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OPTICAL, ELECTRICAL AND THERMOELECTRIC LAWS IN n(p)-TYPE
DEGENERATE "COMPENSATED" InP(1-x)As(x)-CRYSTALLINE ALLOY,
ENHACED BY: OPTICO-ELECTRICAL -AND- ELECTRO-OPTICAL
PHENOMENA, AND OUR STATIC DIELECTRIC CONSTANT, ACCURATE
FERMI ENERGY AND CONDUCTIVITY MODELS. (I)

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ABSTRACT

In degenerate $\mathbf{n}^+(\mathbf{p}^+) - \mathbf{p}(\mathbf{n}) - \mathbf{InP_{1-x}As_x}$ - crystalline alloy, $0 \le x \le 1$, various optical, electrical and thermoelectric laws, relations, and coefficients, enhanced by: the optico-electrical phenomenon (O-EP) and the electro-optical phenomenon (E-OP), and our static dielectric constant law given in Equations (1a, 1b), accurate Fermi energy expression in Eq. (11), and conductivity model in Eq. (18), are now investigated, by basing on the same physical model and mathematical treatment method, as those used in our recent works. One notes that, for x=0, this crystalline alloy is reduced to the n(p)-type degenerate \mathbf{InP} -crystal. Some concluding remarks are given as follows. By basing on our optical [electrical] conductivity models, $\sigma_{O[E]}$, given in Eq. (18), all the optical, electrical, thermoelectric coefficients have been determined, as those given in Equations (19a-19d, 20a-20d, 21-31). In particular, for the physical conditions, as those given in Eq. (15), one remarks that the optical conductivity, σ_{O} ,

obtained from the O-EP, has a same form with that of the electrical conductivity, given from the E-OP, σ_E , as those determined in Eq. (20a), but $\sigma_0 > \sigma_E$ since $m_r(x) < m_{c(v)}(x)$, $m_{c(v)}$ and m_r , being the unperturbed reduced effective electron (hole) mass in conduction (valence)

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bands and the relative carrier mass, respectively. Finally, the numerical results of such optical, electrical and thermoelectric coefficients, calculated by using Equations (18, 19a-19d, 20a-20d, 21-31), are reported in Tables 3-10, suggesting the new ones.

KEYWORDS: Optical-and-electrical conductivity, Seebeck coefficient, Figure of merit), First Van-Cong coefficient, Second Van-Cong coefficient, Thomson coefficient, Peltier coefficient.

INTRODUCTION

In the $\mathbf{n}^+(\mathbf{p}^+) - \mathbf{InP_{1-x}As_x}$ -crystalline alloy, $0 \le x \le 1$, x being the concentration, the optical, electrical and thermoelectric coefficients, enhanced by: (i) the optico-electrical phenomenon (O-EP) and the electro-optical phenomenon (E-OP), (ii) our static dielectric constant law, $\varepsilon(r_{d(a)},x)$, $r_{d(a)}$ being the donor (acceptor) d(a)-radius, given in Equations (1a, 1b), (iii) our accurate reduced Fermi energy, $\xi_{n(p)}$, given in Eq. (11), accurate with a precision of the order of 2.11×10^{-4} [9], affecting all the expressions of optical, electrical and thermoelectric coefficients, and (iv) our optical-and-electrical conductivity models, given in Eq. (18, 20a), are now investigated by basing on our physical model and Fermi-Dirac distribution function, as those given in our recent works. [1-5] It should be noted here that for x=0, the present obtained numerical results are reduced to those given in the n(p)-type degenerate \mathbf{InP} -crystal. [6-16]

Then, some important remarks can be reported as follows.

- (1) As observed in Equations (3, 5, 6a, 6b), the critical impurity density $N_{CDn(CDp)}$, defined by the generalized Mott criterium in the metal-insulator transition (MIT), is just the density of electrons (holes), localized in the exponential conduction (valence)-band tail (EBT), $N_{CDn(CDp)}^{EBT}$, being obtained with a precision of the order of 2.77 \times 10⁻⁷, as given in our recent work. Therefore, the effective electron (hole)-density can be defined as: $N^* \equiv N N_{CDn(CDp)} \simeq N N_{CDn(CDp)}^{EBT}$, N being the total impurity density, as that observed in the compensated crystals.
- (2) The ratio of the inverse effective screening length $k_{sn(sp)}$ to Fermi wave number $k_{Fn(kp)}$ at 0 K, $R_{sn(sp)}(N^*)$, defined in Eq. (7), is valid at any N^* .

- (3) For given $[N, r_{d(a)}, x, T]$, the coefficients: $\sigma_{O[E]}(E)$, $\kappa_{O[E]}(E)$, $\varepsilon_{O[E]}(E)$, and $\alpha_{O[E]}(E)$, are determined in Equations (18, 19b-19d), as functions of the photon energy E, and then their numerical results are reported in Tables 3-8, being new ones.
- (4) Finally, for particular physical conditions, as those given in Eq. (15), one observes that the optical conductivity σ_0 has a same form with that of the electrical conductivity, σ_E , as those given in Eq. (20a), but $\sigma_0 > \sigma_E$ since $m_r(x) < m_{c(v)}(x)$, $m_{c(v)}$ and m_r , being the unperturbed reduced effective electron (hole) mass in conduction (valence) bands and the relative carrier mass, respectively. Then, by basing on those $\sigma_{O[E]}$ -expressions, the thermoelectric laws, relations, and coefficients are determined in Equations (21-31), and their numerical results are reported in Tables 9 and 10, being new ones.

In the following, various Sections are presented in order to investigate the optical, electrical and thermoelectric coefficients, given in the degenerate $n^+(p^+) - InP_{1-x} As_{x^-}$ crystalline alloy.

OUR STATIC DIELECTRIC CONSTANT LAW AND GENERALIZED MOTT CRITERIUM IN THE METAL-INSULATOR TRANSITION

First of all, in the degenerate $n^+(p^+) - \text{In}P_{1-x} \, \text{As}_x$ - crystalline alloy, at T=0 K^[1-5], we denote: the donor (acceptor) d(a)-radius by $r_{d(a)}$, the corresponding intrinsic one by: $r_{do(ao)} = r_{P(In)}$, respectively, the effective averaged numbers of equivalent conduction (valence)-bands by: $g_{c(v)}$, the unperturbed reduced effective electron (hole) mass in conduction (valence) bands by $m_{c(v)}(x)/m_o$, m_o being the free electron mass, the relative carrier mass by: $m_r(x) \equiv \frac{m_c(x) \times m_v(x)}{m_c(x) + m_v(x)} < m_{c(v)}(x)$ for given x, the unperturbed static dielectric constant by: $\epsilon_o(x)$, and the intrinsic band gap by: $E_{go}(x)$, as those given in **Table 1**, **reported in Appendix 1**.

Here, the effective carrier mass $m_{n(p)}^*(x)$ is equal to $m_{c(v)}(x)$. Therefore, we can define the effective donor (acceptor)-ionization energy in absolute values as:

$$\begin{split} E_{do(ao)}(x) &= \frac{13600 \times [m_{c(v)}(x)/m_o]}{[\epsilon_o(x)]^2} \text{ meV , and then, the isothermal bulk modulus, by:} \\ B_{do(ao)}(x) &\equiv \frac{E_{do(ao)}(x)}{\left(\frac{4\pi}{3}\right) \times \left(r_{do(ao)}\right)^3} \,. \end{split}$$

Our Static Dielectric Constant Law $\left[m_{n(p)}^*(x) \equiv m_{c(v)}(x)\right]$

Here, the changes in all the energy-band-structure parameters, expressed in terms of the effective dielectric constant $\varepsilon(r_{d(a)}, x)$, are developed as follows.

At $r_{d(a)} = r_{do(ao)}$, the needed boundary conditions are found to be, for the impurity-atom volumes: $V = (4\pi/3) \times (r_{d(a)})^3$ and $V_{do(ao)} = (4\pi/3) \times (r_{do(ao)})^3$, according to the pressures: $p, p_o = 0$, and to the deformation potential energies (or the strain energies): α , $\alpha_o = 0$. Further, the two important equations, used to determine the α -variation, $\Delta \alpha \equiv \alpha - \alpha_o = \alpha$, are defined by: $\frac{dp}{dV} = \frac{B_{do(ao)}(x)}{V}$ and $p = -\frac{d\alpha}{dV}$, giving rise to: $\frac{d}{dV}(\frac{d\alpha}{dV}) = \frac{B_{do(ao)}(x)}{V}$. Then, by an integration, one gets:

$$\begin{split} \left[\Delta\alpha(r_{d(a)},x)\right]_{n(p)} &= B_{do(ao)}(x) \times (V - V_{do(ao)}) \times \text{ ln } \left(\frac{V}{V_{do(ao)}}\right) = E_{do(ao)}(x) \times \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \\ &\ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 \geq 0. \end{split}$$

Furthermore, we also showed that, as $r_{d(a)} > r_{do(ao)}$ ($r_{d(a)} < r_{do(ao)}$), the compression (dilatation) gives rise to the increase (the decrease) in the energy gap $E_{gn(gp)}(r_{d(a)},x)$, and the effective donor (acceptor)-ionization energy $E_{d(a)}(r_{d(a)},x)$ in absolute values, obtained in the effective Bohr model, which is represented respectively by : $\pm \left[\Delta \alpha(r_{d(a)},x) \right]_{n(n)}$,

$$\begin{split} E_{gn(gp)}(r_{d(a)}, x) - E_{go}(x) &= E_{d(a)}(r_{d(a)}, x) - E_{do(ao)}(x) = E_{do(ao)}(x) \times \left[\left(\frac{\epsilon_o(x)}{\epsilon(r_{d(a)})} \right)^2 - 1 \right] = \\ &+ \left[\Delta \alpha(r_{d(a)}, x) \right]_{n(p)}, \end{split}$$

 $\text{ for } r_{d(a)} \geq r_{do(ao)}, \text{ and for } r_{d(a)} \leq r_{do(ao)},$

$$E_{gn(gp)}(r_{d(a)},x) - E_{go}(x) = E_{d(a)}(r_{d(a)},x) - E_{do(ao)}(x) = E_{do(ao)}(x) \times \left[\left(\frac{\epsilon_o(x)}{\epsilon(r_{d(a)})} \right)^2 - 1 \right] = - \left[\Delta \alpha(r_{d(a)},x) \right]_{n(p)} + \left[\frac{\epsilon_o(x)}{\epsilon(r_{d(a)})} \right]_{n(p)} + \left[\frac{\epsilon_o(x)}{\epsilon$$

Therefore, one obtains the expressions for relative dielectric constant $\epsilon(r_{d(a)}, x)$ and energy band gap $E_{gn(gp)}(r_{d(a)}, x)$, as:

$$\text{(i)-for } r_{d(a)} \geq r_{do(ao)}, \quad \text{since } \epsilon(r_{d(a)}, x) = \frac{\epsilon_o(x)}{\sqrt{1 + \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3}} \leq \epsilon_o(x), \text{ being a new}$$

 $\varepsilon(\mathbf{r}_{\mathbf{d}(\mathbf{a})},\mathbf{x})$ -law,

$$E_{gn(gp)}\big(r_{d(a)},x\big) - E_{go}(x) = E_{d(a)}\big(r_{d(a)},x\big) - E_{do(ao)}(x) = E_{do(ao)}(x) \times \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 \geq 0, \tag{1a}$$

according to the increase in both $E_{gn(gp)}(r_{d(a)},x)$ and $E_{d(a)}(r_{d(a)},x)$, with increasing $r_{d(a)}$ and for a given x, and

$$(\textbf{ii)-} \text{for } r_{d(a)} \leq r_{do(ao)} \text{ , since } \epsilon(r_{d(a)},x) = \frac{\epsilon_o(x)}{\sqrt{1 - \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3}} \geq \epsilon_o(x) \text{ , with } a$$

 $\text{condition, given by: } \left[\left(\frac{r_{d(a)}}{r_{do(ao)}} \right)^3 - 1 \right] \times \ln \left(\frac{r_{d(a)}}{r_{do(ao)}} \right)^3 < 1, \text{ being a new } \epsilon(r_{d(a)}, x) \text{-law,}$

$$E_{gn(gp)}\big(r_{d(a)},x\big) - E_{go}(x) = E_{d(a)}\big(r_{d(a)},x\big) - E_{do(ao)}(x) = -E_{do(ao)}(x) \\ \times \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \\ \times \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 \leq 0, \tag{1b}$$

corresponding to the decrease in both $E_{gn(gp)}(r_{d(a)},x)$ and $E_{d(a)}(r_{d(a)},x)$, with decreasing $r_{d(a)}$ and for a given x.

It should be noted that, in the following, all the optical, electrical and thermoelectric properties strongly depend on this **new** $\varepsilon(\mathbf{r}_{d(a)}, \mathbf{x})$ -law.

Furthermore, the effective Bohr radius $a_{Bn(Bp)}(r_{d(a)}, x)$ is defined by:

$$a_{\text{Bn(Bp)}}(r_{\text{d(a)}}, x) \equiv \frac{\varepsilon(r_{\text{d(a)}}, x) \times \hbar^2}{m_{\text{n(p)}}^*(x) \times m_0 \times q^2} = 0.53 \times 10^{-8} \text{ cm} \times \frac{\varepsilon(r_{\text{d(a)}}, x)}{m_{\text{n(p)}}^*(x)}.$$
 (2)

Generalized Mott Criterium in the MIT $\left[m_{n(p)}^*(x) \equiv m_{c(v)}(x)\right]$

Now, it is interesting to remark that the critical total donor (acceptor)-density in the MIT at T=0 K, $N_{CDn(NDp)}(r_{d(a)}, x)$, was given by the Mott's criterium, with an empirical parameter, $M_{n(p)}$, as^[3]:

$$N_{CDn(CDp)}(r_{d(a)}, x)^{1/3} \times a_{Bn(Bp)}(r_{d(a)}, x) = M_{n(p)}, M_{n(p)} = 0.25,$$
depending thus on our **new** $\varepsilon(\mathbf{r_{d(a)}}, \mathbf{x})$ -law.

This excellent one can be explained from the definition of the reduced effective Wigner-Seitz (WS) radius $r_{sn(sp),M}$, in the Mott's criterium, being characteristic of interactions, by:

$$r_{sn(sp),M}(N = N_{CDn(CDp)}(r_{d(a)}, x), r_{d(a)}, x) \equiv \left(\frac{3}{4\pi N_{CDn(CDp)}(r_{d(a)}, x)}\right)^{\frac{1}{3}} \times \frac{1}{a_{Bn(Bp)}(r_{d(a)}, x)} = 2.4813963, \quad (4)$$

for any $(r_{d(a)}, x)$ -values. Then, from Eq. (4), one also has:

$$N_{CDn(CDp)}(r_{d(a)}, x)^{1/3} \times a_{Bn(Bp)}(r_{d(a)}, x) = \left(\frac{3}{4\pi}\right)^{\frac{1}{3}} \times \frac{1}{2.4813963} = 0.25 = M_{n(p)},$$
 (5)

explaining thus the existence of the Mott's criterium.

Furthermore, by using $M_{n(p)}=0.25$, according to the empirical Heisenberg parameter $\mathcal{H}_{n(p)}=0.47137$, as those given in our previous work^[3], we have also showed that $N_{CDn(CDp)}$ is just the density of electrons (holes) localized in the exponential conduction (valence)-band tail , $N_{CDn(CDp)}^{EBT}$, with a precision of the order of 2.77×10^{-7} , respectively .^[3] So,

$$N_{\text{CDn(NDp)}}(r_{\text{d(a)}}, x) \cong N_{\text{CDn(CDp)}}^{\text{EBT}}(r_{\text{d(a)}}, x). \tag{6a}$$

It shoud be noted that the values of $M_{n(p)}$ and $\mathcal{H}_{n(p)}$ could be chosen so that those of $N_{CDn(CDp)}$ and $N_{CDn(CDp)}^{EBT}$ are found to be in good agreement with their experimental results.

Therefore, the effective density of electrons (holes) given in parabolic conduction (valence) bands, N^* , can be defined, as that given in compensated materials:

$$N^{*}(N, r_{d(a)}, x) \equiv N - N_{CDn(NDp)}(r_{d(a)}, x) \cong N - N_{CDn(CDp)}^{EBT}(r_{d(a)}, x).$$
(6b)

In summary, as observed in our previous paper [3], for a given x and an increasing $r_{d(a)}$, $\epsilon(r_{d(a)},x)$ decreases, while $E_{gno(gpo)}(r_{d(a)},x)$, $N_{CDn(NDp)}(r_{d(a)},x)$ and $N_{CDn(CDp)}^{EBT}(r_{d(a)},x)$ increase, affecting strongly all the optical, electrical, and thermoelectric coefficients, as those observed in following Sections.

PHYSICAL MODEL

In the degenerate $n^+(p^+) - \text{InP}_{1-x} \, \text{As}_x$ -crystalline alloy, the reduced effective Wigner-Seitz (WS) radius $r_{sn(sp)}$, characteristic of interactions, being given in Eq. (4), in which N is replaced by N*, is now defined by: $\gamma \times r_{sn(sp)} \left(N^*, r_{d(a)}, x\right) \equiv \frac{k_{Fn(Fp)}^{-1}}{\alpha_{Bn(Bp)}} < 1$, $r_{sn(sp)} \left(N^*, r_{d(a)}, x\right) \equiv \left(\frac{3g_{c(v)}}{4\pi N^*}\right)^{1/3} \times \frac{1}{\alpha_{Bn(Bp)}(r_{d(a)}, x)}$, being proportional to $N^{*-1/3}$. Here, $\gamma = (4/9\pi)^{1/3}$, $k_{Fn(Fp)}(N^*) \equiv \left(\frac{3\pi^2 N^*}{g_{c(v)}}\right)^{\frac{1}{3}}$ is the Fermi wave.

Then, the ratio of the inverse effective screening length $k_{sn(sp)}$ to Fermi wave number $k_{Fn(kp)}$

is defined by:
$$R_{sn(sp)}(N^*) \equiv \frac{k_{sn(sp)}}{k_{Fn(Fp)}} = \frac{k_{Fn(Fp)}^{-1}}{k_{sn(sp)}^{-1}} = R_{snWS(spWS)} + \left[R_{snTF(spTF)} - R_{snWS(spWS)}\right]e^{-r_{sn(sp)}} < 1,$$
 (7)

being valid at any N*.

Here, these ratios, R_{snTF(spTF)} and R_{snWS(spWS)}, can be determined as follows.

First, for $N \gg N_{CDn(NDp)}(r_{d(a)},x)$, according to the **Thomas-Fermi** (**TF**)-**approximation**, the ratio $R_{snTF(spTF)}(N^*)$ is reduced to

$$R_{snTF(spTF)}(N^*) \equiv \frac{k_{snTF(spTF)}}{k_{Fn(Fp)}} = \frac{k_{Fn(Fp)}^{-1}}{k_{snTF(spTF)}^{-1}} = \sqrt{\frac{4\gamma r_{sn(sp)}}{\pi}} \ll 1,$$
 (8)

being proportional to $N^{*-1/6}$.

Secondly, for $N \ll N_{CDn(NDp)}(r_{d(a)})$, according to the Wigner-Seitz (WS)-approximation, the ratio $R_{snWS(snWS)}$ is respectively reduced to

$$R_{sn(sp)WS}(N^*) \equiv \frac{k_{sn(sp)WS}}{k_{Fn}} = 0.5 \times \left(\frac{3}{2\pi} - \gamma \frac{d[r_{sn(sp)}^2 \times E_{CE}(N^*)]}{dr_{sn(sp)}} \right), \tag{9a}$$

Where $E_{CE}(N^*)$ is the majority-carrier correlation energy (CE), being determined by:

$$E_{CE}(N^*) = \frac{_{-0.87553}}{_{0.0908+r_{sn(sp)}}} + \frac{\frac{_{0.87553}}{_{0.0908+r_{sn(sp)}}} + \left(\frac{_{2[1-\ln(2)]}}{\pi^2}\right) \times \ln(r_{sn(sp)}) - 0.093288}{_{1+0.03847728\times r_{sn(sp)}^{1.67378876}}} \,.$$

Furthermore, in the highly degenerate case, the physical conditions are found to be given by:

$$\frac{k_{Fn(Fp)}^{-1}}{a_{Bn(Bp)}} < \frac{\eta_{n(p)}}{E_{Fno(Fpo)}} \equiv \frac{1}{A_{n(p)}} < \frac{k_{Fn(Fp)}^{-1}}{k_{sn(sp)}^{-1}} \equiv R_{sn(sp)} < 1, \ \eta_{n(p)}(N^*) \equiv \frac{\sqrt{2\pi \times (\frac{N^*}{g_{c(v)}})}}{\epsilon(r_{d(a)})} \times q^2 k_{sn(sp)}^{-1/2}, \tag{9b}$$

Which gives:
$$A_{n(p)}(N^*) = \frac{E_{Fno(Fpo)}(N^*)}{\eta_{n(p)}(N^*)}, \ E_{Fno(Fpo)}(N^*, r_{d(a)}, x) \equiv \frac{\hbar^2 \times k_{Fn(Fp)}^2(N^*)}{2 \times m_{n(p)}^*(x) \times m_o}.$$

BAND GAP NARROWING (BGN)

First, the BGN is found to be given by:

$$\Delta E_{gn(gp)}(N^*, r_{d(a)}, x) \simeq a_1 + \frac{\varepsilon_0(x)}{\varepsilon(r_{d(a)}, x)} \times N_r^{\frac{1}{3}} + a_2 \times \frac{\varepsilon_0(x)}{\varepsilon(r_{d(a)}, x)} \times N_r^{\frac{1}{3}} \times (2.503 \times [-E_{CE}(r_{sn(sp)})] \times r_{sn(sp)}) + a_3 \times \left[\frac{\varepsilon_0(x)}{\varepsilon(r_{d(a)}, x)}\right]^{\frac{5}{4}} \times \sqrt{\frac{m_{v(c)}}{m_{n(p)}^*(x)}} \times N_r^{\frac{1}{4}} + 2a_4 \times \left[\frac{\varepsilon_0(x)}{\varepsilon(r_{d(a)}, x)}\right]^{\frac{1}{2}} \times N_r^{\frac{1}{2}} + 2a_5 \times \left[\frac{\varepsilon_0(x)}{\varepsilon(r_{d(a)}, x)}\right]^{\frac{3}{2}} \times N_r^{\frac{1}{6}}, N_r = \frac{N^*}{9.999 \times 10^{17} \text{ cm}^{-3}},$$
 (10a)

Here, for $\Delta E_{gn;N}(N^*,r_d,x)$, one has: $a_1=3.8\times 10^{-3}(eV)$, $a_2=6.5\times 10^{-4}(eV)$, $a_3=2.8\times 10^{-3}(eV)$, $a_4=5.597\times 10^{-3}(eV)$, and $a_5=8.1\times 10^{-4}(eV)$, and for $\Delta E_{gp;N}(N^*,r_a,x)$, one has: $a_1=3.15\times 10^{-3}(eV)$, $a_2=5.41\times 10^{-4}(eV)$, $a_3=2.32\times 10^{-3}(eV)$, $a_4=4.12\times 10^{-3}(eV)$, and $a_5=9.8\times 10^{-5}(eV)$.

Therefore, at T=0 K and N* = 0, and for any x and $r_{d(a)}$, one gets: $\Delta E_{gn(gp)} = 0$, according to the metal-insulator transition (MIT).

Secondly, one has:

$$\Delta E_{gn(gp)}(T,x) = 10^{-4} T^2 \times \left[\frac{5.405 \times x}{T+204} + \frac{7.205 \times (1-x)}{T+94} \right] (eV). \tag{10b}$$

FERMI ENERGY AND FERMI-DIRAC DISTRIBUTION FUNCTION

Fermi Energy

Here, for a presentation simplicity, we change all the sign of various parameters, given in the degenerate $p^+ - InP_{1-x} As_x$ -crystalline alloy, in order to obtain the same one, as given in the degenerate $n^+ - InP_{1-x} As_x$ - crystalline alloy, according to the reduced Fermi energy $E_{Fn(Fp)}$, $\xi_{n(p)}(N^*, r_{d(a)}, x, T) \equiv \frac{E_{Fn(Fp)}(N^*, r_{d(a)}, x, T)}{k_B T} > 0 (< 0)$, obtained respectively in the degenerate (non-degenerate) case.

For any $(N^*, r_{d(a)}, x, T)$, the reduced Fermi energy $\xi_{n(p)}(N^*, r_{d(a)}, x, T)$ or the Fermi energy $E_{Fn(Fp)}(N^*, r_{d(a)}, x, T)$, obtained in our previous paper [9], obtained with a precision of the order of 2.11×10^{-4} , is found to be given by:

$$\xi_{n(p)}(u) \equiv \frac{E_{Fn(Fp)}(u)}{k_B T} = \frac{G(u) + Au^B F(u)}{1 + Au^B} \equiv \frac{V(u)}{W(u)}, A = 0.0005372 \text{ and } B = 4.82842262,$$
 (11)

Where u is the reduced electron density, $u(N^*, r_{d(a)}, x, T) \equiv \frac{N^*}{N_{c(v)}(T, x)}$

$$\begin{split} N_{c(v)}(T,x) &= 2g_{c(v)} \times \left(\frac{m_{n(p)}^*(x) \times m_0 \times k_B T}{2\pi\hbar^2}\right)^{\frac{3}{2}} \ (cm^{-3}) \quad , \quad F(u) = au^{\frac{2}{3}} \left(1 + bu^{-\frac{4}{3}} + cu^{-\frac{8}{3}}\right)^{-\frac{2}{3}}, \\ a &= \left[3\sqrt{\pi}/4\right]^{2/3}, \end{split}$$

$$b = \frac{1}{8} \left(\frac{\pi}{a}\right)^2 \quad , \ c = \frac{62.3739855}{1920} \left(\frac{\pi}{a}\right)^4 \ , \qquad \text{ and } \qquad G(u) \simeq Ln(u) + 2^{-\frac{3}{2}} \times u \times e^{-du} \ ; \quad d = 2^{3/2} \left[\frac{1}{\sqrt{27}} - \frac{3}{16}\right] > 0.$$

So, in the non-degenerate case (u \ll 1), one has: $E_{Fn(Fp)}(u) = k_BT \times G(u) \simeq k_BT \times Ln(u)$ as $\mathbf{u} \to \mathbf{0}$, the limiting non-degenerate condition, and in the very degenerate case (u \gg 1), one gets: $E_{Fn(Fp)}(u \gg 1) = k_BT \times F(u) = k_BT \times au^{\frac{2}{3}} \left(1 + bu^{-\frac{4}{3}} + cu^{-\frac{8}{3}}\right)^{-\frac{2}{3}} \simeq \frac{\hbar^2 \times k_{Fn(Fp)}^2(N^*)}{2 \times m_{n(p)}^*(x) \times m_0}$ as $\mathbf{u} \to \infty$, the limiting degenerate condition. In other words, $\xi_{n(p)} \equiv \frac{E_{Fn(Fp)}}{k_BT}$ is accurate, and it also verifies the correct limiting conditions.

In particular, as $T \to 0 \, K$, since $u^{-1} \to 0$, Eq. (11) is reduced to: $E_{Fno(Fpo)}(N^*) \equiv \frac{\hbar^2 \times k_{Fn(Fp)}^2(N^*)}{2 \times m_{n(p)}^*(x) \times m_o}$, proportional to $(N^*)^{2/3}$, noting that, for a given N^* , $E_{Fno(Fpo)} \left(m_{n(p)}^*(x) = m_r(x) \right) > E_{Fno(Fpo)} \left(m_{n(p)}^*(x) = m_{c(v)}(x) \right)$ since $m_r(x) < m_{c(v)}(x)$ for given x. Further, at $T=0 \, K$ and $N^*=0$, being the physical conditions, given for the metal-insulator transition (MIT).

In the following, it should be noted that all the optical and electrical-and-thermoelectric properties strongly depend on such the accurate expression of $\xi_{n(p)}(N^*, r_{d(a)}, x, T)$. [9]

Fermi-Dirac Distribution Function (FDDF)

The Fermi-Dirac distribution function (FDDF) is given by: $f(E) \equiv (1 + e^{\gamma})^{-1}$, $\gamma \equiv (E - E_{Fn(Fp)})/(k_BT)$.

So, the average of E^p, calculated using the FDDF-method, as developed in our previous works^[1,6] is found to be given by:

$$\langle E^p \rangle_{FDDF} \equiv G_p(E_{Fn(Fp)}) \times E_{Fn(Fp)}^p \equiv \int_{-\infty}^{\infty} E^p \times \left(-\frac{\partial f}{\partial E} \right) dE, \quad -\frac{\partial f}{\partial E} = \frac{1}{k_B T} \times \frac{e^{\gamma}}{(1+e^{\gamma})^2}.$$

Further, one notes that, at 0 K, $-\frac{\partial f}{\partial E} = \delta (E - E_{Fno(Fpo)})$, $\delta (E - E_{Fno(Fpo)})$ being the Dirac delta (δ)-function. Therefore, $G_p(E_{Fno(Fpo)}) = 1$.

Then, at low T, by a variable change $\gamma \equiv (E-E_{Fn(Fp)})/(k_BT),$ one has:

$$\begin{split} G_p\big(E_{Fn(Fp)}\big) &\equiv 1 + E_{Fn(Fp)}^{-p} \times \int_{-\infty}^{\infty} \frac{e^{\gamma}}{(1+e^{\gamma})^2} \times \big(k_B T \gamma + E_{Fn(Fp)}\big)^p d\gamma = 1 + \sum_{\mu=1,2,\dots}^p C_p^{\beta} \times \\ (k_B T)^{\beta} \times E_{Fn(Fp)}^{-\beta} \times I_{\beta}, \text{ where } C_p^{\beta} &\equiv p(p-1) \dots (p-\beta+1)/\beta! \qquad \text{ and the integral } I_{\beta} \text{ is given by:} \end{split}$$

$$\begin{split} I_{\beta} &= \int_{-\infty}^{\infty} \frac{\gamma^{\beta} \times e^{\gamma}}{(1+e^{\gamma})^{2}} \, d\gamma = \int_{-\infty}^{\infty} \frac{\gamma^{\beta}}{\left(e^{\gamma/2} + e^{-\gamma/2}\right)^{2}} \, d\gamma, \text{ vanishing for old values of } \beta. \text{ Then, for even} \\ \text{values of } \beta = 2n, \text{ with } n = 1, 2, \dots, \text{ one obtains:} \end{split}$$

$$I_{2n} = 2 \int_0^\infty \frac{\gamma^{2n} \times e^{\gamma}}{(1 + e^{\gamma})^2} d\gamma$$

Now, using an identity $(1+e^{\gamma})^{-2} \equiv \sum_{s=1}^{\infty} (-1)^{s+1} s \times e^{\gamma(s-1)}$, a variable change: $s\gamma = -t$, the Gamma function: $\int_0^{\infty} t^{2n} e^{-t} dt \equiv \Gamma(2n+1) = (2n)!$, and also the definition of the Riemann's zeta function: $\zeta(2n) \equiv 2^{2n-1} \pi^{2n} |B_{2n}|/(2n)!$, B_{2n} being the Bernoulli numbers, one finally gets: $I_{2n} = (2^{2n} - 2) \times \pi^{2n} \times |B_{2n}|$. So, from above Eq. of $\langle E^p \rangle_{FDDF}$, we get in the degenerate case the following ratio:

$$G_{p}\left(E_{Fn(Fp)}\right) \equiv \frac{\langle E^{p}\rangle_{FDDF}}{E_{Fn(Fp)}^{p}} = 1 + \sum_{n=1}^{p} \frac{p(p-1)\dots(p-2n+1)}{(2n)!} \times (2^{2n}-2) \times |B_{2n}| \times y^{2n} \equiv G_{p\geq 1}(y), \quad (12)$$

$$\text{Where } y \equiv \frac{\pi}{\xi_{n(p)}(N^*,r_{d(a)},x,T)} = \frac{\pi k_B T}{E_{Fn(Fp)}(N^*,r_{d(a)},x,T)}, \text{ noting that } G_{p=1}(y \equiv \frac{\pi k_B T}{E_{Fn(Fp)}} = \frac{\pi}{\xi_{n(p)}}) = 1 \ , \\ \text{and as } T \to 0 \ K, \ G_{p>1}(y \to 0) \to 1.$$

Then, some usual results of $G_{p\geq 1}(y)$ are given in the **Table 2**, reported in Appendix 1, being needed to determine all the following optical, electrical and thermoelectric properties.

OPTICAL-AND-ELECTRICAL PROPERTIES

Optico-Electrical Phenomenon (O-EP) and Electro-Optical Phenomenon (E-OP)

In the degenerate $n^+(p^+) - InP_{1-x} As_x$ -crystalline alloy, one has:

(i) in the **E-OP**, the reduced band gap is defined by:

$$E_{gn2(gp2)} \equiv E_{gn(gp)} - \Delta E_{gn(gp)} (N^*, r_{d(a)}, x) - \Delta E_{gn(gp)} (T, x), \tag{13}$$

Where the intrinsic band gap $E_{gn(gp)}$ is defined in Equations (1a, 1b), $\Delta E_{gn(gp)}(N^*, r_{d(a)}, x)$ and $\Delta E_{gn(gp)}(T, x)$ are respectively determined in Equations (10a, 10b), and

(ii) in the (**O-EP**), the photon energy is defined by: $E \equiv \hbar \omega$, and the optical band gap, as: $E_{gn1(gp1)} \equiv E_{gn2(gp2)} + E_{Fn(Fp)}$.

Therefore, for $E \ge E_{gn1(gp1)}(E_{gn2(gp2)})$, the effective photon energy E^* is found to be given by:

$$E^* \equiv E - E_{gn1(gp1)}(E_{gn2(gp2)}) \ge 0. \tag{14}$$

From above Equations, one notes that: $E^* \equiv [E - E_{gn1(gp1)}] = E_{Fn(Fp)}$, given in the O-EP, if $E = [E_{gn1(gp1)} + E_{Fn(Fp)}]$ and $m_{n(p)}^*(x) = m_r(x)$, and $E^* \equiv E - E_{gn2(gp2)} = E_{Fn(Fp)}$, given in the E-OP, if $E = [E_{gn2(gp2)} + E_{Fn(Fp)}]$ and $m_{n(p)}^*(x) = m_{c(v)}(x)$, noting that $E_{Fn(Fp)}(m_r(x)) > E_{Fn(Fp)}(m_{c(v)}(x))$, since $m_r(x) < m_{c(v)}(x)$, for a given x. (15)

Eq. (15) thus shows that, in both O-EP and E-OP, the Fermi energy-level penetrations into conduction (valence)-bands, observed in the $n^+(p^+)$ – type degenerate $n^+(p^+)$ – InP_{1-x} As_x -crystalline alloy, $E_{Fn(Fp)}$, are well defined.

Optical Coefficients

The optical properties for any medium, defined in the O-EP and E-OP, respectively, according to: $\left[m_{n(p)}^* \equiv m_r(x)[m_{c(v)}(x)]\right]$, can be described by the complex refraction: $\mathbb{N}_{O[E]} \equiv n_{O[E]} - i\kappa_{O[E]}$, $n_{O[E]}$ and $\kappa_{O[E]}$ being the refraction index and the extinction coefficient, the complex dielectric function: $\mathcal{E}_{O[E]} = \epsilon_{1 \ O[E]} - i\epsilon_{2 \ O[E]}$, where $i^2 = -1$, and $\mathcal{E}_{O[E]} = \mathbb{N}_{O[E]}^2$. Further, if denoting the normal-incidence reflectance and the optical absorption by $R_{O[E]}$ and $\propto_{O[E]}$, and the effective joint density of states by:

$$\begin{split} & JDOS_{n(p)\;O[E]}(E) \equiv \frac{1}{2\pi^2} \times \left(\frac{2m_{n(p)}^*(x)}{\hbar^2}\right)^{3/2} \times \left[\frac{E - E_{gn1(gp1)}(E_{gn2(gp2)})}{E - \left[E_{gn1(gp1)}(E_{gn2(gp2)}) + E_{Fn(Fp)} - E_{Fno(Fpo)}\right]}\right]^2 \times \\ & \sqrt{E_{Fno(Fpo)}}, \text{ and } F_{O[E]}(E) \equiv \frac{\hbar q^2 \times |v(E)|^2}{n_{O[E]}(E) \times cE \times \epsilon(r_{d(a)},x) \times \epsilon_{free\;space}}, \text{ one gets}^{[2]}; \end{split}$$

$$\epsilon_{1 \text{ O[E]}}(E) \equiv n_{\text{O[E]}}^{2} - \kappa_{\text{O[E]}}^{2}, \epsilon_{2 \text{ O[E]}}(E) \equiv 2\kappa_{\text{O[E]}} n_{\text{O[E]}}, \text{ and } R_{\text{O[E]}}(E) \equiv \frac{\left[n_{\text{O[E]}} - 1\right]^{2} + \kappa_{\text{O[E]}}^{2}}{\left[n_{\text{O[E]}} + 1\right]^{2} + \kappa_{\text{O[E]}}^{2}}.$$
 (16)

Here, $\epsilon_{free\,space} = 8.854187817 \times 10^{-12} \left(\frac{c^2}{N \times m^2}\right)$ is the permittivity of the free space, -q is the charge of the electron, $\left| \ v_{0[E]}(E) \right|$ is the matrix elements of the velocity operator between valence (conduction)-and-conduction (valence) bands, and our approximate expression for the refraction index $n_{0[E]}$ is found to be defined by:

$$n_{O[E]}(E, N^*, r_{d(a)}, x, T) = n_{\infty}(r_{d(a)}, x) + \sum_{i=1}^{4} \frac{X_i(E_{gn1(gp1)}) \times E + Y_i(E_{gn1(gp1)})}{E^2 - B_i E + C_i},$$
(17)

going to a constant as $E \to \infty$, since $n(E \to \infty, r_{d(a)}, x) \to n_{\infty}(r_{d(a)}, x) = \sqrt{\epsilon(r_{d(a)}, x)} \times \frac{\omega_T}{\omega_L}$, given in the well-known Lyddane-Sachs-Teller relation, in which $\omega_T \simeq 5.1 \times 10^{13} \text{ s}^{-1}$ and $\omega_L \simeq 8.9755 \times 10^{13} \text{ s}^{-1}$ are the transverse (longitudinal) optical phonon frequencies, giving rise to: $n_{\infty}(r_{d(a)}, x) \simeq \sqrt{\epsilon(r_{d(a)}, x)} \times 0.568$.

Here, the other parameters are determined by: $X_i(E_{gn1(gp1)}) = \frac{A_i}{Q_i} \times \left[-\frac{B_i^2}{2} + E_{gn1(gp1)}B_i - \frac{A_i}{Q_i} \right]$

$$\begin{split} E_{gn1(gp1)}^2 + C_i \Big] \ , \ \ Y_i \Big(E_{gn1(gp1)} \Big) = & \frac{A_i}{Q_i} \times \left[\frac{B_i \times (E_{gn1(gp1)}^2 + C_i)}{2} - 2 E_{gn1(gp1)} C_i \right] \ , \qquad Q_i = \frac{\sqrt{4 C_i - B_i^2}}{2} \ , \end{split}$$
 where, for i=(1, 2, 3, and 4),

 $A_i = 4.7314 \times 10^{-4}, \; 0.2313655, 0.1117995, 0.0116323 \quad , \quad B_i = 5.871, 6.154, 9.679 \quad , \\ 13.232, \; \text{and} \; C_i = 8.619, 9.784, 23.803, 44.119.$

Now, the optical [electrical] conductivity $\sigma_{O[E]}$ can be defined and expressed in terms of the kinetic energy of the electron (hole), $E_k \equiv \frac{\hbar^2 \times k^2}{2 \times m_{n(D)}^*(x) \times m_o}$, k being the wave number, as:

$$\sigma_{O[E]}(k) \equiv \frac{q^2 \times k}{\pi \times \hbar} \times \frac{k}{k_{sn(sp)}} \times \left[k \times a_{Bn(Bp)}\right] \times \left(\frac{E_k}{\eta_{n(p)}}\right)^{\frac{1}{2}} \left(\frac{1}{\Omega \times cm}\right), \text{ which is thus proportional to } E_k^2,$$

Where
$$\frac{q^2}{\pi \times \hbar} = 7.7480735 \times 10^{-5} \text{ ohm}^{-1}$$
.

Then, we obtain:
$$\langle E^2 \rangle_{FDDF} \equiv G_2(y = \frac{\pi k_B T}{E_{Fn(Fp)}}) \times E_{Fn(Fp)}^2$$
, and $G_2(y) = \left(1 + \frac{y^2}{3}\right) \equiv G_2(N, r_{d(a)}, x, T)$, with $y \equiv \frac{\pi}{\xi_{n(p)}}$, $\xi_{n(p)} = \xi_{n(p)}(N^*, r_{d(a)}, x, T)$ for a presentation simplicity.

Therefore, from above equations (16, 17), if denoting the function $H(N, r_{d(a)}, x, T)$ by:

$$H(N^*, r_{d(a)}, x, T) =$$

$$\left[\frac{k_{Fn(Fp)}(N^*)}{R_{sn(sp)}(N^*)} \times \left[k_{Fn(Fp)}(N^*) \times a_{Bn(Bp)} \big(r_{d(a)}, x \big) \right] \times \sqrt{A_{n(p)}(N^*)} = \frac{E_{Fno(Fpo)}(N^*)}{\eta_{n(p)}(N^*)} \right] \ \times \left[e^{-\frac{1}{2} \left(\frac{1}{2} \left$$

 $G_2(N^*, r_{d(a)}, x, T)$, where $R_{sn(sp)}(N^*) \equiv \frac{k_{sn(sp)}}{k_{Fn(Fp)}}$, being proportional to $E_{Fno(Fpo)}^2$. Then, our optical [electrical] conductivity models, defined in the O-EP and E-OP, respectively, for a simply representation, can thus be assumed to be as:

$$\begin{split} &\sigma_{0}(E,N^{*},r_{d(a)},x,T) = \\ &\frac{q^{2}}{\pi \times \hbar} \times H(N^{*},r_{d(a)},x,T) \times \left[\frac{E - E_{gn1(gp1)}}{E - \left[E_{gn1(gp1)} + E_{Fn(Fp)} - E_{Fno(Fpo)}\right]} \right]^{2} \left(\frac{1}{\Omega \times cm} \right), \text{ and } \\ &\sigma_{E}(E,N,r_{d(a)},x,T) = \\ &\frac{q^{2}}{\pi \times \hbar} \times H(N^{*},r_{d(a)},x,T) \times \left[\frac{E - E_{gn2(gp2)}}{E - \left[(E_{gn2(gp2)} + E_{Fn(Fp)} - E_{Fno(Fpo)}\right]} \right]^{2} \left(\frac{1}{\Omega \times cm} \right). \end{split}$$
(18)

It should be noted here that:

(i) $\sigma_{O[E]} \big(E = E_{gn1(gp1)}[E_{gn2(gp2)}] \big) = 0$, and $\sigma_{O[E]}(E \to \infty) \to \text{Constant}$ for given $\big(N, r_{d(a)}, x, T \big)$ -physical conditions, and

(ii) as $T \rightarrow 0$ K and $N^* = 0$ [or $E_{Fno(Fpo)}(N^*) = 0$], according to: $H(N^*, r_{d(a)}, x, T) = 0$, and for a given E, $\left[E - E_{gn1(gp1)}\right] = \left[E - E_{gn(gp)}\right]$ =Constant, then from Equations (16-18), $n_{O[E]}(E)$ = Constant, $\sigma_{O[E]}(E) = 0$, $\kappa_{O-EP[E-OP]}(E) = 0$, $\epsilon_{1 \, O[E]}(E) = (n_{\infty})^2$ = Constant, $\epsilon_2(E) = 0$, and $\alpha_{O[E]}(E) = 0$.

This result (18) should be new, in comparison with that, obtained from an improved Forouhi-Bloomer parameterization, as given in our previous work.^[2]

Using Equations (16-18), one obtains all the analytically results as:

$$\frac{|v(E)|^2}{E} =$$

$$\frac{8\pi^{2}\hbar}{(2m_{r})^{\frac{3}{2}}\times\sqrt{\eta_{n(p)}}}\times\left[\frac{k_{Fn(Fp)}(N^{*})}{R_{sn(sp)}(N^{*})}\times\left[k_{Fn(Fp)}(N^{*})\times a_{Bn(Bp)}(r_{d(a)},x)\right]\right]\times G_{2}(N^{*},r_{d(a)},x,T),\eqno(19a)$$

$$\kappa_0(E) = \frac{2q^2}{\frac{1}{n(E) \times \epsilon(r_{d(a)}, x) \times \epsilon_{free \, snace} \times E}} \times H(N^*, r_{d(a)}, x, T) \times \frac{1}{n(E) \times \epsilon(r_{d(a)}, x) \times \epsilon_{free \, snace} \times E}$$

$$\left[\frac{E-E_{gn1(gp1)}}{E-\left[E_{gn1(gp1)}+E_{Fn(Fp)}-E_{Fno(Fpo)}\right]}\right]^2 \quad \text{ and } \quad$$

$$\kappa_{\rm E}(\rm E) = \frac{2q^2}{n(\rm E)\times\epsilon(r_{\rm d(a)},x)\times\epsilon_{\rm free\ space}\times\rm E} \times H(\rm N^*,r_{\rm d(a)},x,T) \times \left[\frac{\rm E-E_{\rm gn2(gp2)}}{\rm E-[(E_{\rm gn2(gp2)}+E_{\rm Fn(Fp)}-E_{\rm Fno(Fpo)}]}\right]^2, \eqno(19b)$$

Which gives: $\kappa_{O[E]}(E = E_{gn1(gp1)}[E_{gn2(gp2)}]) = 0$, and $\kappa_{O[E]}(E \to \infty) \to 0$, as those given in Ref.^[2],

$$\epsilon_{2\;0}(E) = \frac{4q^2}{\epsilon(r_{d(a)},x) \times \epsilon_{free\;space} \times E} \times \left. H\left(N^*,r_{d(a)},x,T\right) \times \left[\frac{E - E_{gn1(gp1)}}{E - \left[E_{gn1(gp1)} + E_{Fn(Fp)} - E_{Fno(Fpo)}\right]}\right]^2 \; and \; e^{-\frac{1}{2}} \left. \frac{1}{\epsilon(r_{d(a)},x) \times \epsilon_{free\;space} \times E} \right] + \left. \frac{1}{\epsilon(r_{d(a)},x) \times E} \right] + \left.$$

$$\varepsilon_{2 \text{ E}}(\text{E}) = \frac{4q^2}{\varepsilon(r_{d(a)}, x) \times \varepsilon_{\text{free space}} \times \text{E}} \times \text{H}(\text{N}^*, r_{d(a)}, x, T) \times \left[\frac{\text{E} - \text{E}_{\text{gn2(gp2)}}}{\text{E} - \left[(\text{E}_{\text{gn2(gp2)}} + \text{E}_{\text{Fno(Fpo)}} - \text{E}_{\text{Fno(Fpo)}}\right]}\right]^2, \tag{19c}$$

Which gives: $\varepsilon_{2O-EP[2E-OP]}(E = E_{gn1(gp1)}[E_{gn2(gp2)}]) = 0$, and $\varepsilon_{2O-EP[2E-OP]}(E \to \infty) \to 0$, as those given in Ref. [2],

$$\propto_{O} (E) =$$

$$\frac{4q^2}{\hbar cn(E) \times \epsilon(r_{d(a)},x) \times \epsilon_{free \, space}} \times \left. H\left(N^*,r_{d(a)},x,T\right) \times \left[\frac{E-E_{gn1(gp1)}}{E-\left[E_{gn1(gp1)}+E_{Fn(Fp)}-E_{Fno(Fpo)}\right]}\right]^2 \ \left(\frac{1}{cm}\right) \ \ and$$

$$\alpha_{\rm E}^{}\left(\rm E\right) = \frac{4q^2}{\hbar cn(\rm E) \times \epsilon(r_{\rm d(a)}, x) \times \epsilon_{\rm free\, space}} \times H\left(N^*, r_{\rm d(a)}, x, T\right) \times \left[\frac{\rm E-E_{\rm gn2(gp2)}}{\rm E-\left[(E_{\rm gn2(gp2)} + E_{\rm Fn(Fp)} - E_{\rm Fno(Fpo)}\right]}\right]^2 \left(\frac{1}{\rm cm}\right), \tag{19d}$$

Which gives: $\propto_{O[E]} \left(E = E_{gn1(gp1)}[E_{gn2(gp2)}]\right) = 0$, and $\propto_{O[E]} (E \to \infty) \to Constant$, as those given in.^[2]

Furthermore, from Equations (16, 17, 19b), we can also determine $\varepsilon_{1 \text{ O}[E]}(E)$ and $R_{\text{O}[E]}(E)$.

Now, from Equations (18, 19b, 19c, 19d), using Eq. (15), for $E = [E_{gn1(gp1)}(E_{gn2(gp2)}) + E_{Fn(Fp)}]$, one obtains respectively, as:

$$\sigma_{O}(N^*, r_{d(a)}, x, T) = \frac{q^2}{\pi \times \hbar} \times H(N^*, r_{d(a)}, x, T) \times \left(\frac{E_{Fn(Fp)}}{E_{Fno(Fpo)}}\right)^2 \left(\frac{1}{\Omega \times cm}\right),$$

having the same form with that of $\sigma_E(N, r_{d(a)}, x, T)$ [1], as:

$$\sigma_{E}(N^*, r_{d(a)}, x, T) = \frac{q^2}{\pi \times \hbar} \times H(N^*, r_{d(a)}, x, T) \times \left(\frac{E_{Fn(Fp)}}{E_{Fno(Fno)}}\right)^2 \left(\frac{1}{\Omega \times cm}\right), \tag{20a}$$

Noting here that for given $(N^*, r_{d(a)}, x, T)$ -physical conditions we obtain: $\sigma_0 > \sigma_E$ since $m_r(x) < m_{c(v)}(x)$,

$$\begin{split} \kappa_O\big(N^*,r_{d(a)},x,T\big) &= \frac{2q^2}{n(E)\times\epsilon(r_{d(a)},x)\times\epsilon_{free\,space}\times(E_{gn1(gp1)}+E_{Fn(Fp)})} \times H\big(N^*,r_{d(a)},x,T\big) \times \\ &\left(\frac{E_{Fn(Fp)}}{E_{Fno(Fpo)}}\right)^2 \text{ and } \end{split}$$

$$\kappa_{E}(N^*, r_{d(a)}, x, T) = \frac{2q^2}{n(E) \times \epsilon(r_{d(a)}, x) \times \epsilon_{free \, space} \times (E_{gn2(gp2)} + E_{Fn(Fp)})} \times H(N^*, r_{d(a)}, x, T) \times \left(\frac{E_{Fn(Fp)}}{E_{Fno(Fpo)}}\right)^2, (20b)$$

$$\epsilon_{2\;0}\big(N^*,r_{d(a)},x,T\big) = \frac{4q^2}{\epsilon(r_{d(a)},x)\times\epsilon_{free\;space}\times(E_{gn1(gp1)}+E_{Fn(Fp)})} \times H\big(N^*,r_{d(a)},x,T\big) \times \left(\frac{E_{Fn(Fp)}}{E_{Fno(Fpo)}}\right)^2$$
 and

$$\varepsilon_{2 \text{ E}}\left(N^*, r_{d(a)}, x, T\right) = \frac{4q^2}{\varepsilon(r_{d(a)}, x) \times \varepsilon_{\text{free space}} \times (E_{\text{gn2}(\text{gp2})} + E_{\text{Fn}(\text{Fp})})} \times H\left(N^*, r_{d(a)}, x, T\right) \times \left(\frac{E_{\text{Fn}(\text{Fp})}}{E_{\text{Fno}(\text{Fpo})}}\right)^2,$$
(20c)

$$\begin{split} & \propto_O \left(N^*, r_{d(a)}, x, T \right) = \\ & \frac{4q^2}{\hbar cn(E) \times \epsilon(r_{d(a)}, x) \times \epsilon_{free \, space}} \times \left. H \left(N^*, r_{d(a)}, x, T \right) \times \left(\frac{E_{Fn(Fp)}}{E_{Fno(Fpo)}} \right)^2 \, \left(\frac{1}{cm} \right) \quad \text{and} \quad \end{split}$$

$$\propto_{\mathrm{E}} \left(\mathbf{N}^*, \mathbf{r}_{\mathrm{d}(a)}, \mathbf{x}, \mathbf{T} \right) = \frac{4q^2}{\hbar \mathrm{cn}(\mathbf{E}) \times \epsilon(\mathbf{r}_{\mathrm{d}(a)}, \mathbf{x}) \times \epsilon_{\mathrm{free \, space}}} \times \mathbf{H} \left(\mathbf{N}^*, \mathbf{r}_{\mathrm{d}(a)}, \mathbf{x}, \mathbf{T} \right) \times \left(\frac{\mathbf{E}_{\mathrm{Fn}(\mathrm{Fp})}}{\mathbf{E}_{\mathrm{Fno}(\mathrm{Fpo})}} \right)^2 \, \left(\frac{1}{\mathrm{cm}} \right). \tag{20d}$$

Further, from Equations (16, 17, 20b), we can also determine $\varepsilon_{1 \text{ O}[E]}(E)$ and $R_{\text{O}[E]}(E)$.

Then, the numerical results of various O[E]-coefficients, $X_{O[E]}(E, N^*, r_{d(a)}, x, T)$, as functions of E, obtained from Equations (18, 19b-19d, 20a-20d) for given $(N^*, r_{d(a)}, x, T)$ -physical conditions and $E \ge (or \le) E_{gn1(gp1)}(E_{gn2(gp2)})$, giving raise to the metal-insulator transition (MIT) and the non-MIT (N-MIT), are reported and discussed as follows.

First of all, one notes that from Equations (3, 6a, 6b) the MIT occurs as T=0 K and $N^*(N,r_{d(a)},x)\equiv N-N_{CDn(NDp)}(r_{d(a)},x)\cong N-N_{CDn(CDp)}^{EBT}(r_{d(a)},x)=0$, according, for $E\geq E_{gn(gp)}$, to : $E_{Fno(Fpo)}(N^*=0)\equiv \frac{\hbar^2\times k_{Fn(Fp)}^2(N^*)}{2\times m_{n(p)}^*(x)\times m_o}=0$, and $\kappa_{O[E]}^{MIT}(E,N^*=0)=0$, $\epsilon_{2O[E]}^{MIT}(E,N^*=0)=0$, $\epsilon_{2O[E]}^{MIT}(E,N^*=0)=0$, and $\epsilon_{O[E]}^{MIT}(E,N^*=0)=0$, since, for example, $\epsilon_{2O[E]}^{MIT}(E,N^*=0)=0$, is proportional to $\epsilon_{2O(E)}^2(E,N^*=0)=0$, or to $\epsilon_{2O(E)}^2(E,N^*=0)=0$. But, for such the same physical conditions: $\epsilon_{2O(E)}^2(E,N^*=0)=0$ and $\epsilon_{2O(E)}^2(E,N^*=0)=0$. But, for such the same physical conditions: $\epsilon_{2O(E)}^2(E,N^*=0)=0$, $\epsilon_{2O(E)}^2(E,N^*=0)=0$, we obtain other numerical results such as: $\epsilon_{2O(E)}^{N-MIT}(N^*=0,E)\neq 0$, $\epsilon_{2O(E)}^{N-MIT}(N^*=0,E)\neq 0$ and $\epsilon_{2O(E)}^{N-MIT}(N^*=0,E)\neq 0$, for $\epsilon_{2O(E)}^{N-MIT}(N^*=0,E)\neq 0$, $\epsilon_{2O(E)}^{N-MIT}(N^*=0,E)\neq 0$, and for $\epsilon_{2O(E)}^{N-MIT}(E,N^*=0)=0$, there is an $\epsilon_{2O(E)}^{N-MIT}(E,N^*=0)=0$, and ϵ_{2

Furthermore, in the MIT-case, we have showed that $N_{CDn(CDp)}$ is just the density of electrons (holes) localized in the exponential conduction (valence)-band tail, $N_{CDn(CDp)}^{EBT}$, with a precision of the order of $.77 \times 10^{-7}$, $N_{CDn(NDp)}(r_{d(a)}, x) \cong N_{CDn(CDp)}^{EBT}(r_{d(a)}, x)$ [3], giving

rise to: $E_{Fno(Fpo)}^{EBT}(N^* = N_{CDn(NDp)}) \neq 0$. Then, due to such the idea, we can also determine the corresponding numerical results as:

 $\kappa_{O[E]}^{EBT}(N^* = N_{CDn(NDp)}) \neq 0$, $\varepsilon_{2\ O[E]}^{EBT}(N^* = N_{CDn(NDp)}) \neq 0$, $\sigma_{O[E]}^{EBT}(N^* = N_{CDn(NDp)}) \neq 0$ and $\alpha_{O[E]}^{EBT}(N^* = N_{CDn(NDp)}) \neq 0$, suggesting that they increase with increasing $r_{d(a)}$, as those given in **Table 5, reported in Appendix 1**. Finally, the numerical results of $n_{O[E]}(E)$, $\kappa_{O[E]}(E)$, $\varepsilon_{2\ O[E]}(E)$ and $\varepsilon_{1\ O[E]}(E)$, are obtained by using Equations (17, 19b, 19c and 16), expressed as functions of N for (E=3.2 eV and T=20 K)-conditions, and as functions of T for (E=3.2 eV and N = 10^{20} cm⁻³)-conditions, as those given in **Tables 6n, 6p, 7n and 7p, being reported in Appendix 1**, respectively.

In the following, we will determine the electrical-and-thermoelectric laws, by basing on our $\sigma_{O[E]}$ -models, given in Eq. (20a).

OPTICAL [ELECTRICAL]-AND-THERMOELECTRIC PROPERTIES $[m_{n(p)}^* \equiv m_r(x)[m_{c(v)}(x)]]$

Here, if denoting, for majority electrons (holes), the thermal conductivity by $\sigma_{Th.\ O[E]}(N^*,r_{d(a)},x,T) \ \text{in} \ \frac{W}{cm\times K} \ , \ \text{and} \ \text{the Lorenz number} \ L \ \text{by:} \ L = \frac{\pi^2}{3}\times \left(\frac{k_B}{q}\right)^2 = 2.4429637 \left(\frac{W\times ohm}{K^2}\right) = 2.4429637\times 10^{-8} \left(V^2\times K^{-2}\right), \ \text{then the well-known Wiedemann-Frank law states that the ratio,} \ \frac{\sigma_{Th.O[E]}}{\sigma_{O[E]]}}, \ \text{due to the O-EP [E-OP], is proportional to the temperature T(K), as:}$

$$\frac{\sigma_{\text{Th.O[E]}}(N^*, r_{d(a)}, x, T)}{\sigma_{O[E]}(N^*, r_{d(a)}, x, T)} = L \times T.$$
(21)

Further, the resistivity is found to be given by: $\rho_{O[E]}(N^*, r_{d(a)}, x, T) \equiv 1/\sigma_{O[E]}(N^*, r_{d(a)}, x, T)$, noting again that $N^* \equiv N - N_{CDn(NDp)}(r_{d(a)}, x)$.

In Eq. (20a), one notes that at T=0 K, $\sigma_{O[E]}(N^*, r_{d(a)}, x, T)$ is proportional to $E^2_{Fno(Fpo)}$, or to $(N^*)^{\frac{4}{3}}$. Thus , from Eq. (21), one has: $\sigma_{O[E]}(N^*=0, r_{d(a)}, x, T=0K)=0$ and also $\sigma_{Th.\ O[E]}(N^*=0, r_{d(a)}, x, T=0K)=0$ at $N^*=0$, at which the MIT occurs.

Optical [Electrical] Coefficients

The relaxation time $\tau_{O[E]}$ is related to $\sigma_{O[E]}$ by $^{[1]}$:

 $\tau_{O[E]}(N^*,r_{d(a)},x,T)\equiv\sigma_{O[E]}(N^*,r_{d(a)},x,T)\times\frac{m_{n(p)}^*(x)\times m_o}{q^2\times (N^*/g_{c(v)})}\,. \label{eq:tau_OE}$ Therefore, the mobility $\mu_{O[E]}$ is given by:

$$\mu_{O[E]]}(N^*, r_{d(a)}, x, T) = \frac{q \times \tau_{O[E]}(N^*, r_{d(a)}, x, T)}{m_{n(p)}^*(x) \times m_o} = \frac{\sigma_{O[E]}(N^*, r_{d(a)}, x, T)}{q \times (N^*/g_{c(v)})} \left(\frac{cm^2}{V \times s}\right). \tag{22}$$

Here, at T=0K, $\mu_{O[E]}(N^*,r_{d(a)},x,T)$ is thus proportional to $(N^*)^{1/3}$, since $\sigma_{O[E]}(N^*,r_{d(a)},x,T=0K)$ is proportional to $(N^*)^{4/3}$. Thus, $\tau_{O[E]}(N^*=0,r_{d(a)},x,T=0K)=0$ and $\mu_{O[E]}(N^*=0,r_{d(a)},x,T=0K)=0$ at $N^*=0$, at which the MIT occurs.

Then, the Hall factor is defined by:

$$r_{HO[HE]}(N^*,r_{d(a)},x,T) \equiv \frac{\langle \tau_{O[E]}^2 \rangle_{FDDF}}{\left[\langle \tau_{O[E]} \rangle_{FDDF} \right]^2} = \frac{G_4(y)}{[G_2(y)]^2}, \\ y \equiv \frac{\pi}{\xi_{n(p)}(N^*,r_{d(a)},x,T)} = \frac{\pi k_B T}{E_{Fn(Fp)}(N^*,r_{d(a)},x,T)}, \text{ and therefore, the Hall mobility yields:}$$

$$\mu_{\text{HO[HE]}}(N^*, r_{\text{d(a)}}, x, T) \equiv \mu_{\text{O[E]}}(N^*, r_{\text{d(a)}}, x, T) \times r_{\text{HO[HE]}}(N^*, r_{\text{d(a)}}, x, T) \left(\frac{\text{cm}^2}{\text{V} \times \text{s}}\right), \tag{23}$$

Noting that, at T=0K, since $r_{HE[HO]}(N^*, r_{d(a)}, x, T) = 1$, one therefore gets: $\mu_{HO[HE]}(N^*, r_{d(a)}, x, T) \equiv \mu_{O[E]}(N^*, r_{d(a)}, x, T).$

Our generalized Einstein relation

Our generalized Einstein relation is found to be defined as^[1]:

$$\frac{D_{O[E]}(N^*,r_{d(a)},x,T)}{\mu_{O[E]}(N^*,r_{d(a)},x,T)} \equiv \frac{N^*}{q} \times \frac{dE_{Fn(Fp)}}{dN^*} \equiv \frac{k_B \times T}{q} \times \left(u \frac{d\xi_{n(p)}(u)}{du}\right) = \sqrt{\frac{3 \times L}{\pi^2}} \times T \times \left(u \frac{d\xi_{n(p)}(u)}{du}\right), \qquad \frac{k_B}{q} = \sqrt{\frac{3 \times L}{\pi^2}} \,, \tag{24}$$

Where $D_{E[O]}\left(N^*, r_{d(a)}, x, T\right)$ is the diffusion coefficient, $\xi_{n(p)}(u)$ is defined in Eq. (11), and the mobility $\mu_{O[E]}\left(N^*, r_{d(a)}, x, T\right)$ is determined in Eq. (22). Then, by differentiating this function $\xi_{n(p)}(u)$ with respect to u, one thus obtains $\frac{d\xi_{n(p)}(u)}{du}$. Therefore, Eq. (17) can also be rewritten as: $\frac{D_{O[E]}(N^*, r_{d(a)}, x, T)}{\mu_{O[E]}(N^*, r_{d(a)}, x, T)} = \frac{k_B \times T}{q} \times u \frac{V'(u) \times W(u) - V(u) \times W'(u)}{W^2(u)}$ where $W'(u) = ABu^{B-1}$ and $V'(u) = u^{-1} + 2^{-\frac{3}{2}}e^{-du}(1-du) + \frac{2}{3}Au^{B-1}F(u)\left[\left(1+\frac{3B}{2}\right) + \frac{4}{3}\times\frac{bu^{-\frac{4}{3}}+2cu^{-\frac{8}{3}}}{1+bu^{-\frac{4}{3}}+cu^{-\frac{8}{3}}}\right]$. One remarks that: (i) as $u \to 0$, one has: $W^2 \simeq 1$ and $u[V' \times W - V \times W'] \simeq 1$, and therefore: $\frac{D_{O[E]}(u)}{\mu_{O[E]}} \simeq \frac{k_B \times T}{q}$, and (ii) as $u \to \infty$, one has: $W^2 \approx A^2u^{2B}$ and $u[V' \times W - V \times W'] \approx \frac{2}{3}au^{2/3}A^2u^{2B}$, and therefore, in this **highly degenerate case** and at T=0K, the **above generalized Einstein**

relation is reduced to the usual Einstein one: $\frac{D_{O[E]}(N^*,r_{d(a)},x,T=0K)}{\mu_{O[E]}(N^*,r_{d(a)},x,T=0K)} \approx \frac{2}{3} E_{Fno(Fpo)}(N^*)/q$. In other words, Eq. (24) verifies the correct limiting conditions.

Furthermore, in the present degenerate case ($u \gg 1$), Eq. (24) gives:

$$\frac{D_{O[E]}\left(N^*, r_{d(a)}, x, T = 0K\right)}{\mu_{O[E]}\left(N^*, r_{d(a)}, x, T = 0K\right)} \simeq \frac{2}{3} \times \frac{E_{Fno(Fpo)}(u)}{q} \times \left[1 + \frac{4}{3} \times \frac{\left(bu^{-\frac{4}{3}} + 2cu^{-\frac{8}{3}}\right)}{\left(1 + bu^{-\frac{4}{3}} + cu^{-\frac{8}{3}}\right)}\right] \; ,$$

Where
$$a = \left[3\sqrt{\pi}/4\right]^{2/3}$$
, $b = \frac{1}{8} \left(\frac{\pi}{a}\right)^2$ and $c = \frac{62.3739855}{1920} \left(\frac{\pi}{a}\right)^4$.

Then, in **Tables 8n and 8p, reported in Appendix1**, the numerical results of $\sigma_{O[E]}$, $\mu_{O[E]}$ and $D_{O[E]}$ for given

x and T=(4.2 K and 77 K), are obtained by using Equations (20a, 22 and 24), suggesting that, for a given N, they decrease [decrease], with increasing $r_{d(a)}$.

Thermoelectric Coefficients

Here, as noted above, $E_{Fn(Fp)}\big(m_r(x)\big) > E_{Fn(Fp)}\big(m_{c(v)}(x)\big)$ or $\xi_{n(p)}\big(m_r(x)\big) > \xi_{n(p)}\big(m_{c(v)}(x)\big)$ for a given T, since $m_r(x) < m_{c(v)}(x)$ for given x, corresponding to: $\sigma_0\big(m_r(x)\big) > \sigma_E\big(m_{c(v)}(x)\big)$.

Then, from Eq. (20a), obtained for $\sigma_{O[E]}(N^*, r_{d(a)}, x, T)$, the well-known Mott definition for the thermoelectric power or for the Seebeck coefficient, $S_{E[O]}$, is found to be given by:

$$S_{O[E]}\big(N^*,r_{d(a)},x,T\big) \equiv \frac{-\pi^2}{3} \times \frac{k_B}{q>0} \times k_BT \times \frac{\partial ln\sigma_{O[E]}}{\partial E}\bigg]_{E=E_{Fn(Fn)}} = \frac{-\pi^2}{3} \times \frac{k_B}{q} \times \frac{\partial ln\sigma_{O[E]}(\xi_{n(p)})}{\partial \xi_{n(p)}}.$$

Then, using Eq. (11), for the degenerate case, $\xi_{n(p)} \ge 0$, one gets, by putting

$$Y_{\text{Sb O[E]}}(N^*, r_{d(a)}, x, T) \equiv \left[1 - \frac{y^2}{3 \times G_2\left(y = \frac{\pi}{\xi_{n(p)}}\right)}\right],$$

$$S_{O[E]}(N^*, r_{d(a)}, x, T) \equiv \frac{-\pi^2}{3} \times \frac{k_B}{q} \times \frac{2Y_{Sb \ O[E]}(N^*, r_{d(a)}, x, T)}{\xi_{n(p)}} = -\sqrt{\frac{3 \times L}{\pi^2}} \times \frac{2 \times \xi_{n(p)}}{\left(1 + \frac{3 \times \xi_{n(p)}^2}{\pi^2}\right)} = -2\sqrt{L} \times \frac{\sqrt{\frac{2T_{O[E]Mott}}{1 + 2T_{O[E]Mott}}}}{\sqrt{\frac{V}{K}}} < 0, \quad ZT_{O[E]Mott} = \frac{\pi^2}{3 \times \xi_{n(p)}^2}, \tag{25}$$

according to:

$$\frac{\partial \, S_{O[E]}}{\partial \xi_{n(p)}} = \sqrt{\frac{3 \times L}{\pi^2}} \times 2 \times \frac{\frac{3 \times \xi_{n(p)}^2}{\pi^2} - 1}{\left(1 + \frac{3 \times \xi_{n(p)}^2}{\pi^2}\right)^2} = \sqrt{\frac{3 \times L}{\pi^2}} \times 2 \times \frac{ZT_{O[E]Mott} \times \left[1 - ZT_{O[E]Mott}\right]}{\left[1 + ZT_{O[E]Mott}\right]^2}.$$

Here, one notes that: (i) as $\xi_{n(p)} \to +\infty$ or $\xi_{n(p)} \to +0$, one has a same limiting value of $S_{O[E]}\colon S_{O[E]} \to -0$, (ii) at $\xi_{n(p)} = \sqrt{\frac{\pi^2}{3}} \simeq 1.8138$, since $\frac{\partial \, S_{O[E]}}{\partial \xi_{n(p)}} = 0$, one therefore gets: a minimum $\left(\,S_{O[E]}\right)_{min.} = -\sqrt{L} \simeq -1.563 \times 10^{-4} \, \left(\frac{V}{K}\right)$, and (iii) at $\xi_{n(p)} = 1$ one obtains: $S_{O[E]} \simeq -1.322 \times 10^{-4} \, \left(\frac{V}{K}\right)$.

Further, the figure of merit is found to be defined by:

$$ZT_{O[E]}(N^*, r_{d(a)}, x, T) \equiv \frac{S^2 \times \sigma_{O[E]} \times T}{\kappa} = \frac{S^2}{L} = \frac{4 \times ZT_{O[E]Mott}}{[1 + ZT_{O[E]Mott}]^2}.$$
 (26)

Here, one notes that: (i) $\frac{\partial (ZT_{O[E]})}{\partial \xi_{n(p)}} = 2 \times \frac{S_{O[E]}}{L} \times \frac{\partial S_{O[E]}}{\partial \xi_{n(p)}}$, $S_{E[O]} < 0$, (ii) at $\xi_{n(p)} = \sqrt{\frac{\pi^2}{3}} \simeq 1.8138$, since $\frac{\partial (ZT_{O[E]})}{\partial \xi_{n(p)}} = 0$, one gets: a maximum $\left(ZT_{O[E]}\right)_{max.} = 1$, $ZT_{O[E]Mott} = 1$, and (iii) at $\xi_{n(p)} = 1$, one obtains: $ZT_{O[E]} \simeq 0.715$ and $ZT_{O[E]Mott} = \frac{\pi^2}{3} \simeq 3.290$.

Finally, the first Van-Cong coefficient can be defined by:

$$VC1_{O[E]}(N^*, r_{d(a)}, x, T) \equiv -N^* \times \frac{d S_{O[E]}}{dN^*} \left(\frac{V}{K}\right) = N^* \times \frac{\partial S_{O[E]}}{\partial \xi_{n(p)}} \times -\frac{\partial \xi_{n(p)}}{\partial N^*}, \tag{27}$$

being equal to 0 for $\xi_{n(p)}=\sqrt{\frac{\pi^2}{3}}$,

and the second Van-Cong coefficient as:

$$VC2_{O[E]}(N^*, r_{d(a)}, x, T) \equiv T \times VC1_{O[E]}(V), \tag{28}$$

the Thomson coefficient, Ts, by:

$$Ts_{O[E]}\left(N^*, r_{d(a)}, x, T\right) \equiv T \times \frac{d \, S_{O[E]}}{dT} \left(\frac{V}{K}\right) = T \times \frac{\partial \, S_{O[E]}}{\partial \xi_{n(p)}} \times \frac{\partial \xi_{n(p)}}{\partial T}, \tag{29}$$

being equal to 0 for $\xi_{n(p)} = \sqrt{\frac{\pi^2}{3}}$,

and the Peltier coefficient, Pt_{E[O]}, as:

$$Pt_{O[E]}(N^*, r_{d(a)}, x, T) \equiv T \times S_{O[E]}(V). \tag{30}$$

Then, in **Tables 9n and 9p, reported in Appendix 1**, the numerical results of various thermoelectric coefficients such as: $\sigma_{Th.O[E]}$, $S_{O[E]}$, $VC1_{O[E]}$, $VC2_{O[E]}$, $Ts_{O[E]}$, $Pt_{O[E]}$ and $ZT_{O[E]}$, for given x, $r_{d(a)}$, T=(3K and 80K) and N, are obtained by using Equations (21, 25, 27, 28, 29, 30 and 26), respectively.

In summary, in the O-EP [E-OP] and for given physical conditions: x, $r_{d(a)}$, N (or T), the same values of $\xi_{n(p)}$ decrease, according to the increasing T (or to the decreasing N), since $VC1_{O[E]}(N,r_{d(a)},x,T)$ and $Ts_{O[E]}(N,r_{d(a)},x,T)$ are expressed in terms of $\frac{-d\,S_{O[E]}}{dN^*}$ and $\frac{d\,S_{O[E]}}{dT}$, one has: $[VC1_{O[E]},Ts_{O[E]}]<0$ for $\xi_{n(p)}>\sqrt{\frac{\pi^2}{3}}$, $[VC1_{O[E]},Ts_{O[E]}]=0$ for $\xi_{n(p)}=\sqrt{\frac{\pi^2}{3}}$, and $[VC1_{O[E]},Ts_{O[E]}]>0$ for $\xi_{n(p)}<\sqrt{\frac{\pi^2}{3}}$, stating that for $\xi_{n(p)}=\sqrt{\frac{\pi^2}{3}}\simeq 1.8138$: $S_{O[E]}$, determined in Eq. (25), thus presents **a same minimum** $S_{O[E]\,min.}=-\sqrt{L}\simeq -1.563\times 10^{-4}\,\left(\frac{V}{K}\right)$, and $ZT_{O[E]}$, determined in Eq. (26), therefore presents **a same maximum:** $ZT_{O[E]\,max}=1$, and $(ZT)_{Mott}=1$. Furthermore, for $\xi_{n(p)}=1$, the numerical results of $S_{O[E]}$, $ZT_{O[E]}$, $ZT_{O[E]Mott}$, $VC1_{E[O]}$, and $Ts_{O[E]}$, present the **same results**: $-1.322\times 10^{-4}\,\frac{V}{K}$, $0.715,\ 3.290,\ 1.105\times 10^{-4}\,\frac{V}{K}$, and $1.657\times 10^{-4}\,\frac{V}{K}$, respectively, as those observed in [4, 5], and those given in **Table 10, reported in Appendix 1.**

It seems that these same obtained results could represent a new law for the thermoelectric properties, obtained in the degenerate case $(\xi_{n(p)} \ge 0)$.

Furthermore, it is interesting to remark that the $VC2_{O[E]}$ -coefficient is related to our generalized Einstein relation (24) by:

$$\frac{k_{B}}{q} \times VC2_{O[E]}(N^{*}, r_{d(a)}, x, T) \equiv -\frac{\partial S_{O[E]}}{\partial \xi_{n(p)}} \times \frac{D_{O[E]}(N^{*}, r_{d(a)}, x, T)}{\mu_{O[E]}(N^{*}, r_{d(a)}, x, T)} \quad \left(\frac{V^{2}}{K}\right) , \qquad \frac{k_{B}}{q} = \sqrt{\frac{3 \times L}{\pi^{2}}} ,$$
(31)

according, in this work, with the use of our Eq. (25), to:

$$VC2_{O[E]}\big(N, r_{d(a)}, x, T\big) \equiv -\frac{\frac{D_{O[E]}\left(N^*, r_{d(a)}, x, T\right)}{\mu_{O[E]}\left(N^*, r_{d(a)}, x, T\right)}}{\mu_{O[E]}\left(N^*, r_{d(a)}, x, T\right)} \times 2 \times \frac{\frac{ZT_{O[E]Mott} \times \left[1 - ZT_{O[E]Mott}\right]}{\left[1 + ZT_{O[E]Mott}\right]^2}}{\left[1 + ZT_{O[E]Mott}\right]^2} \quad (V).$$

Of course, our relation (31) is reduced to: $\frac{D_{O[E]}}{\mu_{O[E]}}$, $VC1_{O[E]}$ and $VC2_{O[E]}$, being determined respectively by Equations (24, 27, 28). This may be a new result.

CONCLUDING REMARKS

In the $\mathbf{n}^+(\mathbf{p}^+) - \mathbf{InP_{1-x}As_x}$ -crystalline alloy, $0 \le x \le 1$, x being the concentration, the optical, electrical and thermoelectric coefficients, enhanced by: (i) the optico-electrical phenomenon (O-EP) and the electro-optical phenomenon (E-OP), (ii) our static dielectric constant law, $\epsilon(r_{d(a)}, x)$, $r_{d(a)}$ being the donor (acceptor) d(a)-radius, given in Equations (1a, 1b), (iii) our accurate reduced Fermi energy, $\xi_{n(p)}$, given in Eq. (11), accurate with a precision of the order of $2.11 \times 10^{-4[9]}$, affecting all the expressions of optical, electrical and thermoelectric coefficients, and (iv) our optical-and-electrical conductivity models, given in Eq. (18, 20a), are now investigated by basing on our physical model and Fermi-Dirac distribution function, as those given in our recent works. [1-5]

Some important concluding remarks can be given and discussed as follows.

- (I) First of all, one notes that from Equations (3, 6a, 6b) the MIT occurs as T=0 K and $N^*(N,r_{d(a)},x)\equiv N-N_{CDn(NDp)}(r_{d(a)},x)\cong N-N_{CDn(CDp)}^{EBT}(r_{d(a)},x)=0$, according, for $E\geq E_{gn(gp)}$, to: $E_{Fno(Fpo)}(N^*=0)\equiv \frac{\hbar^2\times k_{Fn(Fp)}^2(N^*)}{2\times m_{n(p)}^*(x)\times m_o}=0$, and $\kappa_{O[E]}^{MIT}(E,N^*=0)=0$, $\epsilon_{O[E]}^{MIT}(E,N^*=0)=0$, and $\epsilon_{O[E]}^{MIT}(E,N^*=0)=0$, since, for example, $\epsilon_{O[E]}^{MIT}(E,N^*=0)=0$, is proportional to $\epsilon_{Fno(Fpo)}^2$, or to $\epsilon_{O[E]}^2$, we obtain other numerical results such as: $\epsilon_{O[E]}^{N-MIT}(N^*=0,E)\neq 0$, $\epsilon_{O[E]}^{N-MIT}(N^*=0,E)\neq 0$, according to the non-MIT (N-MIT), as showed in Tables 3, 4n and 4p, reported in Appendix 1. These Tables also state that, at $\epsilon_{O[E]}^{N-MIT}(N^*=0,E)=\epsilon_{O[E]}^{N-MIT}(N^*=0,E)$ and $\epsilon_{O[E]}^{N-MIT}(N^*=0,E)$ and $\epsilon_{O[E]}^{N-MIT}(N^*=$
- (II) In such the MIT-case, we have also showed that $N_{CDn(CDp)}$ is just the density of electrons (holes) localized in the exponential conduction (valence)-band tail, $N_{CDn(CDp)}^{EBT}$, with a precision of the order of 2.77×10^{-7} , $N_{CDn(NDp)}(r_{d(a)}, x) \cong N_{CDn(CDp)}^{EBT}(r_{d(a)}, x)$ [3], giving rise to: $E_{Fno(Fpo)}^{EBT}(N^* = N_{CDn(NDp)}) \neq 0$. Then, due to such the idea, we can also determine the corresponding numerical results as:

$$\begin{split} \kappa_{O[E]}^{EBT}\big(N^* &= N_{CDn(NDp)}\big) \neq 0 \quad, \quad \epsilon_{2\ O[E]}^{EBT}\big(N^* = N_{CDn(NDp)}\big) \neq 0 \quad, \quad \sigma_{O[E]}^{EBT}\big(N^* = N_{CDn(NDp)}\big) \neq 0 \\ \text{and} \quad &\propto_{O[E]}^{EBT}\big(N^* = N_{CDn(NDp)}\big) \neq 0, \text{ suggesting that they increase with increasing } r_{d(a)}, \text{ as those} \\ \text{given in Table 5, reported in Appendix 1. Finally, the numerical results of } n_{O[E]}(E), \kappa_{O[E]}(E), \\ \epsilon_{2\ O[E]}(E) \text{ and } \epsilon_{1\ O[E]}(E), \text{ are obtained by using Equations (17, 19b, 19c and 16), expressed} \\ \text{as functions of N for } (E=3.2\ \text{eV} \text{ and } T=20\ \text{K})\text{-conditions, and as functions of T for } (E=3.2\ \text{eV} \text{ and } N=10^{20}\text{ cm}^{-3})\text{-conditions, as those given in Tables 6n, 6p, 7n and 7p, being reported in Appendix 1, respectively.} \end{split}$$

- (III) In Tables 8n and 8p, reported in Appendix1, the numerical results of $\sigma_{O[E]}$, $\mu_{O[E]}$ and $D_{O[E]}$ for given x and T=(4.2 K and 77 K), are obtained by using Equations (20a, 22 and 24), suggesting that, for a given N, they decrease [decrease], with increasing $r_{d(a)}$. Further, in Tables 9n and 9p, reported in Appendix 1, the numerical results of various thermoelectric coefficients such as: $\sigma_{Th.O[E]}$, $S_{O[E]}$, $VC1_{O[E]}$, $VC2_{O[E]}$, $Ts_{O[E]}$, $Pt_{O[E]}$ and $Tr_{O[E]}$, for given x, $Tr_{d(a)}$, $Tr_{$
- (IV) From Equations (20a, 21-30), for any given x, $r_{d(a)}$ and N (or T), with increasing T (or decreasing N), one obtains: (i) for $\xi_{n(p)} = \sqrt{\frac{\pi^2}{3}} \simeq 1.8138$, while the numerical results of $S_{O[E]}$ present a same minimum $S_{O[E]\,min.}\left(\simeq -1.563\times 10^{-4}\frac{V}{K}\right)$, those of $ZT_{O[E]}$ show a same maximum $ZT_{ET[OT]\,max.} = 1$, (ii) for $\xi_{n(p)} = 1$, the numerical results of $S_{O[E]}$, $ZT_{O[E]}$, $ZT_{O[E]\,Mott}$, $VC1_{O[E]]}$, and $Ts_{O[E]}$, present the same results: $-1.322\times 10^{-4}\frac{V}{K}$, 0.715, 3.290, $1.105\times 10^{-4}\frac{V}{K}$, and $1.657\times 10^{-4}\frac{V}{K}$, respectively, and finally (iii) for $\xi_{n(p)} = \sqrt{\frac{\pi^2}{3}} \simeq 1.8138$, $ZT_{O[E]\,Mott} = 1$, as those given in Table 10, reported in Appendix 1.

REFERENCES

- 1. Van Cong, H. Optical-Electrical Phenomenon _ Electro-Optical Phenomenon-Transition, Observed in n(p)-Type Degenerate GaP(1-x)Sb(x)-Crystalline Alloy (12). WJERT, 2025; 11(8): 78-100.
- 2. Van Cong, H. et al. Optical Coefficients in the n(p)-Type Degenerate InP(1-x) As(x) Crystalline Alloy, Due to the New Static Dielectric Constant-Law and the Generalized Mott Criterium in the Metal-Insulator Transition (20). WJERT, 2024; 10(12): 378-399.

- 3. Van Cong, H. New Critical Impurity Density in Metal-Insulator Transition, obtained in Various n(p)-Type Degenerate Crystalline Alloys, being Just That of Carriers Localized in Exponential Band Tails. WJERT, 2024; 10(4): 05-23.
- 4. Van Cong H. Same maximum figure of merit ZT(=1), due to the effect of impurity size, obtained in the n(p)-type degenerate Ge -crystal ($\xi_{n(p)} \ge 1$), at same reduced Fermi energy $\xi_{n(p)} = \sqrt{\frac{\pi^2}{3}} \simeq 1.8138$, same minimum Seebeck coefficient (S)_{min.} ($\simeq -1.563 \times 10^{-4} \frac{V}{K}$), same maximum (ZT)_{max.} = 1, and same (ZT)_{Mott} ($= \frac{\pi^2}{3\xi_{n(p)}^2} = 1$), SCIREA Journal of Physics, 2023; 8(4): 407-430.
- 5. Van Cong, H. Same Maximal Figure of Merit ZT(=1), Due to the Effect of Impurity Size, Obtained in the n(p)-Type Degenerate GaAs-Crystal ($\xi_{n(p)} \ge 1$), at Same Reduced Fermi Energy $\xi_{n(p)}(=1.8138)$ and Same Minimum Seebeck Coefficient $S\left(=-1.563 \times 10^{-4} \frac{V}{K}\right)$, at which Same (ZT)_{Mott} $\left(=\frac{\pi^2}{3\xi_{n(p)}^2}=1\right)$. SCIREA Journal of Physics, 2023; 8(2): 133-157.
- 6. Van Cong, H. Effects of donor size and heavy doping on optical, electrical and thermoelectric properties of various degenerate donor-silicon systems at low temperatures. American Journal of Modern Physics, 2018; 7(4): 136-165.
- 7. Kim, H. S. et al. Characterization of Lorenz number with Seebeck coefficient measurement. APL Materials, 2015; 3(4): 041506.
- 8. Hyun, B. D. et al. Electrical-and-Thermoelectric Properties of 90%Bi₂Te₃ 5%Sb₂Te₃ 5%Sb₂Se₃ Single Crystals Doped with SbI₃. Scripta Materialia, 1998; 40(1): 49-56.
- 9. Van Cong, H. and Debiais, G. A simple accurate expression of the reduced Fermi energy for any reduced carrier density. J. Appl. Phys., 1993; 73: 1545-1546.
- 10. Van Cong, H. et al. Size effect on different impurity levels in semiconductors. Solid State Communications, 1984; 49: 697-699.
- 11. Van Cong, H. Diffusion coefficient in degenerate semiconductors. Phys. Stat. Sol. (b), 1984; 101: K27.
- 12. Van Cong, H. and Doan Khanh, B. Simple accurate general expression of the Fermi-Dirac integral $F_i(a)$ and for j > -1. Solid-State Electron., 1992; 35(7): 949-951.

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- 13. Van Cong, H. New series representation of Fermi-Dirac integral $F_j(-\infty < a < \infty)$ for arbitrary j > -1, and its effect on $F_j(a \ge 0_+)$ for integer $j \ge 0$. Solid-State Electron., 1991; 34(5): 489-492.
- 14. Van Cong, H. and G. Mesnard. Thermoelectric effects of heavily doped semiconductors at low temperatures. Phys. Stat. Sol. (b), 1972; 50(1): 53-58.
- 15. Van Cong, H. Fermi energy and band-tail parameters in heavily doped semiconductors. Journal of Physics and Chemistry of Solids, 1975; 36(11): 1237-1240.
- 16. Van Cong, H. Quantum efficiency and radiative lifetime in degerate n-type GaAs. Journal of Physics and Chemistry of Solids, 1981; 36(11): 95-99.

APPENDIX 1

Table 1: In the $InP_{1-x}As_x$ -crystalline alloy, the different values of energy-band-structure parameters, for a given x, are given in the following.^[3]

In the
$$\text{InP}_{1-x}\text{As}_x$$
-crystalline alloy, in which $r_{do(ao)} = r_{P(In)} = 0.110$ (0.144) nm, we have $g_{c(v)}(x) = 1 \times x + 1 \times (1-x) = 1$, $m_{c(v)}(x)/m_o = 0.09$ (0.3) $\times x + 0.077$ (0.5) \times (1 - x) , $\epsilon_o(x) = 14.55 \times x + 12.5 \times (1-x)$, $E_{go}(x) = 0.43 \times x + 1.424 \times (1-x)$.

Table 2: Expressions for $G_{p>1}(y\equiv\frac{\pi}{\xi_{n(p)}})$, due to the Fermi-Dirac distribution function, are used to determine the electrical-and-thermoelectric coefficients.

Table 3: For T=0K and N=N_{CDn(CDp)}($r_{d(a)}$, x), the numerical results of $n_{0[E]}^{N-MIT}$, $\epsilon_{1\ 0[E]}^{N-MIT}$ and $R_{0[E]}^{N-MIT}$ are obtained, using Equations (17, 16), suggesting that they decrease (\searrow) with increasing (\nearrow) $r_{d(a)}$ and $E_{gn(gp)}$, and further they are found to be the same, for given $r_{d(a)}$ and $E_{gn(gp)}$, since $E_{gn1(gp1)} = E_{gn2(gp2)} = E_{gn2(gp2)}$.

Donor		P	As	Sb	Sn
r _d (nm) [4]	7	0.110	0.118	0.136	0.140
At x=0 ,					
$E_{gn}(meV)$	7	1424 [1424]	1424.3 [1424.3]	1427.8 [1427.8]	1429 [1429]
$n_{O[E]}^{N-MIT} \\$	7	3.425 [3.425]	3.401 [3.401]	3.210 [3.210]	3.155 [3.155]
$\epsilon_{1\ O[E]}^{N-MIT}$	7	11.73 [11.73]	11.57 [11.57]	10.30 [10.30]	9.956 [9.956]

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						Technology
$R_{O[E]}^{N-MIT}$	7	0.300 [0.300]	0.298 [0.298]	0.275 [0.275]	0.269 [0.269]	
At x=0.5 ,						
$E_{gn}(meV)$	7	927 [927]	927.3 [927.3]	930.5 [930.5]	931.8 [931.8]	
$n_{O[E]}^{N-MIT}$	7	3.815 [3.815]	3.790 [3.790]	3.592 [3.592]	3.535 [3.535]	
$\epsilon_{1\ O[E]}^{N-MIT}$	>	14.56 [14.56]	14.37 [14.37]	12.90 [12.90]	12.50 [12.50]	
$R_{O[E]}^{N-MIT}$	7	0.342 [0.342]	0.339 [0.339]	0.318 [0.318]	0.312 [0.312]	
At x=1 ,						
$E_{gn}(meV)$	7	430 [430]	430.3 [430.3]	433.3 [433.3]	434.4 [434.4]	
$n_{O[E]}^{N-MIT} \\$	7	4.203 [4.203]	4.177 [4.177]	3.971 [3.971]	3.912 [3.912]	
$\epsilon_{1~O[E]}^{N-MIT}$	7	17.66 [17.66]	17.45 [17.45]	15.77 [15.77]	15.31 [5.31]	
$R_{O[E]}^{N-MIT}$	7	0.379 [0.379]	0.376 [0.376]	0.357 [0.357]	0.351 [0.351]	
Acceptor		Ga	Mg	In	Cd	
r _a (nm)	į	0.126	0.140	0.144	0.148	
At x=0 ,						
$E_{gp}(meV)$	7	1418.2 [1418.2]	1423.7 [1423.7]	1424 [1424]	1424.3 [1424.3]	
$n_{O[E]}^{N-MIT}$	7	3.501 [3.501]	3.429 [3.429]	3.425 [3.425]	3.421 [3.421]	
$\epsilon_{1~O[E]}^{N-MIT}$	7	12.26 [12.26]	11.76 [11.76]	11.73 [11.73]	11.71 [11.71]	
$R_{O[E]}^{N-MIT}$	7	0.309 [0.309]	0.301 [0.301]	0.300 [0.300]	0.299 [0.299]	
At x=0.5 ,						
$E_{\rm gp}({\rm meV})$	7	923.1 [923.1]	926.8 [926.8]	927.0 [927.0]	927.2 [927.2]	
$n_{O[E]}^{N-MIT} \\$	7	3.893 [3.893]	3.819 [3.819]	3.816 [3.816]	3.812 [3.812]	
$\epsilon_{1\ O[E]}^{N-MIT}$	7	15.16 [15.16]	14.59 [14.59]	14.56 [14.56]	14.53 [14.53]	
$\epsilon_{1\ O[E]}^{N-MIT}$	7	0.350 [0.350]	0.342 [0.342]	0.341 [0.341]	0.341 [0.341]	
At x=1 ,						· · · · · · · · · · · · · · · · · · ·
$E_{gp}(meV)$	7	427.4 [427.4]	429.9 [429.9]	430.0 [430.0]	430.1 [430.1]	
$n_{O[E]}^{N-MIT} \\$	7	4.283 [4.283]	4.207 [4.207]	4.203 [4.203]	4.199 [4.199]	
$\epsilon_{1\ O[E]}^{N-MIT}$	7	18.34 [18.34]	17.70 [17.70]	17.66 [17.66]	17.63 [17.63]	
$R_{O[E]}^{MIT} \\$	7	0.386 [0.386]	0.379 [0.379]	0.379 [0.379]	0.378 [0.378]	

Table 4n. For T=0K and N=N_{CDn}(r_d , x), and for given x and r_d , the numerical results of $n_{O[E]}^{N-MIT}$, $\epsilon_{1\ O[E]}^{N-MIT}$ and $R_{O[E]}^{N-MIT}$ are obtained, using Equations (17, 16), suggesting that, for a given E, they are found to be the same, since $E_{gn1}=E_{gn2}=E_{gn}$.

E in eV	$n_{O[E]}^{N-MIT}$	$\epsilon_{1\ O[E]}^{N-MIT}$	$R_{O[E]}^{N-MIT}$
At x=0, and in t	the As-X(x)-system, in which	$E_{gn}(r_{As}, x = 0) = 1.424$	13 eV,
1.4243	3.401 [3.401]	11.57 [11.57]	0.298 [0.298]
2	3.885 [3.885]	15.09 [15.09]	0.349 [0.349]
2.5	4.613 [4.613]	21.28 [21.28]	0.414 [0.414]
3	4.565 [4.565]	20.84 [20.84]	0.410 [0.410]
3.5	3.601 [3.601]	12.97 [12.97]	0.318 [0.318]
4	3.754 [3.754]	14.09 [14.09]	0.335 [0.335]
4.5	4.134 [4.134]	17.09 [17.09]	0.373 [0.373]
5	2.268 [2.268]	5.14 [5.14]	0.150 [0.150]
5.5	0.998 [0.998]	0.995 [0.995]	$1.4 \times 10^{-6} \ [1.4 \times 10^{-6}]$
6	1.143 [1.143]	1.307 [1.307]	$4.5 \times 10^{-3} [4.5 \times 10^{-3}]$
 10 ²²	1.984 [1.984]	3.937 [3.937]	0.109 [0.109]
At x=0.5, and in	n the As-X(x)-system, in which	$E_{gn}(r_{As}, x = 0.5) = 0$.9273 eV,
0.9273	3.790 [3.790]	14.37 [14.37]	0.339 [0.339]
2	4.893 [4.893]	23.94 [23.94]	0.436 [0.436]
2.5	5.928 [5.928]	35.14 [35.14]	0.506 [0.506]
3	5.397 [5.397]	29.13 [29.13]	0.472 [0.472]
3.5	3.714 [3.714]	13.80 [13.80]	0.331 [0.331]
4	3.923 [3.923]	15.39 [15.39]	0.352 [0.352]
4.5	4.419 [4.419]	19.53 [19.53]	0.398 [0.398]
5	1.968 [1.968]	3.87 [3.87]	0.106 [0.106]
5.5	0.418 [0.418]	0.174 [0.174]	0.169 [0.169]
6	0.672 [0.672]	0.452 [0.452]	0.038 [0.038]
 10 ²²	2.064 [2.064]	4.259 [4.259]	0.120 [0.120]
At x=1, and in t	the As-X(x)-system, in which	$E_{\rm gn}(r_{\rm As}, x = 1) = 0.430$)3 eV,
0.4303	4.177 [4.177]	17.45 [17.45]	0.376 [0.376]
2	6.084 [6.084]	37.02 [37.02]	0.515 [0.515]
2.5	7.471 [7.471]	55.81 [55.81]	0.583 [0.583]
3	6.263 [6.263]	39.23 [39.23]	0.525 [0.525]
3.5	3.699 [3.699]	13.68 [13.68]	0.330 [0.330]
4	3.996 [3.996]	15.97 [15.97]	0.360 [0.360]
4.5	4.640 [4.640]	21.53 [21.53]	0.416 [0.416]
5	1.535 [1.535]	2.36 [2.36]	0.044 [0.044]
5.5	-0.312 [-0.312]	0.097 [0.097]	3.639 [3.639]
6	0.077 [0.077]	0.006 [0.006]	0.733 [0.733]

E in eV $n_{O[E]}^{MIT}$ $\epsilon_{1.0[E]}^{MIT}$ $\epsilon_{1.0[E]}^{MIT}$ $\epsilon_{O[E]}^{MIT}$ $\epsilon_{O[E]}^$				
At $x=0$, and in the Sn-X(x)-system, in which $E_{gn}(\Gamma_{Sn}, x=0)=1.4291 \text{ eV},$ 1.4291 3.155 [3.155] 9.96 [9.96] 0.269 [0.269] 2 3.634 [3.634] 13.20 [13.20] 0.323 [0.323] [0.25] 2.5 4.359 [4.359] 19.00 [19.00] 0.393 [0.393] 3.3 4.315 [4.315] 18.62 [18.62] 0.389 [0.389] 3.5 3.358 [3.358] 11.27 [11.27] 0.293 [0.293] 4.4 3.510 [3.510] 12.32 [12.32] 0.310 [0.310] 4.5 3.889 [3.889] 15.12 [15.12] 0.349 [0.349] [10 ²²	2.141 [2.141]	4.582 [4.582]	0.132 [0.132]
1.4291 3.155 3.155 9.96 9.96 0.269 0.269 0.269 2 3.634 3.634 13.20 13.20 0.323 0.323 2.5 4.359 4.359 19.00 19.00 0.393 0.393 3 4.315 4.315 18.62 18.62 0.389 0.389 3.5 3.358 3.358 3.150 12.32 12.32 0.310 0.310 4.5 3.889 3.889 15.12 15.12 0.349 0.349 5 2.029 2.029 4.11 4.11 0.115 0.115 6 0.905 0.905 0.819 0.819 0.002 0.002 10 ²² 1.741 1.741 3.033 3.033 0.073 0.073 At x=0.5, and in the Sn-X(x)-system, in which Egn (r_{Sn} , x = 0.5) = 0.9318 eV, 0.9318 3.535 3.535 12.50 12.50 0.312 0.312 2 4.631 4.631 21.45 21.45 0.416 0.416 2.5 5.663 5.663 32.07 32.07 0.490 0.499 3 5.138 5.138 26.40 26.40 0.454 0.454 3.5 3.462 3.462 11.99 11.99 0.304 0.304 4.5 4.165 4.165	E in eV	$n_{O[E]}^{MIT}$	$\epsilon_{1\ O[E]}^{MIT}$	$R_{O[E]}^{MIT}$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	At x=0, and in	the Sn-X(x)-system, in which	$E_{gn}(r_{Sn}, x = 0) = 1.4291$	eV,
2.5	1.4291	3.155 [3.155]	9.96 [9.96]	0.269 [0.269]
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2	3.634 [3.634]	13.20 [13.20]	0.323 [0.323]
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	4.359 [4.359]	19.00 [19.00]	0.393 [0.393]
4 3.510 [3.510] 12.32 [12.32] 0.310 [0.310] 4.5 3.889 [3.889] 15.12 [15.12] 0.349 [0.349] 5.5 2.029 [2.029] 4.11 [4.11] 0.115 [0.115] 5.5 0.761 [0.761] 0.579 [0.579] 0.018 [0.018] 6.6 0.905 [0.905] 0.819 [0.819] 0.002 [0.002] 10 ²² 1.741 [1.741] 3.033 [3.033] 0.073 [0.073]	3	4.315 [4.315]	18.62 [18.62]	0.389 [0.389]
4.5 3.889 [3.889] 15.12 [15.12] 0.349 [0.349] 55 2.029 [2.029] 4.11 [4.11] 0.115 [0.115] 5.5 0.761 [0.761] 0.579 [0.579] 0.018 [0.018] 66 0.905 [0.905] 0.819 [0.819] 0.002 [0.002] 10 ²² 1.741 [1.741] 3.033 [3.033] 0.073 [0.073] 0.07	3.5	3.358 [3.358]	11.27 [11.27]	0.293 [0.293]
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4	3.510 [3.510]	12.32 [12.32]	0.310 [0.310]
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	4.5	3.889 [3.889]	15.12 [15.12]	0.349 [0.349]
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	5	2.029 [2.029]	4.11 [4.11]	0.115 [0.115]
10 ²² 1.741 [1.741] 3.033 [3.033] 0.073 [0.073] At x=0.5, and in the Sn-X(x)-system, in which $E_{gn}(r_{Sn}, x=0.5)=0.9318$ eV, 0.9318 3.535 [3.535] 12.50 [12.50] 0.312 [0.312] 2 4.631 [4.631] 21.45 [21.45] 0.416 [0.416] 2.5 5.663 [5.663] 32.07 [32.07] 0.490 [0.490] 3 5.138 [5.138] 26.40 [26.40] 0.454 [0.454] 3.5 3.462 [3.462] 11.99 [11.99] 0.304 [0.304] 4 3.670 [3.670] 13.47 [13.47] 0.327 [0.327] 4.5 4.165 [4.165] 17.35 [17.35] 0.375 [0.375] 5 1.720 [1.720] 2.96 [2.96] 0.070 [0.070] 5.5 0.172 [0.172] 0.029 [0.029] 0.499 [0.499] 6 0.425 [0.425] 0.181 [0.181] 0.163 [0.163] 10 ²² 1.811 [1.811] 3.281 [3.281] 0.083 [0.083] At x=1, and in the Sn-X(x)-system, in which $E_{gn}(r_{Sn}, x=1)=0.4344$ eV, 0.4344 3.912 [3.912] 15.315 [15.31] 0.351 [0.351] 2 5.812 [5.812] 33.78 [33.78] 0.499 [0.499] 3.5 7.196 [7.196] 51.78 [51.78] 0.571 [0.571] 3 5.995 [5.995] 35.94 [35.94] 0.510 [0.510] 3.5 3.438 [3.438] 11.82 [11.82] 0.302 [0.302] 4.5 4.377 [4.377] 19.16 [19.16] 0.394 [0.394] 5.5 1.278 [1.278] 1.63 [1.63] 0.015 [0.015] 5.5 -0.566 [-0.566] 0.321 [0.321] 13.06 [13.06] 6 -0.178 [-0.178] 0.032 [0.032] 2.055 [2.055]	5.5	0.761 [0.761]	0.579 [0.579]	0.018 [0.018]
At x=0.5, and in the Sn-X(x)-system, in which $E_{gn}(r_{Sn}, x = 0.5) = 0.9318 \text{ eV}$, 0.9318 $3.535 \mid 3.535 \mid 12.50 \mid 12.50 \mid 0.312 \mid 0.$	6	0.905 [0.905]	0.819 [0.819]	0.002 [0.002]
At x=0.5, and in the Sn-X(x)-system, in which $E_{gn}(r_{Sn}, x = 0.5) = 0.9318 \text{ eV}$, 0.9318 $3.535 \mid 3.535 \mid 12.50 \mid 12.50 \mid 0.312 \mid 0.$				
0.9318 3.535 [3.535] 12.50 [12.50] 0.312 [0.312] 2 4.631 [4.631] 21.45 [21.45] 0.416 [0.416] 2.5 5.663 [5.663] 32.07 [32.07] 0.490 [0.490] 3 5.138 [5.138] 26.40 [26.40] 0.454 [0.454] 3.5 3.462 [3.462] 11.99 [11.99] 0.304 [0.304] 4 3.670 [3.670] 13.47 [13.47] 0.327 [0.327] 4.5 4.165 [4.165] 17.35 [17.35] 0.375 [0.375] 5 1.720 [1.720] 2.96 [2.96] 0.070 [0.070] 5.5 0.172 [0.172] 0.029 [0.029] 0.499 [0.499] 6 0.425 [0.425] 0.181 [0.181] 0.163 [0.163] 10 ²² 1.811 [1.811] 3.281 [3.281] 0.083 [0.083] At x=1, and in the Sn-X(x)-system, in which $E_{gn}(\mathbf{r}_{gn}, \mathbf{r}_{xn}, \mathbf{r}_{xn} = 1) = 0.4344 \text{ eV},$ 0.4344 3.912 [3.912] 15.315 [15.31] 0.351 [0.351] 2 5.812 [5.812] 33.78 [33.78] 0.499 [0.499] 2.5 7.196 [7.196] 51.78 [51.78] 0.571 [0.571] 3	10 ²²	1.741 [1.741]	3.033 [3.033]	0.073 [0.073]
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	At $x=0.5$, and is	n the Sn-X(x)-system, in which	ch $E_{gn}(r_{Sn}, x = 0.5) = 0.9$	318 eV,
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.9318	3.535 [3.535]	12.50 [12.50]	0.312 [0.312]
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2	4.631 [4.631]	21.45 [21.45]	0.416 [0.416]
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2.5	5.663 [5.663]	32.07 [32.07]	0.490 [0.490]
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3	5.138 [5.138]	26.40 [26.40]	0.454 [0.454]
4.5 4.165 [4.165] 17.35 [17.35] 0.375 [0.375] 5 1.720 [1.720] 2.96 [2.96] 0.070 [0.070] 5.5 0.172 [0.172] 0.029 [0.029] 0.499 [0.499] 6 0.425 [0.425] 0.181 [0.181] 0.163 [0.163] 5 1022 1.811 [1.811] 3.281 [3.281] 0.083 [0.083] 1 1022 1.811 [1.811] 3.281 [3.281] 0.083 [0.083] 1 1022 1.812 [3.912] 15.315 [15.31] 0.351 [0.351] 1 1032 1 1032 1 1032 1 1032 1 1033 1 1033 1 1033 1 1033 1 1033 1 1033 1 1033 1 1035	3.5	3.462 [3.462]	11.99 [11.99]	0.304 [0.304]
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4	3.670 [3.670]	13.47 [13.47]	0.327 [0.327]
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4.5	4.165 [4.165]	17.35 [17.35]	0.375 [0.375]
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	5	1.720 [1.720]	2.96 [2.96]	0.070 [0.070]
1.811 [1.811] 3.281 [3.281] 0.083 [0.083] At $x=1$, and in the Sn-X(x)-system, in which $E_{gn}(r_{Sn}, x=1)=0.4344$ eV, 0.4344 3.912 [3.912] 15.315 [15.31] 0.351 [0.351] 2 5.812 [5.812] 33.78 [33.78] 0.499 [0.499] 2.5 7.196 [7.196] 51.78 [51.78] 0.571 [0.571] 3 5.995 [5.995] 35.94 [35.94] 0.510 [0.510] 3.5 3.438 [3.438] 11.82 [11.82] 0.302 [0.302] 4 3.735 [3.735] 13.95 [13.95] 0.334 [0.334] 4.5 4.377 [4.377] 19.16 [19.16] 0.394 [0.394] 5 1.278 [1.278] 1.63 [1.63] 0.015 [0.015] 5.5 -0.566 [-0.566] 0.321 [0.321] 13.06 [13.06] 6 -0.178 [-0.178] 0.032 [0.032] 2.055 [2.055]	5.5	0.172 [0.172]	0.029 [0.029]	0.499 [0.499]
At x=1, and in the Sn-X(x)-system, in which $E_{gn}(r_{Sn}, x = 1) = 0.4344 \text{ eV}$, 0.4344 0.3912 [3.912] 0.351 [0.351] 0.499 [0.499] 0.499 [0.499] 0.599 [0.499] 0.599 [0.571] 0.599 [0.571] 0.599 [0.571] 0.599 [0.571] 0.599 [0.5995] 0.599	6	0.425 [0.425]	0.181 [0.181]	0.163 [0.163]
At x=1, and in the Sn-X(x)-system, in which $E_{gn}(r_{Sn}, x = 1) = 0.4344 \text{ eV}$, 0.4344 0.434		101111011	2.204 (2.204)	0.000 to 000
0.4344 3.912 [3.912] 15.315 [15.31] 0.351 [0.351] 2 5.812 [5.812] 33.78 [33.78] 0.499 [0.499] 2.5 7.196 [7.196] 51.78 [51.78] 0.571 [0.571] 3 5.995 [5.995] 35.94 [35.94] 0.510 [0.510] 3.5 3.438 [3.438] 11.82 [11.82] 0.302 [0.302] 4 3.735 [3.735] 13.95 [13.95] 0.334 [0.334] 4.5 4.377 [4.377] 19.16 [19.16] 0.394 [0.394] 5 1.278 [1.278] 1.63 [1.63] 0.015 [0.015] 5.5 -0.566 [-0.566] 0.321 [0.321] 13.06 [13.06] 6 -0.178 [-0.178] 0.032 [0.032] 2.055 [2.055]	1022	1.811 [1.811]	3.281 [3.281]	0.083 [0.083]
2 5.812 [5.812] 33.78 [33.78] 0.499 [0.499] 2.5 7.196 [7.196] 51.78 [51.78] 0.571 [0.571] 3 5.995 [5.995] 35.94 [35.94] 0.510 [0.510] 3.5 3.438 [3.438] 11.82 [11.82] 0.302 [0.302] 4 3.735 [3.735] 13.95 [13.95] 0.334 [0.334] 4.5 4.377 [4.377] 19.16 [19.16] 0.394 [0.394] 5 1.278 [1.278] 1.63 [1.63] 0.015 [0.015] 5.5 -0.566 [-0.566] 0.321 [0.321] 13.06 [13.06] 6 -0.178 [-0.178] 0.032 [0.032] 2.055 [2.055]	At x=1, and in	the Sn-X(x)-system, in which	$E_{gn}(r_{Sn}, x = 1) = 0.4344$	eV,
2.5 7.196 [7.196] 51.78 [51.78] 0.571 [0.571] 3 5.995 [5.995] 35.94 [35.94] 0.510 [0.510] 3.5 3.438 [3.438] 11.82 [11.82] 0.302 [0.302] 4 3.735 [3.735] 13.95 [13.95] 0.334 [0.334] 4.5 4.377 [4.377] 19.16 [19.16] 0.394 [0.394] 5 1.278 [1.278] 1.63 [1.63] 0.015 [0.015] 5.5 -0.566 [-0.566] 0.321 [0.321] 13.06 [13.06] 6 -0.178 [-0.178] 0.032 [0.032] 2.055 [2.055]	0.4344	3.912 [3.912]	15.315 [15.31]	0.351 [0.351]
3 5.995 [5.995] 35.94 [35.94] 0.510 [0.510] 3.5 3.438 [3.438] 11.82 [11.82] 0.302 [0.302] 4 3.735 [3.735] 13.95 [13.95] 0.334 [0.334] 4.5 4.377 [4.377] 19.16 [19.16] 0.394 [0.394] 5 1.278 [1.278] 1.63 [1.63] 0.015 [0.015] 5.5 -0.566 [-0.566] 0.321 [0.321] 13.06 [13.06] 6 -0.178 [-0.178] 0.032 [0.032] 2.055 [2.055]	2	5.812 [5.812]	33.78 [33.78]	0.499 [0.499]
3.5 3.438 [3.438] 11.82 [11.82] 0.302 [0.302] 4 3.735 [3.735] 13.95 [13.95] 0.334 [0.334] 4.5 4.377 [4.377] 19.16 [19.16] 0.394 [0.394] 5 1.278 [1.278] 1.63 [1.63] 0.015 [0.015] 5.5 -0.566 [-0.566] 0.321 [0.321] 13.06 [13.06] 6 -0.178 [-0.178] 0.032 [0.032] 2.055 [2.055]	2.5	7.196 [7.196]	51.78 [51.78]	0.571 [0.571]
4 3.735 [3.735] 13.95 [13.95] 0.334 [0.334] 4.5 4.377 [4.377] 19.16 [19.16] 0.394 [0.394] 5 1.278 [1.278] 1.63 [1.63] 0.015 [0.015] 5.5 -0.566 [-0.566] 0.321 [0.321] 13.06 [13.06] 6 -0.178 [-0.178] 0.032 [0.032] 2.055 [2.055]	3	5.995 [5.995]	35.94 [35.94]	0.510 [0.510]
4.5 4.377 [4.377] 19.16 [19.16] 0.394 [0.394] 5 1.278 [1.278] 1.63 [1.63] 0.015 [0.015] 5.5 -0.566 [-0.566] 0.321 [0.321] 13.06 [13.06] 6 -0.178 [-0.178] 0.032 [0.032] 2.055 [2.055]	3.5	3.438 [3.438]	11.82 [11.82]	0.302 [0.302]
5 1.278 [1.278] 1.63 [1.63] 0.015 [0.015] 5.5 -0.566 [-0.566] 0.321 [0.321] 13.06 [13.06] 6 -0.178 [-0.178] 0.032 [0.032] 2.055 [2.055]	4	3.735 [3.735]	13.95 [13.95]	0.334 [0.334]
5.5 -0.566 [-0.566] 0.321 [0.321] 13.06 [13.06] 6 -0.178 [-0.178] 0.032 [0.032] 2.055 [2.055]	4.5	4.377 [4.377]	19.16 [19.16]	0.394 [0.394]
6 -0.178 [-0.178] 0.032 [0.032] 2.055 [2.055]	5	1.278 [1.278]	1.63 [1.63]	0.015 [0.015]
	5.5	-0.566 [-0.566]	0.321 [0.321]	13.06 [13.06]
	6	-0.178 [-0.178]	0.032 [0.032]	2.055 [2.055]

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10²² 1.879 [1.879] 3.530 [3.530] 0.093 [0.093]

Table 4p: For T=0K and N=N_{CDp}(r_a , x), and for given x and r_d , the numerical results of $n_{O[E]}^{N-MIT}$, $\epsilon_{1\ O[E]}^{N-MIT}$ and $R_{O[E]}^{N-MIT}$ are obtained, using Equations (17, 16), suggesting that, for a given E, they are found to be the same, since $E_{gp1} = E_{gp2} = E_{gp}$.

E in eV	$n_{O[E]}^{N-MIT}$	$\epsilon_{1 \ O[E]}^{N-MIT}$	$R_{O[E]}^{N-MIT}$
At x=0, and in	the Mg-X(x)-system, in whic	$h E_{gp}(r_{Mg}, x = 0) = 1.42$	237 eV,
1.4237	3.429 [3.429]	11.76 [11.76]	0.301 [0.301]
2	3.913 [3.913]	15.09 [15.09]	0.349 [0.349]
2.5	4.641 [4.641]	21.54 [21.54]	0.417 [0.417]
3	4.594 [4.594]	21.10 [21.10]	0.413 [0.413]
3.5	3.629 [3.629]	13.17 [13.17]	0.322 [0.322]
4	3.781 [3.781]	14.30 [14.30]	0.338 [0.338]
4.5	4.161 [4.161]	17.32 [17.32]	0.375 [0.375]
5	2.295 [2.295]	5.27 [5.27]	0.154 [0.154]
5.5	1.024 [1.024]	1.049 [1.049]	$1.4 \times 10^{-4} [1.4 \times 10^{-4}]$
6	1.170 [1.170]	1.369 [1.369]	$6.1 \times 10^{-3} \ [6.1 \times 10^{-3}]$
10 ²²	2.012 [2.012]	4.047 [4.047]	0.113 [0.113]
At x=0.5, and i	n the Mg-X(x)-system, in wh	$ich E_{gp}(r_{Mg}, x = 0.5) =$	0.9268 eV,
0.9268	3.819 [3.819]	14.59 [14.59]	0.342 [0.342]
2	4.922 [4.922]	24.23 [24.23]	0.439 [0.439]
2.5	5.958 [5.958]	35.49 [35.49]	0.508 [0.508]
3	5.427 [5.427]	29.45 [29.45]	0.474 [0.474]
3.5	3.743 [3.743]	14.01 [14.01]	0.334 [0.334]
4	3.952 [3.952]	15.62 [15.62]	0.355 [0.355]
4.5	4.448 [4.448]	19.78 [19.78]	0.400 [0.400]
5	1.996 [1.996]	3.98 [3.98]	0.110 [0.110]
5.5	0.445 [0.445]	0.198 [0.198]	0.147 [0.147]
6	0.700 [0.700]	0.490 [0.490]	0.031 [0.031]
•••			
10 ²²	2.092 [2.092]	4.378 [4.378]	0.125 [0.125]
At x=1, and in	the Mg-X(x)-system, in whic	h $E_{gp}(r_{Mg}, x = 1) = 0.42$	299 eV,
0.4299	4.207 [4.207]	17.70 [17.70]	0.379 [0.379]
2	6.115 [6.115]	37.39 [37.39]	0.517 [0.517]
2.5	7.502 [7.502]	56.28 [56.28]	0.585 [0.585]
3	6.294 [6.294]	39.61 [39.61]	0.527 [0.527]
3.5	3.728 [3.728]	13.90 [13.90]	0.333 [0.333]
4	4.026 [4.026]	16.21 [16.21]	0.362 [0.362]
4.5	4.670 [4.670]	21.81 [21.81]	0.419 [0.419]

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5	1.564 [1.564]	2.45 [2.45]	0.048 [0.048]
5.5	-0.283 [-0.283]	0.080 [0.080]	3.205 [3.205]
6	0.106 [0.106]	0.011 [0.011]	0.652 [0.652]
•••			
10^{22}	2.170 [2.170]	4.710 [4.710]	0.136 [0.136]
E in eV	$n_{O-EP[E-OP]}$	$\epsilon_{1O-EP[E-OP]}$	$R_{O-EP[E-OP]}$
At x=0, and in t	the In-X(x)-system, in which	$E_{\rm gp}(r_{\rm In}, x = 0) = 1.424 \epsilon$	V,
1.424	3.425 [3.425]	11.73 [11.73]	0.300 [0.300]
2	3.909 [3.909]	15.28 [15.28]	0.351 [0.351]
2.5	4.637 [4.637]	21.50 [21.50]	0.416 [0.416]
3	4.590 [4.590]	21.06 [21.06]	0.412 [0.412]
3.5	3.625 [3.625]	13.14 [13.14]	0.322 [0.322]
4	3.778 [3.778]	14.27 [14.27]	0.338 [0.338]
4.5	4.158 [4.158]	17.29 [17.29]	0.375 [0.375]
5	2.292 [2.292]	5.25 [5.25]	0.154 [0.154]
5.5	1.021 [1.021]	1.043 [1.043]	$1.1 \times 10^{-4} [1.1 \times 10^{-4}]$
6	1.167 [1.167]	1.361 [1.361]	$5.9 \times 10^{-3} [5.9 \times 10^{-3}]$
•••			
10^{22}	2.008 [2.008]	4.033 [4.033]	0.112 [0.112]
At x=0.5, and in	n the In-X(x)-system. in which	ch $E_{gp}(r_{In}, x = 0.5) = 0.9$	
0.927	3.816 [3.816]	14.56 [14.56]	0.342 [0.342]
2	4.918 [4.918]	24.19 [24.19]	0.438 [0.438]
2.5	5.953 [5.953]	35.44 [35.44]	0.507 [0.507]
3	5.423 [5.423]	29.41 [29.41]	0.474 [0.474]
3.5	3.739 [3.739]	13.98 [13.98]	0.334 [0.334]
4	3.948 [3.948]	15.59 [15.59]	0.355 [0.355]
4.5	4.444 [4.444]	19.75 [19.75]	0.400 [0.400]
5	1.993 [1.993]	3.97 [3.97]	0.110 [0.110]
5.5	0.442 [0.442]	0.196 [0.196]	0.149 [0.149]
6	0.697 [0.697]	0.485 [0.485]	0.032 [0.032]
	F	r 1	
10 ²²	2.089 [2.089]	4.363 [4.363]	0.124 [0.124]
At x=1, and in	the In-X(x)-system, in which	$ch E_{gno}(r_{In}, x = 1) = 0.43$	00 eV,
0.4300	4.203 [4.203]	17.665 [17.665]	0.379 [0.379]
2	6.111 [6.111]	37.34 [37.34]	0.516 [0.516]
2.5	7.498 [7.498]	56.22 [56.22]	0.585 [0.585]
	6.290 [6.290]	39.56 [39.56]	0.526 [0.526]
3			0.020 [0.020]
			0.332 [0.332]
3.5	3.725 [3.725]	13.87 [13.87]	0.332 [0.332] 0.362 [0.362]
3.5 4	3.725 [3.725] 4.022 [4.022]	13.87 [13.87] 16.18 [16.18]	0.362 [0.362]
3 3.5 4 4.5 5	3.725 [3.725]	13.87 [13.87]	

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6	0.103 [0.103]	0.011 [0.011]	0.661 [0.661]
 10 ²²	2.167 [2.167]	4.694 [4.694]	0.136 [0.136]

Table 5. For T=0K and N=2N_{CDn(CDp)} $(r_{d(a)}, x)$, and for given x and $r_{d(a)}$, then from Equations (20a, 20b, 20c and 20d),

one obtains: $\kappa_{O[E]}^{EBT} \left(N^* = N_{CDn(NDp)} \right) \neq 0$, $\epsilon_{2\ O[E]}^{EBT} \left(N^* = N_{CDn(NDp)} \right) \neq 0$, $\sigma_{O[E]}^{EBT} \left(N^* = N_{CDn(NDp)} \right) \neq 0$ and $\alpha_{O[E]}^{EBT} \left(N^* = N_{CDn(NDp)} \right) \neq 0$, suggesting that they increase with increasing $r_{d(a)}$.

Donor		P	As	Sb	Sn	
r _d (nm) [4]	7	0.110	0.118	0.136	0.140	
At x=0 ,						
$\sigma^{EBT}_{O[E]}(\tfrac{\scriptscriptstyle 1}{\Omega\times cm})$	7	117.6 [97.74]	120.4 [100.1]	147.2 [122.3]	156.3 [130.0]	
$\kappa_{\rm O[E]}^{\rm EBT}\times 10^4$	7	9.100 [7.580]	9.616 [8.011]	15.19 [12.67]	17.42 [14.54]	
$\epsilon_{2~O[E]}^{EBT} \times 10^{3}$	7	6.255 [5.215]	6.564 [5.473]	9.790 [8.176]	11.04 [9.229]	
$\alpha_{O[E]}^{EBT} \left(\frac{1}{cm}\right)$	7	129.6 [107.6]	136.9 [113.7]	216.4 [179.7]	248.4 [206.2]	
At x=0.5 ,						
$\sigma^{EBT}_{O[E]}(\tfrac{_1}{\Omega\times cm})$	7	125.1 [97.96]	128.2 [100.3]	156.6 [122.6]	166.4 [130.2]	
$\kappa_{\rm O[E]}^{\rm EBT}\times 10^4$	1	12.43 [9.764]	13.12 [10.31]	20.64 [16.25]	23.65 [18.63]	
$\epsilon_{2~O[E]}^{EBT} \times 10^3$	7	9.511 [7.478]	9.980 [7.849]	14.88 [11.73]	16.78 [13.24]	
$\alpha_{O[E]}^{EBT} \left(\frac{1}{cm}\right)$	7	114.4 [89.53]	120.9 [94.57]	190.3 [148.8]	218.2 [170.6]	
At x=1 ,						
$\sigma^{EBT}_{O[E]}(\tfrac{_1}{\Omega\times cm})$	7	137.7 [98.14]	141.1 [100.5]	172.4 [122.8]	183.2 [130.5]	
$\kappa_{\mathrm{O[E]}}^{\mathrm{EBT}} \times 10^{4}$	7	25.44 [18.28]	26.85 [19.31]	42.03 [30.36]	48.06 [34.79]	
$\epsilon_{2~O[E]}^{EBT} \times 10^3$	7	21.44 [15.42]	22.49 [16.18]	33.48 [24.21]	37.73 [27.34]	
$\alpha_{O[E]}^{EBT} \left(\frac{1}{cm}\right)$	7	106.4 [75.74]	112.3 [79.97]	176.2 [125.5]	201.9 [143.7]	
Acceptor		Ga	Mg	In	Cd	
r _a (nm)	7	0.126	0.140	0.144	0.148	
At x=0 ,						
$\sigma^{EBT}_{O[E]}(\tfrac{_{10}{^4}}{_{\Omega\times cm}})$	7	1.190 [0.059]	1.274 [0.063]	1.278 [0.063]	1.282 [0.064]	
$\kappa_{\mathrm{O[E]}}^{\mathrm{EBT}}$	7	0.082 [0.0038]	0.097 [0.0044]	0.098 [0.0045]	0.099 [0.0046]	
$\epsilon_{2~O[E]}^{EBT}$	7	0.552 [0.027]	0.632 [0.031]	0.637 [0.032]	0.641 [0.032]	
$\alpha_{O[E]}^{EBT} \left(\frac{10^3}{cm}\right)$	7	9.971 [0.466]	11.01 [0.509]	11.06 [0.512]	18.01 [0.832]	
At v=0.5						

At x=0.5,

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$\sigma^{EBT}_{O[E]}({\scriptstyle_{\underline{\Omega\times cm}}})$	7	0.567 [0.044]	0.607 [0.047]	0.609 [0.047]	0.611 [0.047]
$\kappa_{{ m O[E]}}^{ m EBT}$	7	0.029 [0.0021]	0.034 [0.0025]	0.034 [0.0025]	0.034 [0.0025]
$\epsilon_{2~O[E]}^{EBT}$	7	0.243 [0.019]	0.278 [0.021]	0.280 [0.022]	0.282 [0.022]
$\alpha_{0[E]}^{EBT} \left(\frac{10^3}{cm}\right)$	7	3.485 [0.260]	3.815 [0.283]	3.833 [0.284]	6.236 [0.463]
At x=1 ,					
$\sigma^{EBT}_{O[E]}(\tfrac{_{10}{^4}}{_{\Omega\times cm}})$	7	0.245 [0.030]	0.262 [0.033]	0.263 [0.033]	0.264 [0.033]
$\kappa_{\mathrm{O[E]}}^{\mathrm{EBT}}$	7	0.009 [0.0011]	0.011 [0.0013]	0.011 [0.0013]	0.011 [0.0013]
$\epsilon_{2\ O[E]}^{EBT}$	7	0.098 [0.012]	0.112 [0.014]	0.113 [0.014]	0.113 [0.014]
$\alpha_{O[E]}^{EBT} \left(\frac{10^3}{cm}\right)$	7	1.132 [0.139]	1.232 [0.150]	1.237 [0.151]	2.012 [0.246]

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For $\mathbf{r_d} = \mathbf{r_{As}}$,

Table 6n. In the X(x)-system, at E=3.2 eV and T=20 K, for given r_d and x, the numerical results of $n_{O[E]}(E)$, $\kappa_{O[E]}(E)$, $\epsilon_{1O[E]}(E)$ and $\epsilon_{2O[E]}(E)$, are obtained, as functions of N, by using Equations (17, 19b, 19c and 16), respectively, noting that, with increasing N, $\eta_{o[E]}$ increases [increases], and $E_{gn1\ O[E]}$ increases [decreases], respectively.

N $(10^{18} \text{ cm}^{-3})$ 7	15	26	60	100

$\eta_{o[E]} \gg 1$				
	192.6 [166.9]	278.0 [240.9]	485.7 [420.9]	682.8 [591.7]
E _{gn1 O[E]} in eV	1.41 [1.08]	1.46 [0.98]	1.61 [0.77]	1.77 [0.60]
n _{O[E]}	4.23 [4.52]	4.19[4.61]	4.05 [4.78]	3.88 [4.92]
$\kappa_{\mathrm{O[E]}}$	0.07 [0.05]	0.12 [0.08]	0.27[0.18]	0.46 [0.28]
ε _{10[E]}	17.91 [20.48]	17.52 [21.2]	16.29 [22.81]	14.89 [24.09]
ε _{20[E]}	0.61 [0.47]	1.01 [0.79]	2.21 [1.71]	3.58 [2.76]
For $\mathbf{r_d} = \mathbf{r_{Sn}},$				
$\eta_{o[E]} \gg 1$	192.3 [166.6]	277.8 [240.7]	485.5 [420.7]	682.7 [591.5]
E _{gn1 O[E]} in eV	1.47 [1.14]	1.54 [1.06]	1.73 [0.89]	1.93 [0.76]
n _{O[E]}	3.93 [4.23]	3.87 [4.30]	3.69 [4.44]	3.49 [4.55]
$\kappa_{\mathrm{O[E]}}$	0.06 [0.05]	0.11 [0.07]	0.24[0.16]	0.41 [0.24]
ε _{10[E]}	15.47 [17.9]	14.97 [18.5]	13.54 [19.67]	11.99 [20.65]
ε _{20[E]}	0.50 [0.39]	0.83 [0.65]	1.80 [1.39]	2.89 [2.24]

$\eta_{o[E]}\gg 1$	186.0 [153.9]	268.5 [222.1]	469.1 [388.1]	659.5 [545.6]
$E_{gn1\ O[E]}$ in eV	0.91 [0.59]	0.95 [0.49]	1.09 [0.29]	1.25 [0.12]
n _{O[E]}	4.75 [5.00]	4.71 [5.08]	4.59 [5.23]	4.46 [5.35]
$\kappa_{\mathrm{O[E]}}$	0.06 [0.04]	0.11 [0.07]	0.24 [0.15]	0.40 [0.24]
ε _{10[E]}	22.57 [25.04]	22.21 [25.8]	21.05 [27.3]	19.72 [28.5]
ε _{20[E]}	0.61 [0.43]	1.01 [0.72]	2.22 [1.57]	3.58 [2.54]
For $\mathbf{r_d} = \mathbf{r_{Sn}}$,				
$ \eta_{o[E]} \gg 1 $	185.7 [153.7]	268.3 [222.0]	468.9 [388.0]	659.4 [545.5]
E _{gn1 O[E]} in eV	0.97 [0.65]	1.03 [0.57]	1.21 [0.41]	1.40 [0.27]
n _{O[E]}	4.45 [4.70]	4.39 [4.76]	4.24 [4.89]	4.07 [4.99]
$\varsigma_{\mathrm{O[E]}}$	0.06 [0.04]	0.09 [0.06]	0.21 [0.13]	0.36 [0.21]
E _{10[E]}	19.78 [22.1]	19.30 [22.7]	17.91 [23.9]	16.41 [24.84]
² 20[E]	0.50 [0.36]	0.83 [0.59]	1.80 [1.28]	2.90 [2.06]
At x=1				
For $\mathbf{r_d} = \mathbf{r_{As}}$,				
$\eta_{o[E]} \gg 1$	185.6 [142.8]	267.9 [206.1]	468.1 [360.1]	658.1 [506.2]
E _{gn1 O[E]} in eV	0.42 [0.10]	0.46 [0.004]	0.60 [-0.199]	0.76 [-0.37]
ı _{O[E]}	5.21 [5.44]	5.18 [5.50]	5.07 [5.63]	4.95 [5.74]
^C O[E]	0.06 [0.04]	0.10 [0.06]	0.23 [0.13]	0.38 [0.20]
10[E]	27.17 [29.5]	26.81 [30.2]	25.67 [31.7]	24.3 [32.9]
² 20[E]	0.64 [0.40]	1.07 [0.67]	2.34 [1.46]	3.79 [2.35]
For $\mathbf{r_d} = \mathbf{r_{Sn}}$,				
$ \eta_{o[E]} \gg 1 $	185.3 [142.6]	267.7 [205.9]	467.9 [359.9]	657.9 [506.1]
E _{gn1 O[E]} in eV	0.48 [0.16]	0.54 [0.085]	0.72 [-0.077]	0.91 [-0.21]
O[E]	4.90 [5.13]	4.86 [5.18]	4.71 [5.29]	4.56 [5.38]
O[E]	0.05 [0.03]	0.09 [0.05]	0.20 [0.11]	0.33 [0.18]
10[E]	24.06 [26.3]	23.58 [26.9]	22.20 [28.0]	20.69 [28.9]
20[E]	0.53 [0.33]	0.87 [0.55]	1.90 [1.19]	3.06 [1.91]
N $(10^{18} \text{ cm}^{-3})$ /	15	26	60	100

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Table 6p. In the X(x)-system, at E=3.2 eV and T=20 K, for given r_a and x, the numerical results of $n_{O[E]}(E)$, $\kappa_{O[E]}(E)$, $\epsilon_{1O[E]}(E)$ and $\epsilon_{2O[E]}(E)$, are obtained, as functions of N, by using Equations (17, 19b, 19c and 16), respectively, noting that, with increasing N, $\eta_{o[E]}$ increases [increases], and $E_{gp1\ O[E]}$ increases [decreases], respectively.

For $\mathbf{r_d} = \mathbf{r_{Mg}}$, $\mathbf{r_{0[E]}} \gg 1$	$N (10^{18} \text{ cm}^{-3}) $ /	15	26	60	100	
$\begin{array}{c} n_{o[E]} \gg 1 & 130.5 [17.36] & 228.5 [30.46] & 449.2 [59.94] & 652.3 [87.04] \\ E_{gp1.0[E]} \text{in eV} & 1.631 [1.41] & 1.79 [1.40] & 2.16 [1.39] & 2.50 [1.38] \\ n_{O[E]} & 4.05 [4.26] & 3.89 [4.27] & 3.52 [4.28] & 3.15 [4.29] \\ \kappa_{O[E]} & 0.04 [0.002] & 0.10 [0.004] & 0.29 [0.009] & 0.54 [0.013] \\ E_{10[E]} & 16.42 [18.17] & 15.16 [18.22] & 12.29 [18.31] & 9.61 [18.38] \\ E_{20[E]} & 0.36 [0.02] & 0.79 [0.03] & 2.03 [0.07] & 3.43 [0.12] \\ \end{array}$ $\begin{array}{c} \text{For } \mathbf{r_d} = \mathbf{r_{In}}, \\ n_{O[E]} \gg 1 & 129.8 [17.27] & 227.9 [30.39] & 448.8 [59.88] & 652.0 [87.00] \\ E_{gp1.0[E]} \text{in eV} & 1.630 [1.41] & 1.79 [1.40] & 2.16 [1.39] & 2.50 [1.38] \\ n_{O[E]} & 4.05 [4.26] & 3.89 [4.26] & 3.51 [4.27] & 3.14 [4.28] \\ \kappa_{O[E]} & 0.04 [0.002] & 0.10 [0.004] & 0.29 [0.008] & 0.54 [0.013] \\ E_{10[E]} & 16.40 [18.14] & 15.13 [18.19] & 12.27 [18.28] & 9.59 [18.35] \\ E_{20[E]} & 0.36 [0.02] & 0.78 [0.03] & 2.02 [0.07] & 3.42 [0.11] \\ \end{array}$ $\begin{array}{c} \mathbf{At x=0.5} \\ \mathbf{For } \mathbf{r_d} = \mathbf{r_{Mg}}, \\ n_{O[E]} \gg 1 & 163.2 [28.17] & 249.9 [43.13] & 455.1 [78.59] & 647.8 [111.9] \\ E_{gp1.0[E]} \text{in eV} & 1.18 [0.90] & 1.32 [0.89] & 1.66 [0.87] & 1.97 [0.86] \\ n_{O[E]} & 0.06 [0.003] & 0.11 [0.005] & 0.26 [0.012] & 0.47 [0.02] \\ E_{10[E]} & 0.52 [0.03] & 0.94 [0.05] & 2.17 [0.11] & 3.57 [0.17] \\ \end{array}$ $\begin{array}{c} \mathbf{For } \mathbf{r_d} = \mathbf{r_{In}}, \\ n_{O[E]} \gg 1 & 163.0 [28.12] & 249.7 [43.10] & 455.0 [78.57] & 647.6 [111.8] \\ E_{gp1.0[E]} \text{in eV} & 1.18 [0.90] & 1.32 [0.89] & 1.66 [0.87] & 1.97 [0.86] \\ n_{O[E]} \gg 1 & 163.0 [28.12] & 249.7 [43.10] & 455.0 [78.57] & 647.6 [111.8] \\ E_{gp1.0[E]} \text{in eV} & 1.18 [0.90] & 1.32 [0.89] & 1.66 [0.87] & 1.97 [0.86] \\ n_{O[E]} \text{in eV} & 1.18 [0.90] & 1.32 [0.89] & 1.66 [0.87] & 1.97 [0.86] \\ n_{O[E]} \text{in eV} & 1.18 [0.90] & 1.32 [0.89] & 1.66 [0.87] & 1.97 [0.86] \\ n_{O[E]} \text{in eV} & 1.18 [0.90] & 1.32 [0.89] & 1.66 [0.87] &$	At x=0					
$ \begin{aligned} & \mathbf{E}_{\mathbf{gp1}0[E]} & \text{ in eV} & 1.631 \left[1.41\right] & 1.79 \left[1.40\right] & 2.16 \left[1.39\right] & 2.50 \left[1.38\right] \\ & \mathbf{no}_{[E]} & 4.05 \left[4.26\right] & 3.89 \left[4.27\right] & 3.52 \left[4.28\right] & 3.15 \left[4.29\right] \\ & \mathbf{No}_{[G]} & 0.04 \left[0.002\right] & 0.10 \left[0.004\right] & 0.29 \left[0.009\right] & 0.54 \left[0.013\right] \\ & \mathbf{e}_{20[E]} & 16.42 \left[18.17\right] & 15.16 \left[18.22\right] & 12.29 \left[18.31\right] & 9.61 \left[18.38\right] \\ & \mathbf{e}_{20[E]} & 0.36 \left[0.02\right] & 0.79 \left[0.03\right] & 2.03 \left[0.07\right] & 3.43 \left[0.12\right] \end{aligned} $ $ \begin{aligned} & \mathbf{For} \mathbf{r_d} = \mathbf{r_{In}}, \\ & \mathbf{n_0}_{[E]} \gg 1 & 129.8 \left[17.27\right] & 227.9 \left[30.39\right] & 448.8 \left[59.88\right] & 652.0 \left[87.00\right] \\ & \mathbf{E}_{\mathbf{gp1}0[E]} & \mathbf{in eV} & 1.630 \left[1.41\right] & 1.79 \left[1.40\right] & 2.16 \left[1.39\right] & 2.50 \left[1.38\right] \\ & \mathbf{n_0}_{[E]} & 4.05 \left[4.26\right] & 3.89 \left[4.26\right] & 3.51 \left[4.27\right] & 3.14 \left[4.28\right] \\ & \mathbf{No}_{[E]} & 0.04 \left[0.002\right] & 0.10 \left[0.004\right] & 0.29 \left[0.008\right] & 0.54 \left[0.013\right] \\ & \mathbf{e}_{20[E]} & 16.40 \left[18.14\right] & 15.13 \left[18.19\right] & 12.27 \left[18.28\right] & 9.59 \left[18.35\right] \\ & \mathbf{e}_{20[E]} & 0.36 \left[0.02\right] & 0.78 \left[0.03\right] & 2.02 \left[0.07\right] & 3.42 \left[0.11\right] \end{aligned}$ $\mathbf{At} \mathbf{x} = 0.5$ $\mathbf{For} \mathbf{r_d} = \mathbf{r_{Mg}}, \\ & \mathbf{n_0}_{[E]} \gg 1 & 163.2 \left[28.17\right] & 249.9 \left[43.13\right] & 455.1 \left[78.59\right] & 647.8 \left[111.9\right] \\ & \mathbf{E}_{\mathbf{gp1}0[E]} & \mathbf{in eV} & 1.18 \left[0.90\right] & 1.32 \left[0.89\right] & 1.66 \left[0.87\right] & 1.97 \left[0.86\right] \\ & \mathbf{n_0}_{[E]} & 4.55 \left[4.79\right] & 4.42 \left[4.79\right] & 4.11 \left[4.81\right] & 3.79 \left[4.82\right] \\ & \mathbf{N_0}_{[E]} & 0.06 \left[0.003\right] & 0.11 \left[0.005\right] & 0.26 \left[0.012\right] & 0.47 \left[0.02\right] \\ & \mathbf{e}_{20[E]} & 0.52 \left[0.03\right] & 0.94 \left[0.05\right] & 2.17 \left[0.11\right] & 3.57 \left[0.17\right] \\ & \mathbf{For} \mathbf{r_d} = \mathbf{r_{In}}, \\ & \mathbf{n_0}_{[E]} \gg 1 & 163.0 \left[28.12\right] & 249.7 \left[43.10\right] & 455.0 \left[78.57\right] & 647.6 \left[111.8\right] \\ & \mathbf{E}_{\mathbf{gp1}0[E]} & 1.64 \left[4.78\right] & 4.42 \left[4.79\right] & 4.10 \left[4.80\right] & 3.79 \left[4.81\right] \\ & \mathbf{N_0}_{[E]} & 0.06 \left[0.003\right] & 0.10 \left[0.006\right] & 0.26 \left[0.012\right] & 0.47 \left[0.02\right] \\ & \mathbf{E}_{00[E]} & 0.06 \left[0.003\right] & 0.10 \left[0.006\right] & 0.26 \left[0.012\right] & 0.47 \left[0.02\right] \\ & \mathbf{E}_{00[E]} & 0.06 \left[0.003\right] & 0.10 \left[0.006\right] & 0.26 \left[0.012\right] & 0.47 \left[0.02\right] \\ & \mathbf{E}_{00[E]} & 0.06 \left[0.003\right] & 0.10 \left[0.006\right] & 0.26 \left[0.012\right] & 0.47 \left[$	For $\mathbf{r_d} = \mathbf{r_{Mg}},$					
$\begin{array}{c} \sigma_{0}(F) \\ \sigma_{0$	$\eta_{o[E]}\gg 1$	130.5 [17.36]	228.5 [30.46]	449.2 [59.94]	652.3 [87.04]	
$ \begin{aligned} &\kappa_{O[E]} & 0.04 \left[0.002\right] & 0.10 \left[0.004\right] & 0.29 \left[0.009\right] & 0.54 \left[0.013\right] \\ &\varepsilon_{O[E]} & 16.42 \left[18.17\right] & 15.16 \left[18.22\right] & 12.29 \left[18.31\right] & 9.61 \left[18.38\right] \\ &\varepsilon_{O[E]} & 0.36 \left[0.02\right] & 0.79 \left[0.03\right] & 2.03 \left[0.07\right] & 3.43 \left[0.12\right] \end{aligned} $ For $\mathbf{r_d} = \mathbf{r_{in}}$, $ & & & & & & & & & & & & & & & & & & $	$E_{gp1\ O[E]}$ in eV	1.631 [1.41]	1.79 [1.40]	2.16 [1.39]	2.50 [1.38]	
$\begin{array}{c} \mathbf{\epsilon}_{10[E]} & 16.42 [18.17] & 15.16 [18.22] & 12.29 [18.31] & 9.61 [18.38] \\ \mathbf{\epsilon}_{20[E]} & 0.36 [0.02] & 0.79 [0.03] & 2.03 [0.07] & 3.43 [0.12] \\ \\ \mathbf{For} \mathbf{r_d} = \mathbf{r_{in}}, \\ \mathbf{n}_{0[E]} \gg 1 & 129.8 [17.27] & 227.9 [30.39] & 448.8 [59.88] & 652.0 [87.00] \\ \mathbf{E}_{\text{gp1}} 0[E] \text{in eV} & 1.630 [1.41] & 1.79 [1.40] & 2.16 [1.39] & 2.50 [1.38] \\ \mathbf{n}_{0[E]} & 4.05 [4.26] & 3.89 [4.26] & 3.51 [4.27] & 3.14 [4.28] \\ \mathbf{x}_{0[E]} & 0.04 [0.002] & 0.10 [0.004] & 0.29 [0.008] & 0.54 [0.013] \\ \mathbf{\epsilon}_{10[E]} & 16.40 [18.14] & 15.13 [18.19] & 12.27 [18.28] & 9.59 [18.35] \\ \mathbf{\epsilon}_{20[E]} & 0.36 [0.02] & 0.78 [0.03] & 2.02 [0.07] & 3.42 [0.11] \\ \\ \mathbf{At} \mathbf{x} = 0.5 & & & & & & & & & & & \\ \mathbf{For} $	n _{O[E]}	4.05 [4.26]	3.89 [4.27]	3.52 [4.28]	3.15 [4.29]	
$\begin{aligned} & \varepsilon_{20[E]} & 0.36 [0.02] & 0.79 [0.03] & 2.03 [0.07] & 3.43 [0.12] \\ & & For \mathbf{r_d} = \mathbf{r_{In}}, \\ & & & & & & & & & & & & & & & & & & $	$\kappa_{O[E]}$	0.04 [0.002]	0.10 [0.004]	0.29 [0.009]	0.54 [0.013]	
For $\mathbf{r_d} = \mathbf{r_{In}}$, $\mathbf{r_{0[E]}} \gg 1$	$\varepsilon_{10[E]}$	16.42 [18.17]	15.16 [18.22]	12.29 [18.31]	9.61 [18.38]	
$\begin{array}{c} \eta_{o[E]} \gg 1 & 129.8 [17.27] & 227.9 [30.39] & 448.8 [59.88] & 652.0 [87.00] \\ E_{gp10[E]} \text{in eV} & 1.630 [1.41] & 1.79 [1.40] & 2.16 [1.39] & 2.50 [1.38] \\ \eta_{O[E]} & 4.05 [4.26] & 3.89 [4.26] & 3.51 [4.27] & 3.14 [4.28] \\ Ko_{O[E]} & 0.04 [0.002] & 0.10 [0.004] & 0.29 [0.008] & 0.54 [0.013] \\ \epsilon_{10[E]} & 16.40 [18.14] & 15.13 [18.19] & 12.27 [18.28] & 9.59 [18.35] \\ \epsilon_{20[E]} & 0.36 [0.02] & 0.78 [0.03] & 2.02 [0.07] & 3.42 [0.11] \\ \hline \textbf{At x=0.5} \\ \hline \textbf{For } \textbf{r_d} = \textbf{r_{Mg}}, \\ \eta_{O[E]} \gg 1 & 163.2 [28.17] & 249.9 [43.13] & 455.1 [78.59] & 647.8 [111.9] \\ E_{gp10[E]} \text{in eV} & 1.18 [0.90] & 1.32 [0.89] & 1.66 [0.87] & 1.97 [0.86] \\ \eta_{O[E]} & 4.55 [4.79] & 4.42 [4.79] & 4.11 [4.81] & 3.79 [4.82] \\ \aleph_{O[E]} & 0.06 [0.003] & 0.11 [0.005] & 0.26 [0.012] & 0.47 [0.02] \\ \epsilon_{10[E]} & 20.68 [22.91] & 19.55 [22.97] & 16.80 [23.10] & 14.16 [23.21] \\ \epsilon_{20[E]} & 0.52 [0.03] & 0.94 [0.05] & 2.17 [0.11] & 3.57 [0.17] \\ \hline \textbf{For } \textbf{r_d} = \textbf{r_{m}}, \\ \eta_{O[E]} \gg 1 & 163.0 [28.12] & 249.7 [43.10] & 455.0 [78.57] & 647.6 [111.8] \\ E_{gp10[E]} \text{in eV} & 1.18 [0.90] & 1.32 [0.89] & 1.66 [0.87] & 1.97 [0.86] \\ \eta_{O[E]} & 0.06 [0.003] & 0.10 [0.006] & 0.26 [0.012] & 0.47 [0.02] \\ \epsilon_{10[E]} & 0.06 [0.003] & 0.10 [0.006] & 0.26 [0.012] & 0.47 [0.02] \\ \epsilon_{10[E]} & 0.06 [0.003] & 0.10 [0.006] & 0.26 [0.012] & 0.47 [0.02] \\ \epsilon_{10[E]} & 20.65 [22.87] & 19.52 [22.93] & 16.8 [23.06] & 14.13 [23.17] \\ \hline \end{array}$	ε _{20[E]}	0.36 [0.02]	0.79 [0.03]	2.03 [0.07]	3.43 [0.12]	
	For $\mathbf{r_d} = \mathbf{r_{In}},$					
$\begin{array}{c} \mathbf{n}_{0[E]} \\ \mathbf{n}_{0} \\ \mathbf{n}_{0[E]} \\ \mathbf{n}_{0} \\ $	$\eta_{o[E]}\gg 1$	129.8 [17.27]	227.9 [30.39]	448.8 [59.88]	652.0 [87.00]	
$\kappa_{0[E]} = 0.04 [0.002] = 0.10 [0.004] = 0.29 [0.008] = 0.54 [0.013]$ $\varepsilon_{10[E]} = 16.40 [18.14] = 15.13 [18.19] = 12.27 [18.28] = 9.59 [18.35]$ $\varepsilon_{20[E]} = 0.36 [0.02] = 0.78 [0.03] = 2.02 [0.07] = 3.42 [0.11]$ $At $	E _{gp1 O[E]} in eV	1.630 [1.41]	1.79 [1.40]	2.16 [1.39]	2.50 [1.38]	
$ \begin{split} & \epsilon_{\text{IO[E]}} & 16.40 [18.14] & 15.13 [18.19] & 12.27 [18.28] & 9.59 [18.35] \\ & \epsilon_{\text{2O[E]}} & 0.36 [0.02] & 0.78 [0.03] & 2.02 [0.07] & 3.42 [0.11] \\ & \textbf{At x=0.5} & & & & & & & & \\ & & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & \\ & & & $	n _{O[E]}	4.05 [4.26]	3.89 [4.26]	3.51 [4.27]	3.14 [4.28]	
$\begin{aligned} & \epsilon_{20[E]} & 0.36 [0.02] & 0.78 [0.03] & 2.02 [0.07] & 3.42 [0.11] \\ & \mathbf{At x=0.5} \\ & \\ & \mathbf{For r_d = r_{Mg}}, \\ & \mathbf{n_{0[E]}} \gg 1 & 163.2 [28.17] & 249.9 [43.13] & 455.1 [78.59] & 647.8 [111.9] \\ & \mathbf{E_{gp1 0[E]} in eV} & 1.18 [0.90] & 1.32 [0.89] & 1.66 [0.87] & 1.97 [0.86] \\ & \mathbf{n_{0[E]}} & 4.55 [4.79] & 4.42 [4.79] & 4.11 [4.81] & 3.79 [4.82] \\ & \mathbf{\kappa_{0[E]}} & 0.06 [0.003] & 0.11 [0.005] & 0.26 [0.012] & 0.47 [0.02] \\ & \mathbf{\epsilon_{10[E]}} & 20.68 [22.91] & 19.55 [22.97] & 16.80 [23.10] & 14.16 [23.21] \\ & \mathbf{\epsilon_{20[E]}} & 0.52 [0.03] & 0.94 [0.05] & 2.17 [0.11] & 3.57 [0.17] \\ & \mathbf{For r_d = r_{In}}, \\ & \mathbf{n_{0[E]}} \gg 1 & 163.0 [28.12] & 249.7 [43.10] & 455.0 [78.57] & 647.6 [111.8] \\ & \mathbf{E_{gp1 0[E]} in eV} & 1.18 [0.90] & 1.32 [0.89] & 1.66 [0.87] & 1.97 [0.86] \\ & \mathbf{n_{0[E]}} & 4.54 [4.78] & 4.42 [4.79] & 4.10 [4.80] & 3.79 [4.81] \\ & \mathbf{\kappa_{0[E]}} & 0.06 [0.003] & 0.10 [0.006] & 0.26 [0.012] & 0.47 [0.02] \\ & \mathbf{\epsilon_{10[E]}} & 20.65 [22.87] & 19.52 [22.93] & 16.8 [23.06] & 14.13 [23.17] \\ \end{aligned}$	$\kappa_{O[E]}$	0.04 [0.002]	0.10 [0.004]	0.29 [0.008]	0.54 [0.013]	
At \mathbf{x} =0.5 For $\mathbf{r_d} = \mathbf{r_{Mg}}$, $\mathbf{n_{0[E]}} \gg 1$	ε _{10[E]}	16.40 [18.14]	15.13 [18.19]	12.27 [18.28]	9.59 [18.35]	
For $\mathbf{r_d} = \mathbf{r_{Mg}}$, $\mathbf{r_{0[E]}} \gg 1$	$\epsilon_{20[E]}$	0.36 [0.02]	0.78 [0.03]	2.02 [0.07]	3.42 [0.11]	
$\begin{array}{llllllllllllllllllllllllllllllllllll$	At x=0.5					
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	For $\mathbf{r_d} = \mathbf{r_{Mg}},$					
$\begin{array}{llllllllllllllllllllllllllllllllllll$	$\eta_{o[E]} \gg 1$	163.2 [28.17]	249.9 [43.13]	455.1 [78.59]	647.8 [111.9]	
$\kappa_{O[E]} = 0.06 [0.003] = 0.11 [0.005] = 0.26 [0.012] = 0.47 [0.02]$ $\epsilon_{1O[E]} = 20.68 [22.91] = 19.55 [22.97] = 16.80 [23.10] = 14.16 [23.21]$ $\epsilon_{2O[E]} = 0.52 [0.03] = 0.94 [0.05] = 2.17 [0.11] = 3.57 [0.17]$ For $\mathbf{r_d} = \mathbf{r_{In}}$, $\eta_{o[E]} \gg 1 = 163.0 [28.12] = 249.7 [43.10] = 455.0 [78.57] = 647.6 [111.8]$ $E_{gp1 O[E]} \text{ in eV} = 1.18 [0.90] = 1.32 [0.89] = 1.66 [0.87] = 1.97 [0.86]$ $\mathbf{n_{O[E]}} = 4.54 [4.78] = 4.42 [4.79] = 4.10 [4.80] = 3.79 [4.81]$ $\kappa_{O[E]} = 0.06 [0.003] = 0.10 [0.006] = 0.26 [0.012] = 0.47 [0.02]$ $\epsilon_{1O[E]} = 20.65 [22.87] = 19.52 [22.93] = 16.8 [23.06] = 14.13 [23.17]$	E _{gp1 O[E]} in eV	1.18 [0.90]	1.32 [0.89]	1.66 [0.87]	1.97 [0.86]	
	n _{O[E]}	4.55 [4.79]	4.42 [4.79]	4.11 [4.81]	3.79 [4.82]	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\kappa_{\mathrm{O[E]}}$	0.06 [0.003]	0.11 [0.005]	0.26 [0.012]	0.47 [0.02]	
For $\mathbf{r_d} = \mathbf{r_{In}}$, $\eta_{o[E]} \gg 1$	$\epsilon_{10[E]}$	20.68 [22.91]	19.55 [22.97]	16.80 [23.10]	14.16 [23.21]	
$\eta_{o[E]} \gg 1$ 163.0 [28.12] 249.7 [43.10] 455.0 [78.57] 647.6 [111.8] $E_{gp1 \ O[E]}$ in eV 1.18 [0.90] 1.32 [0.89] 1.66 [0.87] 1.97 [0.86] $\eta_{O[E]}$ 4.54 [4.78] 4.42 [4.79] 4.10 [4.80] 3.79 [4.81] $\kappa_{O[E]}$ 0.06 [0.003] 0.10 [0.006] 0.26 [0.012] 0.47 [0.02] $\epsilon_{1O[E]}$ 20.65 [22.87] 19.52 [22.93] 16.8 [23.06] 14.13 [23.17]	$\epsilon_{2O[E]}$	0.52 [0.03]	0.94 [0.05]	2.17 [0.11]	3.57 [0.17]	
$E_{gp1 \ O[E]}$ in eV 1.18 [0.90] 1.32 [0.89] 1.66 [0.87] 1.97 [0.86] $n_{O[E]}$ 4.54 [4.78] 4.42 [4.79] 4.10 [4.80] 3.79 [4.81] $\kappa_{O[E]}$ 0.06 [0.003] 0.10 [0.006] 0.26 [0.012] 0.47 [0.02] $\epsilon_{1O[E]}$ 20.65 [22.87] 19.52 [22.93] 16.8 [23.06] 14.13 [23.17]	For $\mathbf{r_d} = \mathbf{r_{In}}$,					
$n_{O[E]}$ 4.54 [4.78] 4.42 [4.79] 4.10 [4.80] 3.79 [4.81] $\kappa_{O[E]}$ 0.06 [0.003] 0.10 [0.006] 0.26 [0.012] 0.47 [0.02] $\epsilon_{1O[E]}$ 20.65 [22.87] 19.52 [22.93] 16.8 [23.06] 14.13 [23.17]	$\eta_{o[E]} \gg 1$	163.0 [28.12]	249.7 [43.10]	455.0 [78.57]	647.6 [111.8]	
$\kappa_{O[E]}$ 0.06 [0.003] 0.10 [0.006] 0.26 [0.012] 0.47 [0.02] $\epsilon_{IO[E]}$ 20.65 [22.87] 19.52 [22.93] 16.8 [23.06] 14.13 [23.17]	$E_{gp1 O[E]}$ in eV	1.18 [0.90]	1.32 [0.89]	1.66 [0.87]	1.97 [0.86]	
$\epsilon_{10[E]}$ 20.65 [22.87] 19.52 [22.93] 16.8 [23.06] 14.13 [23.17]	n _{O[E]}	4.54 [4.78]	4.42 [4.79]	4.10 [4.80]	3.79 [4.81]	
	$\kappa_{O[E]}$	0.06 [0.003]	0.10 [0.006]	0.26 [0.012]	0.47 [0.02]	
$\epsilon_{\text{2O[E]}}$ 0.52 [0.03] 0.93 [0.05] 2.17 [0.11] 3.56 [0.17]	$\epsilon_{10[E]}$	20.65 [22.87]	19.52 [22.93]	16.8 [23.06]	14.13 [23.17]	
	$\epsilon_{2O[E]}$	0.52 [0.03]	0.93 [0.05]	2.17 [0.11]	3.56 [0.17]	

At x=1					
For $\mathbf{r_d} = \mathbf{r_{Mg}},$					
$\eta_{o[E]} \gg 1$	178.2 [41.11]	261.8 [60.41]	463.5 [106.9]	654.2 [151.0]	
$E_{gp1\ O[E]}$ in eV	0.69 [0.38]	0.82 [0.373]	1.14 [0.346]	1.45 [0.323]	
n _{O[E]}	5.03 [5.26]	4.93 [5.27]	4.66 [5.29]	4.38 [5.31]	
$\kappa_{O[E]}$	0.06 [0.005]	0.11 [0.008]	0.25 [0.018]	0.44 [0.028]	
$\epsilon_{10[E]}$	25.33 [27.7]	24.28 [27.8]	21.65 [28.0]	19.03 [28.2]	
$\epsilon_{2O[E]}$	0.62 [0.05]	1.06 [0.09]	2.36 [0.19]	3.85 [0.29]	
For $\mathbf{r_d} = \mathbf{r_{In}},$					
$\eta_{o[E]} \gg 1$	178.1 [41.09]	261.7 [60.39]	463.4 [106.9]	654.2 [151.0]	
E _{gp1 O[E]} in eV	0.69 [0.38]	0.82 [0.373]	1.14 [0.346]	1.45 [0.324]	
n _{O[E]}	5.03 [5.26]	4.92 [5.27]	4.65 [5.29]	4.38 [5.31]	
$\kappa_{O[E]}$	0.06 [0.005]	0.11 [0.008]	0.25 [0.018]	0.44 [0.027]	
$\epsilon_{10[E]}$	25.29 [27.7]	24.24 [27.8]	21.61 [28.0]	19.00 [28.1]	
$\epsilon_{2O[E]}$	0.62 [0.05]	1.06 [0.09]	2.36 [0.19]	3.84 [0.29]	
N (10 ¹⁸ cm ⁻³) ✓	15	26	60	100	

Table 7n. In the X(x)-system, at E=3.2 eV and $N=10^{20} {\rm cm}^{-3}$, for given r_d and x, the numerical results of $n_{O[E]}(E)$, $\kappa_{O[E]}(E)$, $\epsilon_{1O[E]}(E)$ and $\epsilon_{2O[E]}(E)$, are obtained, as functions of T, by using Equations (17, 19b, 19c and 16), respectively, noting that $\eta_{O[E]}$ and $E_{gn1 \ O[E]}$ both decrease with increasing T, respectively.

T /	20 K	50 K	100 K	300 K	
At x=0					
For $\mathbf{r_d} = \mathbf{r_{As}}$,					
$\eta_{o[E]}\gg 1$	682.8 [591.7]	273.1 [236.7]	136.5 [118.3]	45.50 [39.42]	
$E_{gn1\;O[E]}$ in eV	1.77 [0.60]	1.76 [0.59]	1.74 [0.57]	1.61 [0.44]	
n _{O[E]}	3.88 [4.92]	3.89 [4.92]	3.92 [4.94]	4.04 [5.04]	
$\kappa_{O[E]}$	0.46 [0.28]	0.46 [0.28]	0.46 [0.28]	0.44 [0.27]	
$\epsilon_{10[E]}$	14.89 [24.09]	14.96 [24.17]	15.15 [24.35]	16.15 [25.32]	
$\epsilon_{2O[E]}$	3.58 [2.76]	3.58 [2.76]	3.58 [2.76]	3.58 [2.76]	
For $\mathbf{r_d} = \mathbf{r_{Sn}}$,					
$\eta_{o[E]}\gg 1$	682.7 [591.5]	273.1 [236.6]	136.5 [118.3]	45.49 [39.42]	
$E_{gn1\;O[E]}$ in eV	1.93 [0.76]	1.92 [0.75]	1.89 [0.72]	1.76 [0.59]	
$n_{O[E]}$	3.49 [4.55]	3.50 [4.56]	3.52 [4.58]	3.65 [4.68]	
$\kappa_{O[E]}$	0.41 [0.24]	0.41 [0.24]	0.41 [0.24]	0.40 [0.24]	

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$\epsilon_{10[E]}$	11.99 [20.65]	12.06 [20.72]	12.24 [20.90]	13.17 [21.83]
$\epsilon_{20[E]}$	2.89 [2.24]	2.89 [2.24]	2.89 [2.24]	2.89 [2.24]
At x=0.5				
For $\mathbf{r_d} = \mathbf{r_{As}}$,				
$\eta_{o[E]}\gg 1$	659.5 [545.6]	263.8 [218.4]	131.9 [109.1]	43.95 [36.35]
$E_{gn1\ O[E]}$ in eV	1.25 [0.12]	1.24 [0.11]	1.22 [0.09]	1.12 [-0.01]
n _{O[E]}	4.46 [5.35]	4.46 [5.35]	4.48 [5.37]	4.57 [5.43]
$\kappa_{O[E]}$	0.40 [0.24]	0.40 [0.24]	0.40 [0.24]	0.39 [0.23]
$\epsilon_{10[E]}$	19.72 [28.5]	19.78 [28.6]	19.93 [28.7]	20.75 [29.5]
$\epsilon_{2O[E]}$	3.58 [2.54]	3.58 [2.54]	3.58 [2.54]	3.58 [2.54]
For $\mathbf{r_d} = \mathbf{r_{Sn}}$,				
$\eta_{o[E]} \gg 1$	659.4 [545.5]	263.7 [218.2]	131.9 [109.1]	43.94 [36.34]
$E_{gn1\ O[E]}$ in eV	1.40 [0.27]	1.40 [0.26]	1.38 [0.25]	1.27 [0.14]
n _{O[E]}	4.07 [4.99]	4.07 [4.99]	4.09 [5.01]	4.18 [5.08]
$\kappa_{O[E]}$	0.36 [0.21]	0.35 [0.21]	0.35 [0.20]	0.35 [0.20]
$\epsilon_{10[E]}$	16.41 [24.84]	16.46 [24.89]	16.60 [25.02]	17.38 [25.75]
$\epsilon_{20[E]}$	2.90 [2.06]	2.90 [2.06]	2.90 [2.06]	2.89 [2.06]
At x=1				
For $\mathbf{r_d} = \mathbf{r_{As}}$,				
$\eta_{o[E]} \gg 1$	658.1 [506.2]	263.2 [202.5]	131.6 [101.2]	43.85 [33.72]
$E_{gn1\ O[E]}$ in eV	0.76 [-0.37]	0.75 [-0.39]	0.74 [-0.39]	0.66 [-0.46]
n _{O[E]}	4.95 [5.74]	4.95 [5.74]	4.96 [5.75]	5.02 [5.79]
$\kappa_{O[E]}$	0.38 [0.20]	0.38 [0.20]	0.38 [0.20]	0.38 [0.20]
ε _{10[E]}	24.3 [32.9]	24.38 [32.9]	24.48 [33.0]	25.1 [33.5]
$\epsilon_{20[E]}$	3.79 [2.35]	3.79 [2.35]	3.79 [2.35]	3.80 [2.35]
For $\mathbf{r_d} = \mathbf{r_{Sn}}$,				
$\eta_{o[E]} \gg 1$	657.9 [506.1]	263.2 [202.4]	131.6 [101.2]	43.84 [33.72]
$E_{gn1\ O[E]}$ in eV	0.91 [-0.21]	0.91 [-0.22]	0.90 [-0.23]	0.82 [-0.31]
n _{O[E]}	4.56 [5.38]	4.56 [5.38]	4.57 [5.39]	4.64 [5.44]
$\kappa_{O[E]}$	0.33 [0.18]	0.33 [0.18]	0.33 [0.18]	0.33 [0.17]
ε _{10[E]}	20.69 [28.9]	20.72 [28.9]	20.81 [29.0]	21.42 [29.5]
ε _{20[E]}	3.06 [1.91]	3.06 [1.91]	3.06 [1.91]	3.06 [1.91]
		50 K	100 K	300 K

Table 7p. In the X(x)-system, at E=3.2 eV and N = 10^{20} cm⁻³, for given r_a and x, the numerical results of $n_{O[E]}(E)$, $\kappa_{O[E]}(E)$, $\epsilon_{1O[E]}(E)$ and $\epsilon_{2O[E]}(E)$, are obtained, as functions of T, by using Equations (17, 19b, 19c and 16), respectively, noting that $\eta_{o[E]}$ and $E_{gp1 \ O[E]}$ both decrease with increasing T, respectively.

Т 1	20 K	50 K	100 K	300 K
At x=0				
For $\mathbf{r_d} = \mathbf{r_{Mg}}$,				
$\eta_{o[E]}\gg 1$	652.3 [87.04]	260.9 [34.80]	130.4 [17.36]	43.46 [5.65]
E _{gn1 O[E]} in eV	2.50 [1.38]	2.49 [1.37]	2.47 [1.34]	2.34 [1.22]
n _{O[E]}	3.15 [4.29]	3.16 [4.30]	3.18 [4.32]	3.33 [4.43]
$\kappa_{O[E]}$	0.54 [0.013]	0.54 [0.013]	0.54 [0.013]	0.52 [0.014]
ε _{10[E]}	9.61 [18.38]	9.68 [18.46]	9.86 [18.65]	10.8 [19.65]
ε _{20[E]}	3.43 [0.12]	3.43 [0.12]	3.43 [0.12]	3.43 [0.13]
For $\mathbf{r_d} = \mathbf{r_{In}}$,				
$\eta_{o[E]} \gg 1$	652.0 [87.00]	260.8 [3.78]	130.4 [17.35]	43.45 [5.65]
E _{gn1 O[E]} in eV	2.50 [1.38]	2.49 [1.37]	2.47 [1.35]	2.34 [1.22]
n _{O[E]}	3.14 [4.28]	3.15 [4.29]	3.18 [4.31]	3.32 [4.43]
$\kappa_{\mathrm{O[E]}}$	0.54 [0.013]	0.54 [0.013]	0.54 [0.013]	0.51 [0.014]
[€] 10[E]	9.59 [18.35]	9.66 [18.43]	9.84 [18.62]	10.8 [19.62]
20[E]	3.42 [0.11]	3.42 [0.12]	3.42 [0.12]	3.42 [0.13]
At x=0.5				
For $\mathbf{r_d} = \mathbf{r_{Mg}}$,				
$\eta_{o[E]}\gg 1$	647.8 [111.9]	259.1 [44.73]	129.5 [22.34]	43.16 [7.344]
E _{gn1 O[E]} in eV	1.97 [0.86]	1.97 [0.85]	1.95 [0.84]	1.84 [0.73]
¹ 0[E]	3.79 [4.82]	3.80 [4.82]	3.82 [4.84]	3.92 [4.92]
GO[E]	0.47 [0.02]	0.47 [0.018]	0.47 [0.018]	0.46 [0.018]
- 10[E]	14.16 [23.21]	14.22 [23.26]	14.36 [23.41]	15.18 [24.22]
20[E]	3.57 [0.17]	3.57 [0.17]	3.57 [0.17]	3.58 [0.18]
For $\mathbf{r_d} = \mathbf{r_{In}}$,				
$\eta_{o[E]} \gg 1$	647.6 [111.8]	259.0 [44.72]	129.5 [22.33]	43.16 [7.342]
E _{gn1 O[E]} in eV	1.97 [0.86]	1.97 [0.85]	1.95 [0.84]	1.85 [0.73]
1 _{O[E]}	3.79 [4.81]	3.79 [4.82]	3.81 [4.83]	3.92 [4.92]
O[E]	0.47 [0.02]	0.47 [0.018]	0.47 [0.018]	0.45 [0.019]
10[E]	14.13 [23.17]	14.19 [23.23]	14.3 [23.37]	15.15 [24.18]
E _{20[E]}	3.56 [0.17]	3.56 [0.17]	3.56 [0.17]	3.57 [0.18]

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For $\mathbf{r_d} = \mathbf{r_{Mg}}$,				
$\eta_{o[E]}\gg 1$	654.2 [151.0]	261.7 [60.37]	130.8 [30.17]	43.59 [8.981]
$E_{gn1\;O[E]}$ in eV	1.45 [0.323]	1.44 [0.319]	1.43 [0.306]	1.35 [0.228]
$n_{O[E]}$	4.38 [5.31]	4.39 [5.31]	4.40 [5.32]	4.47 [5.38]
$\kappa_{O[E]}$	0.44 [0.028]	0.44 [0.028]	0.44 [0.028]	0.43 [0.028]
$\epsilon_{10[E]}$	19.03 [28.2]	19.07 [28.2]	19.17 [28.3]	19.82 [28.9]
$\epsilon_{2O[E]}$	3.85 [0.29]	3.85 [0.29]	3.85 [0.29]	3.85 [0.30]
For $\mathbf{r_d} = \mathbf{r_{In}}$,				
$\eta_{o[E]} \gg 1$	654.2 [151.0]	261.7 [60.37]	130.8 [30.16]	43.59 [9.981]
$E_{gn1 O[E]}$ in eV	1.45 [0.324]	1.44 [0.319]	1.43 [0.307]	1.35 [0.228]
n _{O[E]}	4.38 [5.31]	4.38 [5.31]	4.40 [5.32]	4.47 [5.37]
$\kappa_{O[E]}$	0.44 [0.027]	0.44 [0.027]	0.44 [0.027]	0.43 [0.028]
ε _{10[E]}	19.00 [28.1]	19.04 [28.2]	19.14 [28.3]	19.79 [28.9]
$\epsilon_{20[E]}$	3.84 [0.29]	3.84 [0.29]	3.84 [0.29]	3.84 [0.30]
T /	20 K	50 K	100 K	300 K

Table 8n: For given x, r_d , and T=(4.2 K and 77 K), the numerical results of $\sigma_{O[E]}$, $\mu_{O[E]}$ and $D_{O[E]}$, expressed respectively in $\left(\frac{10^4}{\text{ohm}\times\text{cm}}, \frac{10^3\times\text{cm}^2}{\text{V}\times\text{s}}, \frac{10^3\times\text{cm}^2}{\text{s}}\right)$, and as functions of N, are obtained by using Equations (20a, 22 and 24), suggesting that, for a given N, they decrease [decrease], with increasing r_d .

Donor	As	Sn
r_d (nm) \nearrow	0.118	0.140
For x=0 and at T=4.2 K		
N (10 ¹⁹ cm ⁻³)		
1	1.757 [1.371], 10.99 [8.578], 1.855 [1.254]	1.118 [0.878], 7.017 [5.510], 1.182 [0.804]
5	7.804 [6.033], 9.747 [7.535], 4.817 [3.227]	4.888 [3.793], 6.109 [4.741], 3.018 [2.029]
10	14.95 [11.53], 9.335 [7.197], 7.325 [4.893]	9.318 [7.206], 5.819 [4.500], 4.565 [3.059]
For x=0.5 and at T=4.2	K	
N (10 ¹⁹ cm ⁻³)		
1	1.897 [1.365], 11.87 [8.545], 1.936 [1.152]	1.279 [1.002], 8.028 [6.291], 1.352 [0.918]
5	8.452 [6.001], 10.55 [7.505], 5.039 [2.964]	5.625 [4.360], 7.030 [5.449], 3.473 [2.332]
10	16.20 [11.48], 10.12 [7.168], 7.668 [4.494]	10.74 [8.299], 6.709 [5.183], 5.263 [3.523]
For x=1 and at T=4.2 K		
N (10 ¹⁹ cm ⁻³)		-
1	2.149 [1.361], 13.45 [8.517], 2.187 [1.066]	1.361 [0.872], 8.542 [5.472], 1.386 [0.683]
5	9.609 [5.988], 12.00 [7.479], 5.716 [2.740]	6.001 [3.766], 7.500 [4.706], 3.571 [1.724]

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10	18.45 [11.44], 11.52 [7.143], 8.708 [4.155]	11.50 [7.153], 7.163 [4.467], 5.415 [2.598]
For x=0 and at T=	=77 K	
$N (10^{19} \text{ cm}^{-3})$		
1	2.965 [2.184], 18.56 [13.67], 3.129 [1.996]	1.890 [1.401], 11.86 [8.793], 1.996 [1.282]
5	8.430 [6.450], 10.53 [8.055], 5.202 [3.499]	5.280 [4.056], 6.599 [5.068], 3.259 [2.169]
10	15.43 [11.84], 9.632 [7.394], 7.557 [5.027]	9.615 [7.404], 6.004 [4.624], 4.710 [3.143]
For x=0.5 and at	T=77 K	
N (10 ¹⁹ cm ⁻³)		
1	3.203 [2.176], 20.05 [13.62], 3.265 [1.834]	2.162 [1.599], 13.57 [10.04], 2.284 [1.463]
5	9.129 [6.424], 11.40 [8.023], 5.442 [3.168]	6.076 [4.661], 7.594 [5.825], 3.751 [2.493]
10	16.72 [11.79], 10.44 [7.364], 7.911 [4.617]	11.08 [8.526], 6.922 [5.325], 5.430 [3.619]
For x=1 and at T=	=77 K	
N (10 ¹⁹ cm ⁻³)		
1	3.627 [2.170], 22.70 [13.58], 3.689 [1.697]	2.301 [1.392], 14.45 [8.740], 2.343 [1.089]
5	10.38 [6.402], 12.96 [7.996], 6.173 [2.929]	6.482 [4.026], 8.102 [5.032], 3.857 [1.842]
10	19.03 [11.75], 11.88 [7.339], 8.985 [4.269]	11.83 [7.349], 7.391 [4.590], 5.587 [2.669]

Table 8p: For given x, r_a , and T=(4.2 K and 77 K), the numerical results of $\sigma_{O[E]}$, $\mu_{O[E]}$ and $D_{O[E]}$, expressed respectively in $\left(\frac{10^4}{\text{ohm}\times\text{cm}}, \frac{10^4\times\text{cm}^2}{\text{V}\times\text{s}}, \frac{10^3\times\text{cm}^2}{\text{s}}\right)$, and as functions of N, are obtained by using Equations (20a, 22 and 24), suggesting that, for a given N, they decrease [decrease] with increasing r_a .

Acceptor	Mg	In
r_a (nm) \nearrow	0.140	0.144
For x=0 and at T=4.2 K		
N (10 ¹⁹ cm ⁻³)		_
3	4.039 [0.166], 1.079 [0.044], 3.213 [0.017]	4.003 [0.164], 1.073 [0.044], 3.187 [0.017]
5	7.184 [0.269], 1.034 [0.039], 4.649 [0.023]	7.129 [0.267], 1.028 [0.038], 4.616 [0.023]
10	14.75 [0.498], 0.986 [0.033], 7.390 [0.033]	14.64 [0.496], 0.980 [0.033], 7.341 [0.033]
For x=0.5 and at T=4.2	K	
N (10 ¹⁹ cm ⁻³)		
3	5.055 [0.283], 1.155 [0.065], 3.686 [0.036]	5.019 [0.282], 1.148 [0.064], 3.661 [0.035]
5	8.443 [0.444], 1.114 [0.058], 5.126 [0.046]	8.386 [0.441], 1.107 [0.058], 5.092 [0.046]
10	16.62 [0.812], 1.066 [0.052], 7.934 [0.067]	16.51 [0.807], 1.059 [0.051], 7.883 [0.066]
For x=1 and at T=4.2 K		
N (10 ¹⁹ cm ⁻³)		
3	6.089 [0.509], 1.306 [0.109], 4.338 [0.084]	6.049 [0.506], 1.298 [0.108], 4.310 [0.083]
5	9.937 [0.795], 1.263 [0.101], 5.946 [0.110]	9.873 [0.790], 1.255 [0.100], 5.909 [0.109]

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10	19.24 [1.466], 1.212 [0.092], 9.112 [0.160]	19.12 [1.457], 1.204 [0.091], 9.054 [0.159]
For x=0 and at T	=77 K	
$N (10^{19} \text{ cm}^{-3})$		
3	4.044 [0.178], 1.081 [0.047], 3.216 [0.019]	4.008 [0.176], 1.074 [0.046], 3.190 [0.018]
5	7.188 [0.277], 1.035 [0.040], 4.651 [0.024]	7.133 [0.276], 1.029 [0.039], 4.618 [0.023]
10	14.75 [0.504], 0.986 [0.034], 7.391 [0.034]	14.65 [0.501], 0.980 [0.033], 7.342 [0.033]
For x=0.5 and at	T=77 K	
N (10 ¹⁹ cm ⁻³)		
3	5.061 [0.294], 1.156 [0.067], 3.689 [0.037]	5.025 [0.292], 1.149 [0.066], 3.664 [0.036]
5	8.447 [0.452], 1.114 [0.060], 5.128 [0.047]	8.390 [0.449], 1.107 [0.059], 5.094 [0.046]
10	16.62 [0.817], 1.066 [0.052], 7.936 [0.067]	16.51 [0.813], 1.059 [0.052], 7.885 [0.066]
For x=1 and at T	=77 K	
N (10 ¹⁹ cm ⁻³)		
3	6.095 [0.519], 1.308 [0.111], 4.341 [0.085]	6.056 [0.516], 1.300 [0.110], 4.314 [0.084]
5	9.942 [0.803], 1.264 [0.102], 5.949 [0.111]	9.878 [0.798], 1.256 [0.101], 5.911 [0.110]
10	19.25 [1.471], 1.212 [0.093], 9.114 [0.161]	19.12 [1.463], 1.205 [0.092], 9.056 [0.160]

Table 9n: For given x, r_d , T=(3K and 80K) and N, the numerical results of various thermoelectric coefficients: $\sigma_{Th.O[E]}$, $S_{O[E]}$, $VC1_{O[E]}$, $VC2_{O[E]}$, $Ts_{O[E]}$, $Pt_{O[E]}$ and $Tt_{O[E]}$, are obtained by using Equations (21, 25, 27, 28, 29, 30 and 26), respectively. Further, their variations with increasing r_d are represented by the arrows: \nearrow (increase), and \searrow (decrease).

Donor	As	Sb	Sn
For x=0 and N=3 \times 10 ¹⁸ cm ⁻³	,		
$\xi_{n(T=3K)} \qquad \qquad \searrow$	437.040 [378.719]	434.909 [376.872]	433.968 [376.056]
$\xi_{n(T=80K)} \qquad \searrow$	16.465 [14.290]	16.385 [14.221]	16.350 [14.190]
$\sigma_{Th.0[E]](3K)}\big(\frac{10^{-4}\times\!W}{cm\times\!K}\big)\qquad \searrow$	4.323 [3.402]	3.085 [2.444]	2.789 [2.214]
$\sigma_{Th.0[E]](80K)}\big(\frac{10^{-2}\times\!W}{cm\times\!K}\big)\qquad \searrow$	5.788 [4.070]	4.164 [2.947]	3.777 [2.679]
$-S_{O[E](3K)}\big(\frac{10^{-6}\!\times\!V}{K}\big)\qquad \searrow$	1.297 [1.497]	1.304 [1.504]	1.306 [1.508]
$-S_{O[E](80K)}\big(\frac{10^{-5}\times V}{K}\big) \searrow$	3.402 [3.905]	3.418 [3.923]	3.426 [3.931]
$-\text{VC1}_{0[E](3K)}\left(\frac{10^{-7}\times V}{K}\right)$	8.648 [9.980]	8.691 [10.029]	8.710 [10.051]
$-\text{VC1}_{\text{O[E] (80K)}}\left(\frac{10^{-5}\times\text{V}}{\text{K}}\right) \text{`} \text{`}$	2.193 [2.489]	2.203 [2.499]	2.207 [2.505]
$-\text{VC2}_{0[E](3K)}\big(\frac{10^{-6}\times V}{K}\big) \text{\searrow}$	2.594 [2.994]	2.607 [3.009]	2.613 [3.015]
$-\text{VC2}_{\text{O[E] (80K)}}\left(\frac{10^{-3}\times\text{V}}{\text{K}}\right) \text{`\searrow}$	1.755 [1.991]	1.762 [1.999]	1.766 [2.004]

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$-\operatorname{Ts}_{0[E](3K)}\left(\frac{10^{-6}\times V}{K}\right)$	1.297 [1.497]	1.304 [1.504]	1.306 [1.508]	
$-Ts_{O[E](80K)}\left(\frac{10^{-5}\times V}{K}\right)$	3.290 [3.734]	3.304 [3.749]	3.311 [3.757]	
$-Pt_{O[E](3K)}(10^{-6} \times V)$ \	3.892 [4.491]	3.911 [4.513]	3.919 [4.523]	
$-Pt_{0[E](80K)}(10^{-3} \times V)$ \	2.722 [3.124]	2.735 [3.138]	2.740 [3.145]	
$ZT_{O[E](3K)}(10^{-5})$	6.889 [9.174]	6.957 [9.265]	6.987 [9.305]	
$ZT_{O[E](80K)}(10^{-2})$	4.738 [6.242]	4.783 [6.300]	4.804 [6.326]	
For $x=0.5$ and $N=3 \times 10^{18}$ cm	1^{-3} , one has:			
$\xi_{n(T=3K)}$	422.123 [349.224]	420.051 [347.510]	419.136 [346.752]	
ξ _{n(T=80K)}	15.908 [13.191]	15.801 [13.127]	15.797 [13.099]	
$\sigma_{\text{Th.O[E]] (3K)}} \left(\frac{10^{-4} \times W}{\text{cm} \times \text{K}}\right)$	4.655 [3.390]	3.316 [2.436]	2.995 [2.206]	
$\sigma_{Th.O[E]] (80K)} \left(\frac{10^{-2} \times W}{cm \times K}\right)$	6.237 [4.064]	4.478 [2.943]	4.059 [2.675]	
$-S_{O[E](3K)}\left(\frac{10^{-6}\times V}{K}\right) \qquad \searrow$	1.343 [1.623]	1.350 [1.631]	1.353 [1.635]	
$-S_{O[E](80K)}\big(\frac{10^{-5}\times V}{K}\big) \searrow$	3.518 [4.218]	3.535 [4.238]	3.542 [4.247]	
$-VC1_{0[E](3K)}\left(\frac{10^{-7}\times V}{K}\right) \searrow$	8.954 [10.223]	8.998 [10.876]	9.018 [10.899]	
$-VC1_{0[E](80K)}\left(\frac{10^{-5}\times V}{K}\right) \checkmark$	2.262 [2.668]	2.272 [2.679]	2.277 [2.684]	
$-VC2_{0[E](3K)}\left(\frac{10^{-6}\times V}{K}\right) \searrow$	2.686 [3.247]	2.699 [3.263]	2.705 [3.270]	
$-VC2_{O[E](80K)}\left(\frac{10^{-3}\times V}{K}\right) \searrow$	1.810 [2.134]	1.818 [2.143]	1.821 [2.147]	
$-Ts_{O[E](3K)}\left(\frac{10^{-6}\times V}{K}\right) \searrow$	1.343 [1.623]	1.350 [1.631]	1.353 [1.635]	
$-\mathrm{Ts}_{\mathrm{O[E]}\;(80\mathrm{K})}\left(\frac{10^{-5}\times\mathrm{V}}{\mathrm{K}}\right)\;\;\;\searrow$	3.394 [4.002]	3.409 [4.019]	3.415 [4.020]	
$-Pt_{0[E](3K)}(10^{-6} \times V) \searrow$	4.029 [4.871]	4.049 [4.894]	4.058 [4.905]	
$-Pt_{0[E](80K)}(10^{-3} \times V)$ \	2.815 [3.375]	2.828 [3.390]	2.834 [3.398]	
$ZT_{O[E](3K)}(10^{-5})$	7.385 [10.789]	7.458 [10.896]	7.490 [10.944]	
$ZT_{O[E](80K)}(10^{-2})$	5.067 [7.284]	5.116 [7.353]	5.137 [7.383]	
For $x=1$ and $N=3 \times 10^{18}$ cm ⁻¹	³ , one has:			
$\xi_{n(T=3K)}$	421.188 [323.992]	419.108 [322.392]	418.189 [321.685]	
$\xi_{n(T=80K)}$	15.873 [12.253]	15.796 [12.193]	15.761 [12.167]	
$\sigma_{Th.O[E]](3K)} \left(\frac{10^{-4} \times W}{cm \times K}\right) \qquad \searrow$	5.247 [3.379]	3.726 [2.428]	3.362 [2.199]	
$\sigma_{\text{Th.O[E]] (80K)}} \left(\frac{10^{-2} \times W}{\text{cm} \times \text{K}}\right)$	7.031 [4.061]	5.033 [2.941]	4.558 [2.674]	
$-S_{0[E](3K)}\left(\frac{10^{-6}\times V}{K}\right) \qquad \searrow$	1.346 [1.750]	1.353 [1.759]	1.356 [1.762]	
$-S_{O[E](80K)}\big(\frac{10^{-5}\times V}{K}\big) \searrow$	3.526 [4.528]	3.543 [4.549]	3.550 [4.559]	
$-VC1_{0[E](3K)}\left(\frac{10^{-7}\times V}{K}\right) \searrow$	8.974 [11.665]	9.018 [11.723]	9.038 [11.749]	
$-VC1_{O[E](80K)}\left(\frac{10^{-5}\times V}{K}\right)$	2.267 [2.840]	2.277 [2.851]	2.281 [2.857]	

$-VC2_{0[E](3K)}\left(\frac{10^{-6}\times V}{K}\right)$	2.692 [3.399]	2.705 [3.517]	2.711 [3.525]
$-VC2_{0[E](80K)}\left(\frac{10^{-3}\times V}{K}\right)$	1.814 [2.272]	1.822 [2.281]	1.825 [2.285]
$-Ts_{0[E](3K)}\left(\frac{10^{-6}\times V}{K}\right)$ \searrow	1.346 [1.750]	1.353 [1.758]	1.356 [1.762]
$-Ts_{O[E](80K)}\left(\frac{10^{-5}\times V}{K}\right)$	3.401 [4.260]	3.416 [4.277]	3.422 [4.285]
$-\text{Pt}_{\text{O[E] (3K)}}(10^{-6} \times \text{V}) \text{`}$	4.038 [5.250]	4.058 [5.276]	4.067 [5.287]
$-\text{Pt}_{\text{O[E] (80K)}}(10^{-3} \times \text{V})$	2.821 [3.623]	2.834 [3.639]	2.840 [3.647]
$ZT_{O[E](3K)}(10^{-5})$	7.418 [12.535]	7.491 [12.660]	7.524 [12.716]
$ZT_{O[E](80K)}(10^{-2})$	5.089 [8.393]	5.138 [8.472]	5.160 [8.507]

Table 9p: For given x, r_a , T=(3K and 80K) and N, the numerical results of various thermoelectric coefficients: $\sigma_{Th.O[E]}$, $S_{O[E]}$, $VC1_{O[E]}$, $VC2_{O[E]}$, $Ts_{O[E]}$, $Pt_{O[E]}$ and $ZT_{O[E]}$, are obtained by using Equations (21, 25, 27, 28, 29, 30 and 26), respectively. Further, their variations with increasing r_a are represented by the arrows: \nearrow (increase), and \searrow (decrease).

Acceptor	Ga	Mg	In
For $x=0$ and $N=2.5 \times 10$	19 cm ⁻³ , one has:		
$\xi_{n(T=3K)}$	1534.82 [204.83]	1470.44 [196.23]	1466.76 [195.74]
$\xi_{n(T=80K)}$	57.577 [7.847]	55.164 [7.532]	55.026 [7.514]
$\sigma_{\text{Th.O[E]] (3K)}} \left(\frac{10^{-3} \times W}{\text{cm} \times \text{K}}\right) \qquad \Sigma$	2.834 [0.116]	2.386 [0.101]	2.346 [0.100]
$\sigma_{\text{Th.O[E]] (80K)}} \left(\frac{10^{-2} \times W}{\text{cm} \times \text{K}} \right)$	7.570 [0.339]	6.327 [0.298]	6.267 [0.296]
$-S_{O[E](3K)}\left(\frac{10^{-7}\times V}{K}\right) \qquad \searrow$	3.694 [27.679]	3.856 [28.891]	3.866 [28.96]
$-S_{O[E](80K)}\left(\frac{10^{-6}\times V}{K}\right) \searrow$	9.838 [68.593]	10.267 [71.150]	10.293 [71.302]
$-VC1_{O[E](3K)}\left(\frac{10^{-7}\times V}{K}\right) \searrow$	2.463 [18.449]	2.571 [19.256]	2.577 [19.304]
$-VC1_{O[E](80K)}\left(\frac{10^{-6}\times V}{K}\right) \searrow$	6.541 [39.317]	6.824 [40.256]	6.841 [40.310]
$-VC2_{O[E](3K)}\left(\frac{10^{-7}\times V}{K}\right) \searrow$	7.388 [55.347]	7.712 [57.768]	7.731 [57.913]
$-VC2_{O[E](80K)}\left(\frac{10^{-4}\times V}{K}\right) \searrow$	5.232 [31.454]	5.459 [32.205]	5.473 [32.248]
$-Ts_{O[E](3K)}\left(\frac{10^{-7}\times V}{K}\right) \searrow$	3.694 [27.673]	3.856 [28.884]	3.865 [28.957]
$-\operatorname{Ts}_{O[E](80K)}\left(\frac{10^{-6}\times V}{K}\right)$	9.811 [58.976]	10.237 [60.385]	10.262 [60.465]
$-Pt_{0[E](3K)}(10^{-6} \times V) \searrow$	1.108 [8.304]	1.157 [8.667]	1.160 [8.689]
$-Pt_{0[E](80K)}(10^{-4} \times V)$ \	7.870 [54.874]	8.214 [56.920]	8.234 [57.041]
$ZT_{O[E](3K)}(10^{-6})$	5.586 [313.62]	6.086 [341.67]	6.117 [343.39]
$ZT_{O[E](80K)}(10^{-3})$	3.962 [192.59]	4.315 [207.22]	4.337 [208.11]
For x=0.5 and N=2.5 × 1	10 ¹⁹ cm ⁻³ one has:		
$\xi_{n(T=3K)}$	1641.67 [283.52]	1617.95 [279.42]	1616.61 [279.19]

$\xi_{n(T=80K)}$	61.583 [10.750]	60.694 [10.598]	60.643 [10.590]
$\sigma_{\text{Th.O[E]] (3K)}} \left(\frac{10^{-3} \times W}{\text{cm} \times \text{K}}\right) \qquad \forall$	3.535 [0.198]	3.070 [0.177]	3.048 [0.176]
$\sigma_{\text{Th.O[E]] (80K)}} \left(\frac{10^{-2} \times W}{\text{cm} \times \text{K}}\right)$	9.441 [0.554]	8.200 [0.496]	8.140 [0.493]
$-S_{0[E](3K)}\left(\frac{10^{-7}\times V}{K}\right) \qquad \searrow$	3.454 [19.997]	3.504 [20.291]	3.507 [20.307]
$-S_{0[E](80K)}\left(\frac{10^{-6}\times V}{K}\right) \vee$	9.199 [51.283]	9.333 [51.976]	9.341[52.015]
$-VC1_{0[E](3K)}\left(\frac{10^{-7}\times V}{V}\right) \searrow$	2.302 [13.330]	2.336 [13.525]	2.338 [13.537]
$-VC1_{O[E] (80K)} \left(\frac{10^{-6} \times V}{\kappa}\right) $	6.118 [31.572]	6.207 [31.924]	6.212 [31.944]
$-VC2_{O[E](3K)}\left(\frac{10^{-7}\times V}{K}\right) \qquad \searrow$	6.907 [39.990]	7.009 [40.577]	7.014 [40.610]
••			
$-VC2_{O[E](80K)}\left(\frac{10^{-4}\times V}{K}\right) \searrow$	4.894 [25.257]	4.965 [25.539]	4.970 [25.555]
$-\mathrm{Ts}_{\mathrm{O[E]}(3\mathrm{K})}\left(\frac{10^{-7}\times\mathrm{V}}{\mathrm{K}}\right) V$	3.454 [19.995]	3.504 [20.288]	3.507 [20.305]
$-Ts_{0[E](80K)}\left(\frac{10^{-6}\times V}{K}\right)$	9.177 [47.358]	9.310 [47.886]	9.318 [47.916]
$-Pt_{0[E](3K)}(10^{-6} \times V)$ \	1.036 [5.999]	1.051 [6.087]	1.052 [6.092]
$-\text{Pt}_{\text{O[E] (80K)}}(10^{-4}\times\text{V}~)~~\searrow$	7.359 [41.026]	7.466 [41.580]	7.473 [41.612]
$ZT_{0[E](3K)}(10^{-6})$	4.883 [163.69]	5.027 [168.53]	5.035 [168.81]
$ZT_{O[E](80K)}(10^{-3})$	3.464 [107.65]	3.566 [110.58]	3.572 [110.75]
For x=1 and N=2.5 \times 10 ¹⁹ cm	1 ⁻³ one has:		
$\xi_{n(T=3K)}$	1706.86 [393.893]	1699.02 [392.084]	1698.58 [391.982]
$\xi_{n(T=80K)}$	64.026 [14.855]	63.733 [14.788]	63.716 [14.784]
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$\sigma_{\text{Th.O[E]] (3K)}} \left(\frac{10^{-3} \times W}{\text{cm} \times \text{K}} \right) \qquad \searrow$	4.253 [0.354]	3.743 [0.318]	3.718 [0.316]
$\begin{array}{ll} \sigma_{Th.0[E]](3K)}(\frac{10^{-3}\times W}{cm\times K}) & \searrow \\ \\ \sigma_{Th.0[E]](80K)}(\frac{10^{-2}\times W}{cm\times K}) & \searrow \end{array}$	4.253 [0.354] 11.357 [0.971]	3.743 [0.318] 9.995 [0.871]	3.718 [0.316] 9.930 [0.866]
$\sigma_{Th.0[E]](80K)} \left(\frac{10^{-2} \times W}{cm \times K}\right)$	11.357 [0.971]	9.995 [0.871]	9.930 [0.866]
$\sigma_{\text{Th.O[E]] (80K)}} \left(\frac{10^{-2} \times W}{\text{cm} \times K} \right) \qquad \searrow$ $-S_{\text{O[E] (3K)}} \left(\frac{10^{-7} \times V}{K} \right) \qquad \searrow$ $-S_{\text{O[E] (80K)}} \left(\frac{10^{-6} \times V}{K} \right) \qquad \searrow$	11.357 [0.971] 3.322 [14.394]	9.995 [0.871] 3.337 [14.461]	9.930 [0.866] 3.338 [14.464]
$\sigma_{\text{Th.O[E]] (80K)}} \left(\frac{10^{-2} \times W}{\text{cm} \times K} \right) \qquad \searrow$ $-S_{O[E] (3K)} \left(\frac{10^{-7} \times V}{K} \right) \qquad \searrow$	11.357 [0.971] 3.322 [14.394] 8.848 [37.607]	9.995 [0.871] 3.337 [14.461] 8.889 [37.773]	9.930 [0.866] 3.338 [14.464] 8.891 [37.783]
$\begin{array}{l} \sigma_{\text{Th.O[E]] (80K)}} \left(\frac{10^{-2} \times W}{\text{cm} \times K} \right) & \searrow \\ -S_{O[E] (3K)} \left(\frac{10^{-7} \times V}{K} \right) & \searrow \\ -S_{O[E] (80K)} \left(\frac{10^{-6} \times V}{K} \right) & \searrow \\ -VC1_{O[E] (3K)} \left(\frac{10^{-7} \times V}{K} \right) & \searrow \\ -VC1_{O[E] (80K)} \left(\frac{10^{-6} \times V}{K} \right) & \searrow \end{array}$	11.357 [0.971] 3.322 [14.394] 8.848 [37.607] 2.214 [9.595]	9.995 [0.871] 3.337 [14.461] 8.889 [37.773] 2.225 [9.639]	9.930 [0.866] 3.338 [14.464] 8.891 [37.783] 2.226 [9.642]
$\begin{array}{l} \sigma_{\text{Th.O[E]] (80K)}} \left(\frac{10^{-2} \times W}{\text{cm} \times K} \right) \qquad \searrow \\ \\ -S_{O[E] (3K)} \left(\frac{10^{-7} \times V}{K} \right) \qquad \searrow \\ \\ -S_{O[E] (80K)} \left(\frac{10^{-6} \times V}{K} \right) \qquad \searrow \\ \\ -VC1_{O[E] (3K)} \left(\frac{10^{-7} \times V}{K} \right) \qquad \searrow \end{array}$	11.357 [0.971] 3.322 [14.394] 8.848 [37.607] 2.214 [9.595] 5.886 [24.055]	9.995 [0.871] 3.337 [14.461] 8.889 [37.773] 2.225 [9.639] 5.913 [24.152]	9.930 [0.866] 3.338 [14.464] 8.891 [37.783] 2.226 [9.642] 5.914 [24.158]
$\begin{array}{l} \sigma_{\text{Th.O[E]] (80K)}}\left(\frac{10^{-2}\times W}{\text{cm}\times K}\right) \qquad \searrow \\ -S_{O[E] (3K)}\left(\frac{10^{-7}\times V}{K}\right) \qquad \searrow \\ -S_{O[E] (80K)}\left(\frac{10^{-6}\times V}{K}\right) \qquad \searrow \\ -VC1_{O[E] (3K)}\left(\frac{10^{-7}\times V}{K}\right) \qquad \searrow \\ -VC2_{O[E] (80K)}\left(\frac{10^{-6}\times V}{K}\right) \qquad \searrow \\ -VC2_{O[E] (3K)}\left(\frac{10^{-7}\times V}{K}\right) \qquad \searrow \end{array}$	11.357 [0.971] 3.322 [14.394] 8.848 [37.607] 2.214 [9.595] 5.886 [24.055] 6.644 [28.787]	9.995 [0.871] 3.337 [14.461] 8.889 [37.773] 2.225 [9.639] 5.913 [24.152] 6.674 [28.919]	9.930 [0.866] 3.338 [14.464] 8.891 [37.783] 2.226 [9.642] 5.914 [24.158] 6.676 [28.927]
$\begin{array}{l} \sigma_{\text{Th.O[E]] (80K)}}\left(\frac{10^{-2}\times W}{\text{cm}\times K}\right) & \searrow \\ -S_{O[E] (3K)}\left(\frac{10^{-7}\times V}{K}\right) & \searrow \\ -S_{O[E] (80K)}\left(\frac{10^{-6}\times V}{K}\right) & \searrow \\ -VC1_{O[E] (3K)}\left(\frac{10^{-7}\times V}{K}\right) & \searrow \\ -VC2_{O[E] (80K)}\left(\frac{10^{-6}\times V}{K}\right) & \searrow \\ -VC2_{O[E] (80K)}\left(\frac{10^{-7}\times V}{K}\right) & \searrow \\ -VC2_{O[E] (80K)}\left(\frac{10^{-7}\times V}{K}\right) & \searrow \end{array}$	11.357 [0.971] 3.322 [14.394] 8.848 [37.607] 2.214 [9.595] 5.886 [24.055] 6.644 [28.787] 4.708 [19.244]	9.995 [0.871] 3.337 [14.461] 8.889 [37.773] 2.225 [9.639] 5.913 [24.152] 6.674 [28.919] 4.730 [19.322]	9.930 [0.866] 3.338 [14.464] 8.891 [37.783] 2.226 [9.642] 5.914 [24.158] 6.676 [28.927] 4.732 [19.326]
$\begin{array}{l} \sigma_{\text{Th.O[E]] (80K)}}\left(\frac{10^{-2}\times W}{\text{cm}\times K}\right) \qquad \searrow \\ -S_{O[E] (3K)}\left(\frac{10^{-7}\times V}{K}\right) \qquad \searrow \\ -S_{O[E] (80K)}\left(\frac{10^{-6}\times V}{K}\right) \qquad \searrow \\ -VC1_{O[E] (3K)}\left(\frac{10^{-7}\times V}{K}\right) \qquad \searrow \\ -VC2_{O[E] (80K)}\left(\frac{10^{-6}\times V}{K}\right) \qquad \searrow \\ -VC2_{O[E] (80K)}\left(\frac{10^{-7}\times V}{K}\right) \qquad \searrow \\ -VC3_{O[E] (3K)}\left(\frac{10^{-7}\times V}{K}\right) \qquad \searrow \\ -VC3$	11.357 [0.971] 3.322 [14.394] 8.848 [37.607] 2.214 [9.595] 5.886 [24.055] 6.644 [28.787] 4.708 [19.244] 3.322 [14.393]	9.995 [0.871] 3.337 [14.461] 8.889 [37.773] 2.225 [9.639] 5.913 [24.152] 6.674 [28.919] 4.730 [19.322] 3.337 [14.459]	9.930 [0.866] 3.338 [14.464] 8.891 [37.783] 2.226 [9.642] 5.914 [24.158] 6.676 [28.927] 4.732 [19.326] 3.338 [14.464]
$\begin{array}{l} \sigma_{\text{Th.O[E]] (80K)}}\left(\frac{10^{-2}\times W}{\text{cm}\times K}\right) \qquad \searrow \\ -S_{O[E] (3K)}\left(\frac{10^{-7}\times V}{K}\right) \qquad \searrow \\ -S_{O[E] (80K)}\left(\frac{10^{-6}\times V}{K}\right) \qquad \searrow \\ -VC1_{O[E] (3K)}\left(\frac{10^{-7}\times V}{K}\right) \qquad \searrow \\ -VC2_{O[E] (80K)}\left(\frac{10^{-6}\times V}{K}\right) \qquad \searrow \\ -VC2_{O[E] (80K)}\left(\frac{10^{-7}\times V}{K}\right) \qquad \searrow \\ -TS_{O[E] (3K)}\left(\frac{10^{-7}\times V}{K}\right) \qquad \searrow \\ -TS_{O[E] (80K)}\left(\frac{10^{-7}\times V}{K}\right) \qquad \searrow \\ -TS_{O[E] (80K)}\left(\frac{10^{-6}\times V}{K}\right) \qquad \searrow \\ \end{array}$	11.357 [0.971] 3.322 [14.394] 8.848 [37.607] 2.214 [9.595] 5.886 [24.055] 6.644 [28.787] 4.708 [19.244] 3.322 [14.393] 8.829 [36.083]	9.995 [0.871] 3.337 [14.461] 8.889 [37.773] 2.225 [9.639] 5.913 [24.152] 6.674 [28.919] 4.730 [19.322] 3.337 [14.459] 8.869 [36.229]	9.930 [0.866] 3.338 [14.464] 8.891 [37.783] 2.226 [9.642] 5.914 [24.158] 6.676 [28.927] 4.732 [19.326] 3.338 [14.464] 8.872 [36.237]

Table 10: Here, in the O-EP [E-OP] and for given physical conditions: x, $r_{d(a)}$, N (or T), the same values of $\xi_{n(p)}$ decrease, according to the increasing T (or to the decreasing N), and other thermoelectric coefficients are in variations, as indicated by the arrows as: (increase: \nearrow , decrease: \searrow). One notes here that (i) for $\xi_{n(p)} \simeq 1.8138$, while the numerical results of $S_{O[E]}$ present a same minimum $S_{O[E]\min}\left(\simeq -1.563\times 10^{-4}\frac{V}{K}\right)$, those of $ZT_{O[E]}$ show a same maximum $ZT_{O[E]\max}=1$, (ii) for $\xi_p=1$, those of $S_{O[E]}$, $ZT_{O[E]}$, $ZT_{O[E]Mott}$, $VC1_{E[O]}$, and $Ts_{O[E]}$ present the same results: $-1.322\times 10^{-4}\frac{V}{K}$, 0.715, 3.290, $1.105\times 10^{-4}\frac{V}{K}$, and $1.657\times 10^{-4}\frac{V}{K}$, respectively, and (iii) for $\xi_p\simeq 1.8138$, $(ZT)_{O[E]Mott}=1$.

$\xi_{n(p)}$	1.880 [1.880]	1.8138 [1.8138]	1.750 [1.750]	1 [1]	0.998 [0.998]
$S_{O[E]}\left(10^{-4}\frac{V}{K}\right)$	-1.562 [-1.562] 💃	-1.563 [-1.563]	→ -1.562 [-1.562]	→ -1.322 [-1.322]	7 −1.320 [−1.320]
$\mathrm{ZT}_{\mathrm{O[E]}}$	0.999 [0.999] 🗷	1 [1]	▶ 0.999 [0.999]	> 0.715 [0.715]	> 0.713 [0.713]
$(ZT)_{O[E] Mott}$ /	0.931 [0.931]	1 [1]	1.074 [1.074]	3.290 [3.290]	3.306 [3.306]
$VC1_{E[O]} \left(10^{-4} \frac{V}{K} \right)$	-0.061[-0.061] 7	0 [0]	7 0.063 [0.063]	→ 1.105 [1.105]	7 1.109 [1.109]
$Ts_{O[E]}\left(10^{-4}\frac{V}{K}\right)$	-0.092 [-0.092]	0 [0]	7 0.094 [0.094]	↑ 1.657 [1.657]	7 1.663 [1.663]