transition study. Physica B, 2014; 436: 130-139.
- 7. Van Cong, H. et al. Size effect on different impurity levels in semiconductors. Solid State Communications, 1984; 49: 697-699.

8. Van Cong, H. & Debiais, G. A simple accurate expression of the reduced Fermi energy for any reduced carrier density. J. Appl. Phys., 1993; 73: 1545-1546.

www.wjert.org ISO 9001: 2015 Certified Journal 349

APPENDIX 1

Table 1. In the MIT-case, T=0K, N=N_{CDn(p)}($r_{d(a)}$,x), and the critical photon energy $E_{CPE} = E = E_{gno(gpo)}(r_{d(a)}$,x), if $E = E_{gn1(gp1)}(r_{d(a)}$,x) = $E_{CPE}(r_{d(a)}$,x), the numerical results of optical functions such as : $n_{MIT}(r_{d(a)}$,x), obtained from Eq. (21), and those of other ones: $\varepsilon_{1(MIT)}(r_{d(a)}$,x) and $R_{MIT}(r_{d(a)}$,x), from Eq. (16), decrease (Σ) with increasing (Σ) $r_{d(a)}$ and r_{CPE} .

Donor		P	Se	Те	Sn
r _d (nm) [4]	7	0.110	r _{do} =0.114 nr	n 0.132	0.140
At x=0 ,					
E _{CPE} in meV	7	1839.84	1840	1843.5	1847.55
n _{MIT}	>	2.977	2.972	2.874	2.786
$\varepsilon_{1(MIT)}$	>	8.866	8.836	8.262	7.762
R_{MIT}	7	0.247	0.246	0.234	0.222
			At x=0.5 ,		
E _{CPE} in meV	7	2209.75	2210	2215.5	2221.9
n_{MIT}	>	2.693	2.688	2.591	2.504
$\varepsilon_{1(MIT)}$	>	7.251	7.224	6.714	6.270
R _{MIT}	>	0.210	0.209	0.196	0.184
			At x=1 ,		
E _{CPE} in meV	7	2579.64	2580	2588	2597.4
n _{MIT}	>	2.406	2.401	2.306	2.220
$\varepsilon_{1(MIT)}$	>	5.790	5.766	5.318	4.927
R _{MIT}	>	0.170	0.1697	0.1561	0.143
Acceptor		(Ga I	n	Cd
r _a (nm)	7	0.	.126 0.	144 r _a	_o =0.148 nm
At x=0 ,					
E _{CPE} in meV	7	18	329.1 183	39.6	1840
n _{MIT}	>	3.	074 2.9	976	2.972
$\varepsilon_{1(MIT)}$	7	9	0.45 8.	85	8.83
R_{MIT}	>	0.	.259 0.2	247	0.246
A4 0.5					
At $x=0.5$, E_{CPE} in meV	2	21	192.9 220	00.4	2210
	<i>></i>			09.4 591	2.688
n _{MIT}	7			24	7.22
$\varepsilon_{1(MIT)}$					
R _{MIT}	7		.223 0.2	210	0.209

At
$$x=1$$
,

 E_{CPE} in meV \nearrow 2555.1 2579.1 2580

 n_{MIT} \searrow 2.506 2.405 2.401

 $\varepsilon_{1(MIT)}$ \searrow 6.28 5.78 5.766

 R_{MIT} \searrow 0.184 0.170 0.1697

Table 2. Here, as T=0K and N=N_{CDn(p)}($\mathbf{r}_{d(\mathbf{a})}$, \mathbf{x}), and for $E \to \infty$ the numerical results of $n_{\infty}(\mathbf{r}_{d(\mathbf{a})}$, x), $\varepsilon_{1,\infty}(\mathbf{r}_{d(\mathbf{a})}$, x), $\sigma_{0,\infty}(\mathbf{r}_{d(\mathbf{a})}$, x), $\sigma_{\infty}(\mathbf{r}_{d(\mathbf{a})}$, x) and $R_{\infty}(\mathbf{r}_{d(\mathbf{a})}$, x) go to their appropriate limiting constants.

Donor		P	Se	Te	Sn
At x=0 ,					
n_{∞}	7	1.8197	1.8147	1.7187	1.6330
	>	3.311	3.293	2.954	2.667
σ _{0,∞} in	10 ⁵ Ω×cm	8.303	8.281	7.842	7.451
	$(10^9 \times cm^{-1})$				
R_{∞}	>	0.084	0.0838	0.0699	0.0578
At x=0.5	5,				
n_{∞}	7	1.7654	1.7605	1.6674	1.5842
	7	3.116	3.099	2.780	2.510
$\sigma_{0,\infty}$ in	10 ⁵ Ω×cm	8.055	8.033	7.608	7.229
	$(10^9 \times cm^{-1})$	=2.1602			
R_{∞}	>	0.077	0.0759	0.0626	0.0511
At x=1 ,					
n_{∞}	7	1.7093	1.7046	1.6144	1.5339
	7	2.922	2.906	2.606	2.353
σ _{0,∞} in	10 ⁵ Ω×cm	7.800	7.778	7.367	6.999
	$(10^9 \times cm^{-1})$				
R_{∞}	>	0.068	0.0679	0.0552	0.0444
Accepto	r	Ga	In	Cd	
			At x=0 ,		
n_{∞}	7	1.910	1.818	1.815	
$\varepsilon_{1,\infty}$	<i>\</i>	3.648	3.304	3.293	
$\sigma_{0,\infty}$ in	$\frac{10^5}{\Omega \times cm}$	8.715	8.294	8.281	

α_{∞} in $(10^9 \times cm^{-1})=2.16$	602		
R _∞ ∨	0.098	0.084	0.0838
At x=0.5 ,			
n_{∞}	1.853	1.763	1.760
$\varepsilon_{1,\infty}$	3.433	3.110	3.099
$\sigma_{0,\infty}$ in $\frac{10^5}{\Omega \times cm}$	8.455	8.046	8.033
α_{∞} in $(10^9 \times cm^{-1})=2.16$	602		
R _∞ ∨	0.089	0.0763	0.0759
		At x=1 ,	
n_{∞}	1.794	1.707	1.705
$\varepsilon_{1,\infty}$ \	3.218	2.915	2.906
$\sigma_{0,\infty}$ in $\frac{10^5}{\Omega \times cm}$	8.186	7.791	7.778
α_{∞} in $(10^9 \times cm^{-1})=2.16$	602		
R_{∞}	0.0808	0.0683	0.0679

Table 3n: In the P-X(x)-system, and at T=0K and N = N_{CDn}(r_p,x), according to the MIT, our numerical results of n, κ , ϵ_1 and ϵ_2 are obtained from Equations (21, 20, 16), respectively, and expressed as functions of E [$\geq E_{CPE}(r_p,x)$] and κ , noting that (i) $\kappa = 0$ and $\epsilon_2 = 0$ at $E = E_{CPE}(r_p,x)$, and $\kappa \to 0$ and $\epsilon_2 \to 0$ as $E \to \infty$.

E in eV	n	κ	ε_1	$arepsilon_2$
		At x=0,		
$E_{CPE}=1.8398$	2.9776	0	8.8660	0
2	3.087	0.171	9.501	1.055
2.5	3.593	0.165	12.881	1.185
3	3.799	1.106	13.213	8.401
3.5	3.313	1.435	8.915	9.509
4	3.443	1.412	9.859	9.726
4.5	3.750	2.303	8.757	17.269
5	2.322	3.338	- 5.753	15.501
5.5	1.272	2.423	-4.253	6.164
6	1.347	1.845	-1.590	4.969
1022	1.8197	0	3.3113	0
		At x=0.5,		
$E_{CPE} = 2.2097$	2.6927	0	7.2509	0
2.5	2.913	0.032	8.485	0.186

Cong.			World Journal of Engineering Research and Technology					
3	3.231	0.513	10.177	3.315				
3.5	3.074	0.867	8.700	5.330				
4	3.203	0.970	9.321	6.215				
4.5	3.463	1.707	9.082	11.821				
5	2.385	2.602	-1.085	12.414				
5.5	1.522	1.958	-1.519	5.960				
6	1.549	1.531	0.054	4.744				
1022	1.7654	0	3.1165	0				
		At x=1,						
$E_{CPE} = 2.5796$	2.4062	0	5.7899	0				
3	2.681	0.145	7.167	0.778				
3.5	2.765	0.441	7.450	2.439				
4	2.910	0.610	8.098	3.555				
4.5	3.141	1.200	8.428	7.539				
5	2.374	1.958	1.804	9.300				
5.5	1.688	1.542	0.470	5.208				
6	1.683	1.247	1.276	4.197				
1022	1.7093	0	2.9217	0				
E in eV	n	κ	$arepsilon_1$	$arepsilon_2$				

Table 3p. In the Ga-X(x)-system, and at T=0K and N = $N_{CDp}(r_{Ga},x)$, according to the MIT, our numerical results of n, κ , ϵ_1 and ϵ_2 are obtained from Equations (21, 20, 16), respectively, and expressed as functions of E [$\geq E_{CPE}(r_{Ga},x)$] and x, noting that (i) $\kappa=0$ and $\epsilon_2=0$ at $E=E_{\texttt{CPE}}(r_{\texttt{Ga}}\texttt{x}\texttt{x}),$ and $\kappa\to 0$ and $\epsilon_2\to 0~$ as $E\to \infty.$

	At x=0,		
	,		
3.0744	0	9.4522	0
3.192	0.175	10.158	1.117
3.703	0.170	13.684	1.262
3.905	1.126	13.979	8.795
3.407	1.454	9.496	9.907
3.538	1.426	10.481	10.093
3.846	2.321	9.403	17.856
2.407	3.361	-5.500	16.183
1.352	2.437	-4.112	6.590
1.428	1.854	-1.399	5.298
1.9099	0	3.6476	0
	3.703 3.905 3.407 3.538 3.846 2.407 1.352 1.428	3.703 0.170 3.905 1.126 3.407 1.454 3.538 1.426 3.846 2.321 2.407 3.361 1.352 2.437 1.428 1.854	3.703 0.170 13.684 3.905 1.126 13.979 3.407 1.454 9.496 3.538 1.426 10.481 3.846 2.321 9.403 2.407 3.361 -5.500 1.352 2.437 -4.112 1.428 1.854 -1.399

ISO 9001: 2015 Certified Journal 353 www.wjert.org

		At $x=0.5$,			
$E_{CPE} = 2.1929$	2.7907	0	7.7881	0	
2.5	3.026	0.036	9.156	0.216	
3	3.341	0.535	10.879	3.576	
3.5	3.172	0.889	9.269	5.643	
4	3.300	0.988	9.916	6.525	
4.5	3.562	1.732	9.689	12.340	
5	2.469	2.634	-0.843	13.005	
5.5	1.597	1.978	-1.362	6.318	
6	1.626	1.545	0.257	5.025	
1022	1.8528	0	3.4331	0	
		At $x=1$,			
$E_{CPE} = 2.5551$	2.5062	0	6.2010	0	
3	2.798	0.162	7.802	0.910	
3.5	2.868	0.465	8.012	2.667	
4	3.012	0.632	8.676	3.807	
4.5	3.245	1.231	9.013	7.988	
5	2.458	1.998	2.052	9.824	
5.5	1.761	1.568	0.639	5.523	
6	1.757	1.265	1.486	4.445	
•••					
1022	1.7940	0	3.2185	0	

Table 4n: In the X(x)-system, at E=3.2 eV and T=20 K, for given $\mathbf{r_d}$ and x, and from Equations (12, 15, 21, 20, 16), respectively, we can determine the variations of η_n (\gg 1, degenerate case), $\mathbf{E_{gn1}}$, \mathbf{n} , κ , ε_1 and ε_2 , obtained as functions of N, being represented by the arrows: \nearrow and \searrow , noting that both η_n and $\mathbf{E_{gn1}}$ increase with increasing N. One notes that, with increasing N, the variations of these optical coefficients depend on those of optical band gap, $\mathbf{E_{gn1}}$.

N (10 ¹⁸ cm	⁻³) /	15	26	60	100
			x=0		
For $\mathbf{r_d} = \mathbf{r_{Se}}$;,				
$\eta_n\gg 1$	7	145	209	366	515
$E_{\tt gn1}$ in eV	7	1.736	1.748	1.810	1.892
n	7	3.754	3.742	3.681	3.598
κ	7	1.589	1.562	1.432	1.267
ε_1	7	11.567	11.561	11.497	11.343
ε_2	>	11.931	11.690	10.540	9.121

For $\mathbf{r_d} = \mathbf{r_{Te}}$.				
$\eta_n\gg 1$		144	209	366	515
$\mathbf{E}_{\mathtt{gn1}}$ in eV	7	1.763	1.784	1.863	1.961
n	7	3.631	3.611	3.531	3.433
κ	>	1.530	1.487	1.324	1.138
$arepsilon_{ exttt{1}}$	> 1	0.843	10.828	10.718	10.490
ε_2	> 1	1.114	10.737	9.353	7.814
For $\mathbf{r_d} = \mathbf{r_{Sn}}$,				
$\eta_n\gg 1$	7	144	208.7	365.7	514.7
E _{gn1} in eV	7	1.787	1.814	1.909	2.019
n	>	3.522	3.495	3.400	3.287
κ	7	1.480	1.423	1.236	1.034
ε_1	> 1	0.214	10.188	10.034	9.740
ε_2	> 1	0.429	9.950	8.403	6.796
			0.5		
			x=0.5		
For $\mathbf{r_d} = \mathbf{r_{Se}}$,				
$\eta_n\gg 1$	7	102	149	262	369
$\mathbf{E_{gn1}}$ in eV	7	2.115	2.121	2.160	2.214
n	>	3.315	3.309	3.269	3.210
κ	٧ (0.872	0.863	0.802	0.720
ε_1	> 10	0.229	10.206	10.040	9.789
ε_2	> 5	5.780	5.710	5.245	4.625
For $\mathbf{r_d} = \mathbf{r_{Te}}$		101.6	140.2	261.2	269.2
$\eta_n \gg 1$		101.6	148.3	261.3	368.2
E _{gn1} in eV		2.137	2.148	2.199	2.265
n		3.199	3.187	3.133	3.063
κ		0.837	0.820	0.742	0.648
ε_1		9.533	9.487	9.266	8.963
ε ₂	<u>\</u> .	5.359	5.225	4.651	3.971
For $\mathbf{r_d} = \mathbf{r_{Sn}}$	 }				
$\eta_n\gg 1$	7 1	100.6	147.5	260.6	367.7
E _{gn1} in eV	7	2.156	2.172	2.234	2.308
n	\	3.096	3.079	3.013	2.933
κ	٧ (0.807	0.783	0.692	0.589

355

_						_		
$arepsilon_1$	>	8.932	8.866	8.601	8.255			
$arepsilon_2$	>	4.999	4.819	4.169	3.455			
			x=1					
For $\mathbf{r_d} = \mathbf{r_{Se}}$	₽,						 	
$\eta_n\gg 1$	7	77.32	114	202.5	286			
E _{gn1} in eV	7	2.495	2.497	2.524	2.565			
n	7	2.848	2.846	2.815	2.769			
κ	7	0.367	0.366	0.338	0.298			
ε_1	7	7.978	7.964	7.811	7.579			
$arepsilon_2$	7	2.101	2.084	1.905	1.654			
For $\mathbf{r_d} = \mathbf{r_T}$						· 		
$\eta_n \gg 1$		75.7	112.7	201.5	285.3			
E _{gn1} in eV		2.514	2.521	2.557	2.606			
n		2.737	2.729	2.688	2.632		 	
κ	۷.	0.349	0.342	0.306	0.261			
ε_1	7	7.368	7.332	7.131	6.860			
$arepsilon_2$		1.909	1.867	1.646	1.375			
For $\mathbf{r_d} = \mathbf{r_{Si}}$	n,							
$\eta_n\gg 1$	7	73.7	111	200.3	284.2			
E _{gn1} in eV	7	2.532	2.542	2.587	2.643			
n	7	2.636	2.624	2.574	2.510			
κ	7	0.331	0.321	0.279	0.230			
$arepsilon_1$	7	6.839	6.785	6.549	6.249			
ε_2	7	1.744	1.684	1.435	1.155			
N (10 ¹⁸ cm	-3) 7	1 15	26	60	100			
14 (10-2 cm	-) /	13	20	ου	100			

Cong.

World Journal of Engineering Research and Technology

Table 4p: In the X(x)-system, at E=3.2 eV and T=20 K, for given $\mathbf{r_d}$ and x, and from Equations (12, 15, 21, 20, 16), respectively, we can determine the variations of η_p (\gg 1, degenerate case), E_{gp1} , n, κ , ε_1 and ε_2 , obtained as functions of N, being represented by the arrows: \nearrow and \searrow , noting that both η_p and E_{gp1} increase with increasing N. One notes that, with increasing N, the variations of these optical coefficients depend on those of optical band gap, E_{gp1} .

N (10 ¹⁹ cm ⁻³) ↗	8	10	15	20
		x=0		

World Journal of Engineering Research and Technolog	World Jour	rnal of Eng	ineering Res	search and T	echnology
---	------------	-------------	--------------	--------------	-----------

~		_
	on	Œ
$\mathbf{}$		_

or $\mathbf{r_a} = \mathbf{r_{Ga}}$,				
$\eta_p\gg 1$	7 419	492	655	800
E _{gp1} in eV	7 1.742	1.777	1.869	1.962
n	3.843	3.809	3.717	3.623
κ	1.576	1.501	1.313	1.136
ε_{1}	12.287	12.253	12.093	11.836
ε_2	12.114	11.434	9.765	8.230
		For $\mathbf{r_a} = \mathbf{r_{Ir}}$		
$\eta_p\gg 1$	≯ 410	484	648	794
E _{gp1} in eV	7 1.796	1.838	1.944	2.049
n	3.697	3.656	3.549	3.441
κ	1.460	1.375	1.169	0.982
ε_1	1 1.537	11.475	11.230	10.879
$arepsilon_2$	1 0.796	10.052	8.301	6.759
		Eor =		
$\eta_p\gg 1$	≯ 410	For $\mathbf{r_a} = \mathbf{r_0}$: d , 648	793.6
E _{gp1} in eV	7 1.798	1.840	1.946	2.052
n	3.692	3.651	3.544	3.436
κ	1.456	1.371	1.165	0.977
$arepsilon_1$	11.513	11.450	11.202	10.848
ε_2	1 0.757	10.011	8.258	6.716
		0.7		
		x=0.5		
For $\mathbf{r_a} = \mathbf{r_{Ga}}$	1,			
$\eta_p\gg 1$	№ 259	315	437	544
E _{gp1} in eV	2 .086	2.108	2.171	2.236
n	▶ 3.438	3.415	3.349	3.280
κ	▶ 0.920	0.883	0.785	0.689
ε_1	1 0.975	10.880	10.600	10.283
ε_2	▶ 6.327	6.033	5.261	4.521
		For $\mathbf{r_a} = \mathbf{r_{Ir}}$		
$\eta_p\gg 1$	> 237	295	420	529
E _{gp1} in eV	2.122	2.148	2.221	2.294
n	3.311	3.283	3.207	3.128
	- 5.511	5.205	5.201	5.120

κ	7	0.862	0.819	0.711	0.608		
ε_1	7	10.222	10.107	9.778	9.413		
ε_2	7	5.706	5.381	4.561	3.806		
			E				
n × 1	71	236	For $\mathbf{r_a} = \mathbf{r_{Cd}}$,	420	528.6		
η _p ≫ 1 E _{gp1} in eV		2.123	2.150	2.222	2.296		
n		3.307	3.279	3.202	3.123		
κ -	,	0.860	0.818	0.709	0.606		
ε_1		10.198	10.083	9.752	9.386		
$arepsilon_2$	7	5.688	5.362	4.540	3.785		
=1						 	
For $\mathbf{r_a} = \mathbf{r_{Ga}}$							
$\eta_p \gg 1$	7	116	171	279	370		
E _{gp1} in eV	7	2.437	2.446	2.488	2.536		
n	7	3.002	2.992	2.946	2.891		
κ	7	0.432	0.422	0.376	0.326		
ε_1	7	8.828	8.776	8.536	8.251		
ε_2	7	2.594	2.524	2.216	1.887		
			Forr - r				
$\eta_p\gg 1$	7	48	For $\mathbf{r_a} = \mathbf{r_{In}}$,	241	337		
E _{gp1} in eV	Š	2.480	2.474 🖊	2.519	2.574		
	7	2.868	2.874	2.824	2.762		
n	7	0.385	0.390	0.344	0.291		
K S.	7	8.078	8.108	7.859	7.547		
ε_1 ε_2	7	2.207	2.244	1.944	1.607		
		2.207	2,244	1.744			
			For $\mathbf{r_a} = \mathbf{r_{Cd}}$,				
$\eta_p\gg 1$	7	44	117	240	336.2		
E _{gp1} in eV	7	2.482	2.475 🖊	2.519	2.575		
n	7	2.862	2.870 🔪	2.821	2.758		
κ	7	0.382	0.389	0.343	0.290		
ε_1	7	8.047	8.087	7.839	7.525		
	7	2.186	2.235	1.937	1.599		
ε_2	•						

World Journal of Engineering Research and Technology

Cong.

Table 5n. In the X(x)-system, at E=3.2 eV and N = 10^{20} cm⁻³, for given r_d and x, and from Equations (12, 15, 21, 20, 16), respectively, we can determine the variations of η_n (\gg 1, degenerate case), E_{gn1} , n, κ , ε_1 and ε_2 , obtained as functions of T, being represented by the arrows: \nearrow and \searrow , noting that both η_n and E_{gn1} decrease with increasing T. One notes that, with increasing T, the variations of these optical coefficients depend on those of optical band gap, E_{gn1} .

7	20	50	100	300
		x=0		
,				
	515	206	103	34
7	1.892	1.888	1.876	1.796
7	3.598	3.603	3.615	3.694
7	1.267	1.276	1.300	1.460
7	11.343	11.353	11.381	11.516
7	9.121	9.193	9.402	10.792
		205.9	103	34.3
7	1.961	1.957	1.944	1.865
7	3.433	3.437	3.450	3.530
7	1.138	1.146	1.169	1.321
7	10.490	10.502	10.537	10.716
7	7.814	7.879	8.068	9.331
· >				
	514.7	205.9	102.9	34.29
7	2.019	2.015	2.002	1.923
7	3.287	3.292	3.305	3.386
7	1.034	1.041	1.063	1.209
7	9.740	9.753	9.792	10.003
7	6.796	6.856	7.029	8.186
		x=0.5	5	
	369	147	74	24.5
7				2.131
7			3 227	3.298
7	0.648	0.726	0.743	0.867
		515 1.892 3.598 1.267 11.343 9.121 514.9 1.961 3.433 1.138 10.490 7.814 514.7 2.019 3.287 1.034 9.740 6.796	x=0 , 515 206 1.892 1.888 7 3.598 3.603 1.267 1.276 11.343 11.353 9.121 9.193 514.9 205.9 1.961 1.957 7 3.433 3.437 7 1.138 1.146 7 10.490 10.502 7 7.814 7.879 514.7 205.9 2.019 2.015 7 3.287 3.292 7 1.034 1.041 7 9.740 9.753 7 6.796 6.856 x=0.4 x=0.4	x=0 x

$arepsilon_1$	7	8.963	9.809	9.863	10.163		
ε_2	7	3.971	4.672	4.800	5.586		
For $\mathbf{r_d} = \mathbf{r_T}$	e [,]					- - -	
$\eta_n\gg 1$	7	368.2	147	73.6	24.5		
E _{gn1} in eV	>	2.265	2.261	2.249	2.182		
n	7	3.063	3.068	3.080	3.152		
κ	7	0.648	0.654	0.670	0.768		
ε_1	7	8.963	8.984	9.038	9.344		
ε_2	7	3.971	4.014	4.130	4.845		
For $\mathbf{r_d} = \mathbf{r_{Si}}$	n,					- -	
$\eta_n\gg 1$		368.2	147	73.6	24.5		
E _{gn1} in eV	7	2.265	2.261	2.249	2.182		
n	7	3.062	3.068	3.080	3.152		
κ	7	0.648	0.654	0.670	0.768		
$arepsilon_1$	7	8.963	8.984	9.038	9.344		
ε_2	7	3.971	4.014	4.130	4.845		
			x=1				
For $\mathbf{r_d} = \mathbf{r_{Se}}$							
$\eta_n \gg 1$			114		19		
E _{gn1} in eV			2.561	2.550	2.495		
n	7	2.769	2.774	2.786	2.848		
κ	7	0.298	0.303	0.313	0.368		
ε_1	7	7.579	7.603	7.663	7.975		
ε ₂	<i>,</i>	1.654	1.679	1.742	2.097		
For $\mathbf{r_d} = \mathbf{r_T}$	e,						
$\eta_n\gg 1$	7	285.3	114	57	19		
E _{gn1} in eV	7	2.606	2.602	2.592	2.536		
n	7	2.632	2.637	2.649	2.711		
κ	7	0.261	0.265	0.274	0.326		
ε_1	7	6.860	6.884	6.942	7.246		
ε_2	7	1.375	1.397	1.453	1.770		
For $\mathbf{r_d} = \mathbf{r_{Si}}$	1,						

World Journal of Engineering Research and Technology

Cong.

E _{gn1} in eV	>	2.643	2.638	2.628	2.573
n	7	2.510	2.515	2.527	2.590
κ	7	0.230	0.234	0.242	0.292
ε_1	7	6.249	6.272	6.328	6.623
$arepsilon_2$	7	1.155	1.176	1.226	1.511
T in K	7	20	50	100	300

Table 5p. In the X(x)-system, at E=3.2 eV and N = 10^{20} cm⁻³, for given $\mathbf{r_a}$ and x, and from Equations (12, 15, 21, 20, 16), respectively, we can determine the variations of η_p ($\gg 1$, degenerate case), $\mathbf{E_{gp1}}$, n, κ , ε_1 and ε_2 , obtained as functions of T, being represented by the arrows: \nearrow and \searrow , noting that both η_p and $\mathbf{E_{gp1}}$ decrease with increasing T. One notes that, with increasing T, the variations of these optical coefficients depend on those of optical band gap, $\mathbf{E_{gp1}}$.

T in K	7	20	50	100	300
			x=0		
For $\mathbf{r_a} = \mathbf{r_{Ga}}$	ı,				
$\eta_p\gg 1$	7	492	197	98	33
$E_{\tt gp1}$ in eV	7	1.777	1.773	1.760	1.681
n	7	3.809	3.813	3.825	3.903
κ	7	1.501	1.510	1.537	1.711
ε_1	7	12.253	12.258	12.271	12.304
ε_2	7	11.434	11.517	11.758	13.354
For $\mathbf{r_a} = \mathbf{r_{In}}$,				
$\eta_p\gg 1$	7	484	194	97	32
$\mathbf{E_{gp1}}$ in eV	7	1.838	1.834	1.821	1.742
n	7	3.656	3.660	3.673	3.751
κ	7	1.375	1.384	1.409	1.576
ε_{1}	7	11.475	11.483	11.503	11.586
$arepsilon_2$	7	10.052	10.128	10.350	11.822
For $\mathbf{r_a} = \mathbf{r_{Cd}}$	 I>				
	V	484	193.6	96.8	32.2
E _{gp1} in eV		1.840	1.836	1.823	1.744
n	7	3.651	3.655	3.668	3.746
κ	7	1.371	1.380	1.405	1.572
ε_1	_	11.450	11.458	11.478	11.563

Cong.				World	l Journal	of Engineer	ing Resear	ch an
ε_2	7	10.011	10.087	10.3080	11.776			
			x=0.5					
For $\mathbf{r_a} = \mathbf{r_G}$	a,							
$\eta_p \gg 1$	7	315	126	63	21			
E _{gp1} in eV	7	2.108	2.104	2.092	2.025			
n	7	3.415	3.419	3.431	3.501			
κ	7	0.883	0.890	0.909	1.023			
ε_1	7	10.880	10.899	10.948	11.212			
ε_2	7	6.033	6.089	6.240	7.165			
For $\mathbf{r_a} = \mathbf{r_{In}}$								
	7	295	118	59	20			
E _{gp1} in eV	7	2.148	2.144	2.133	2.065			
n	7	3.283	3.288	3.300	3.370			
κ	7	0.819	0.826	0.844	0.954			
ε_1	7	10.107	10.126	10.176	10.448			
ε_2	7	5.381	5.433	5.573	6.435			
For $\mathbf{r_a} = \mathbf{r_{Co}}$	d,							
$\eta_p\gg 1$	>	294	117.6	58.8	19.6			
E _{gp1} in eV	>	2.150	2.145	2.134	2.066			
n	7	3.279	3.284	3.296	3.366			
κ	7	0.818	0.824	0.842	0.952			
ε_1	7	10.083	10.102	10.152	10.424			
ε_2	7	5.362	5.411	5.554	6.413			
			x=1					
For $\mathbf{r_a} = \mathbf{r_G}$	a,							
$\eta_p\gg 1$	7	171	68	34	11			
E _{gp1} in eV	>	2.446	2.441	2.431	2.375			
n	7	2.992	2.997	3.009	3.070			
κ	7	0.422	0.426	0.438	0.506			
ε_1	7	8.776	8.801	8.861	9.173			
ε_2	7	2.524	2.556	2.639	3.099			
For $\mathbf{r_a} = \mathbf{r_{In}}$	12							

 $\eta_p\gg 1$

Cong. World Journal of Engineering Research and Technology
--

2.470	2.459	2.403
2.879		
	2.891	2.953
0.395	0.407	0.471
8.132	8.191	8.500
2.275	2.351	2.784
47	23	7.72
2.471	2.460	2.403
2.875	2.887	2.950
0.394	0.406	0.470
8.111	8.170	8.479
2.266	2.343	2.774
50	100	300
	8.132 2.275 47 2.471 2.875 0.394 8.111 2.266	8.132 8.191 2.275 2.351 47 23 2.471 2.460 2.875 2.887 0.394 0.406 8.111 8.170 2.266 2.343